

CP Violation: Past, Present, and Future

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“Towards Storage Ring Electric Dipole Measurements”

WE-Heraus Seminar

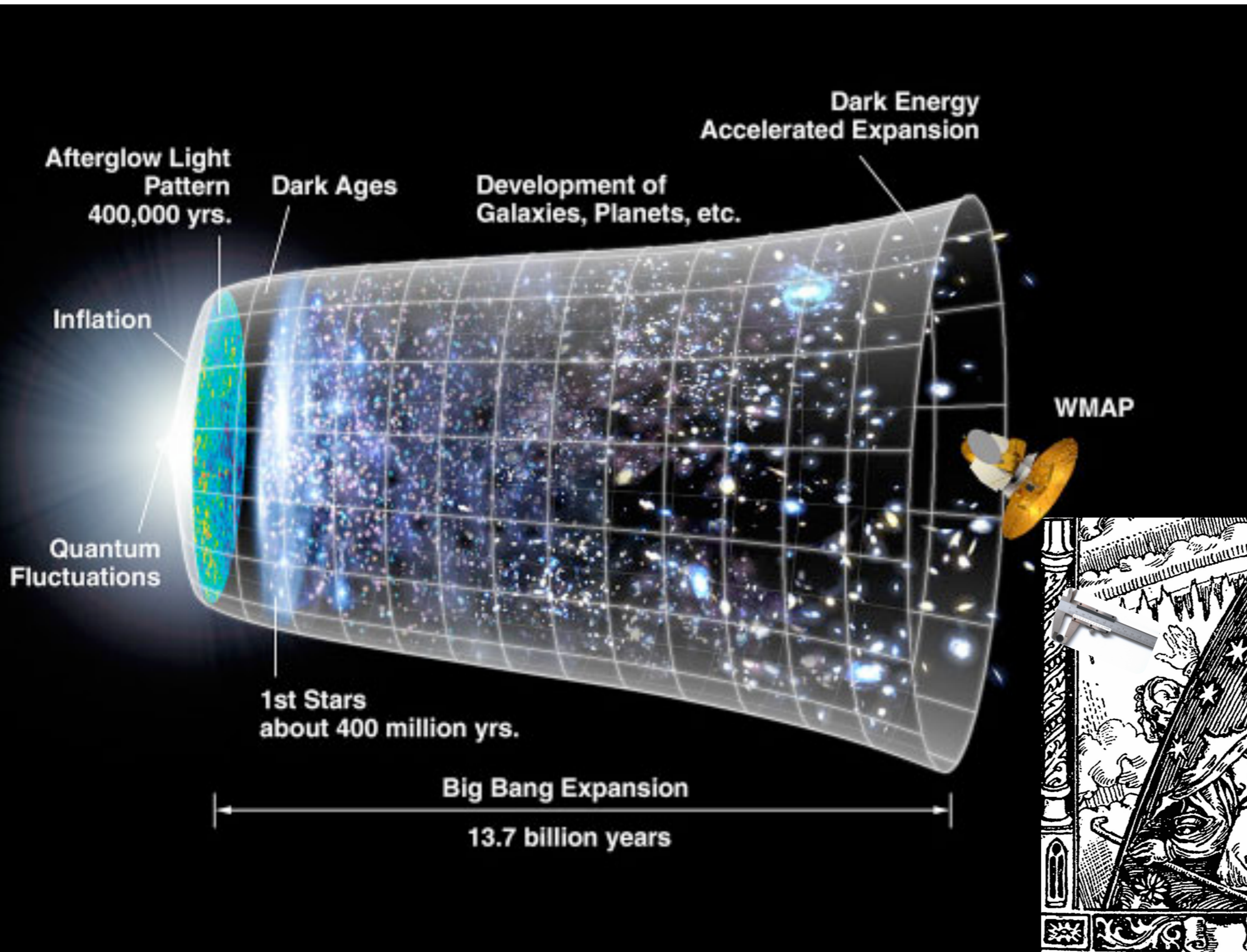
Bad Honnef

[March 29-31, 2021]



A Matter-Dominated Universe?

Precision Measurements of CP Violation Constrain its Mechanism



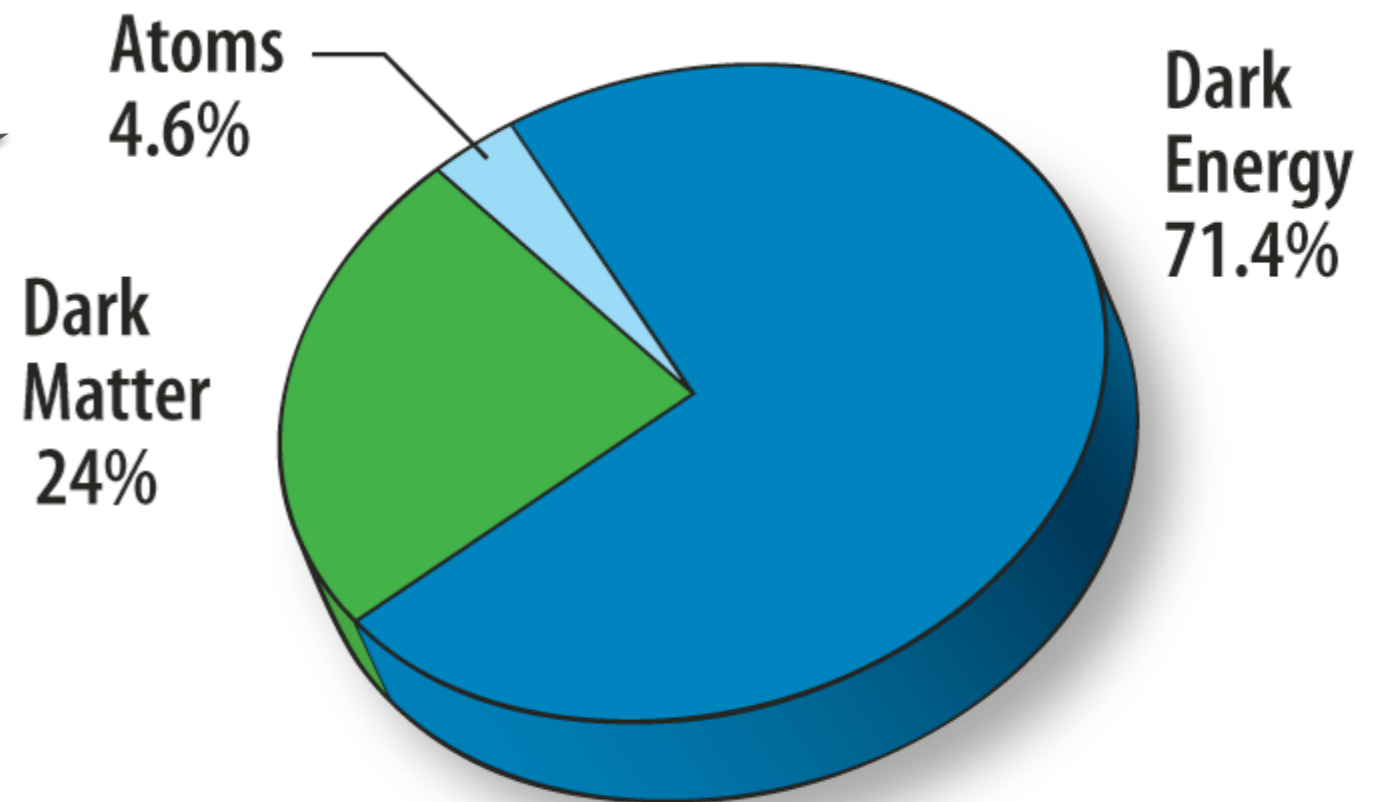
[after C. Flammarion, 1888]

http://www.nasa.gov/vision/universe/starsgalaxies/wmap_pol.html

Three Puzzles

Drive new physics searches

Why is the cosmic energy budget in baryons so small? (and what is everything else?!) →



[NASA]

And the cosmic baryon asymmetry

$$\eta = n_{\text{baryon}}/n_{\text{photon}} = (5.96 \pm 0.28) \times 10^{-10} \quad \text{TODAY} \quad \text{[Steigman, 2012]}$$

so large?

And why is the neutrino mass so very small?

$$m_\nu < 1.1 \text{ eV (90 \% CL)} \quad \text{[KATRIN, 2019]}$$

A Cosmic Baryon Asymmetry

Confronting the observed D/H abundance with big-bang nucleosynthesis yields a baryon asymmetry: [Steigman, 2012]

$$\eta = n_{\text{baryon}}/n_{\text{photon}} = (5.96 \pm 0.28) \times 10^{-10}$$

By initial condition?

We interpret the CMB in terms of an inflationary model, so that this seems unlikely. [Krnjaic, PRD 96 (2017)]

From particle physics?

The particle physics of the early universe can explain this asymmetry if B, C, and CP violation exists in a non-equilibrium environment. [Sakharov, 1967]

Non-equilibrium dynamics are required to avoid “washout” of an asymmetry by back reactions

The Puzzle of the Missing Antimatter

The baryon asymmetry of the universe (BAU) derives from physics beyond the standard model!

The SM almost has the right ingredients:

B? Yes, at high temperatures

C and **CP?** Yes, but CP is “special”

Early numerical estimates are much too small.

[Farrar and Shaposhnikov, 1993; Gavela et al., 1994; Huet and Sather, 1995.]

Non-equilibrium dynamics? No. (!)

$\eta < 10^{-26}$

The Higgs particle is too massive to yield a first-order electroweak phase transition

[e.g., Aoki, Csikor, Fodor, Ukawa, 1999]

So that the SM mechanism fails altogether

And we seek new sources of CP violation....

Recipes for a Baryon Asymmetry?

The BAU derives from physics beyond the standard model!

What new mechanisms are possible?

There are **many** & very probably more to discover

What are the ingredients? Well...

It could involve weak scale supersymmetry.

→ Probe new CPV phases through permanent EDM searches

It could involve an lepton asymmetry that is transferred to baryons — or involve a post-sphaleron baryogenesis mechanism.

→ Discover fundamental Majorana dynamics through discovery of $0\nu\beta\beta$ decay or of $n\bar{n}$ oscillations

It could involve a dark matter particle asymmetry that is transferred to baryons.

→ Discover a dark magnetic moment

(Faraday rotation for light asymmetric DM [SG 2008, 2009]; or DM direct detection...)

On CP Violation (with quarks)

Timeline and definitions

[Bennett, BELLE2-TALK-CONF-2017-094]

How CP can be violated...

in decay:

$$\left| \frac{\bar{A}_f}{A_f} \right| \neq 1$$

in mixing:

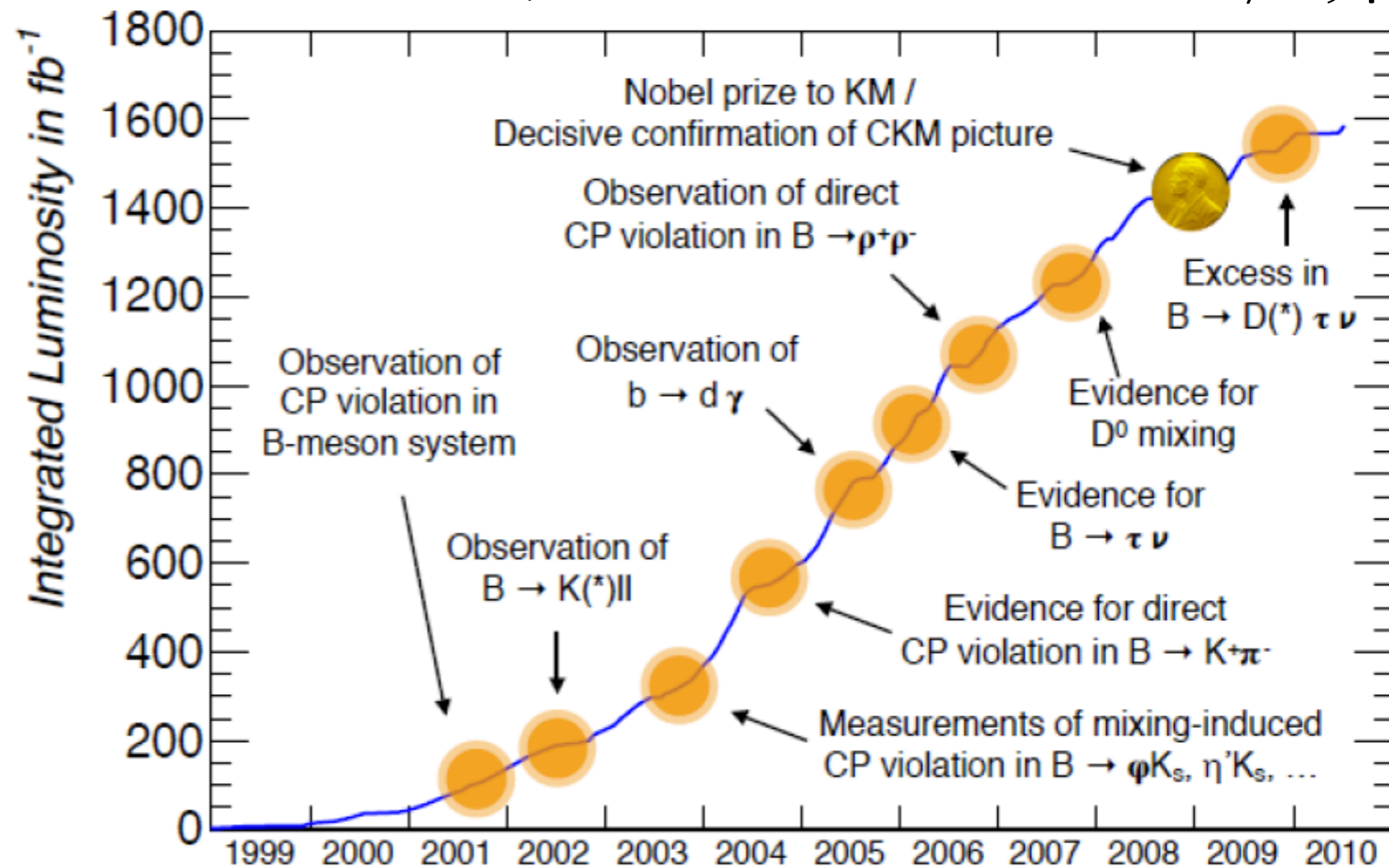
$$\left| \frac{q}{p} \right| \neq 1$$

in interference between mixing & decay:

cf. $M_0 \rightarrow f$ and $M_0 \rightarrow \bar{M}_0 \rightarrow f$

$$\arg(\lambda_f) + \arg(\lambda_{\bar{f}}) \neq 0$$

$$\lambda_f \equiv \frac{q}{p} \frac{\bar{A}_f}{A_f}$$



$$\Re\left(\frac{\epsilon'}{\epsilon}\right) \neq 0 \text{ [KTeV, NA48, 1999]}$$

$$\Gamma(K_L \rightarrow \pi\pi) \neq 0 \text{ [Christensen et al., 1964]; } \epsilon \neq 0$$

Large CPV effects possible in the B system!

7 [Bigi and Sanda; Carter, Dunietz... 1980's]

CP violation in the SM

Observed effects appear through quark mixing
under the weak interaction

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}_{\text{weak}} = V_{\text{CKM}} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{\text{mass}} ; \quad V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

The Cabibbo-Kobayashi-Maskawa (CKM) matrix is a unitary 3x3 matrix with 4 parameters in the Standard Model

$$V_{\text{CKM}} = \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4) \quad \text{[Wolfenstein, 1983]}$$

Quark mixing is hierarchical: $\lambda \simeq 0.2$ & $\eta \neq 0$ (CPV)!

The CKM matrix describes **all** flavor and CP violation **observed** in charged-current processes...

Observed CP violation in the SM

Testing the **Relationships** [L. Wolfenstein (Kaon '99)]

Enter “the” unitarity triangle — each term of $\mathcal{O}(\lambda^3)$

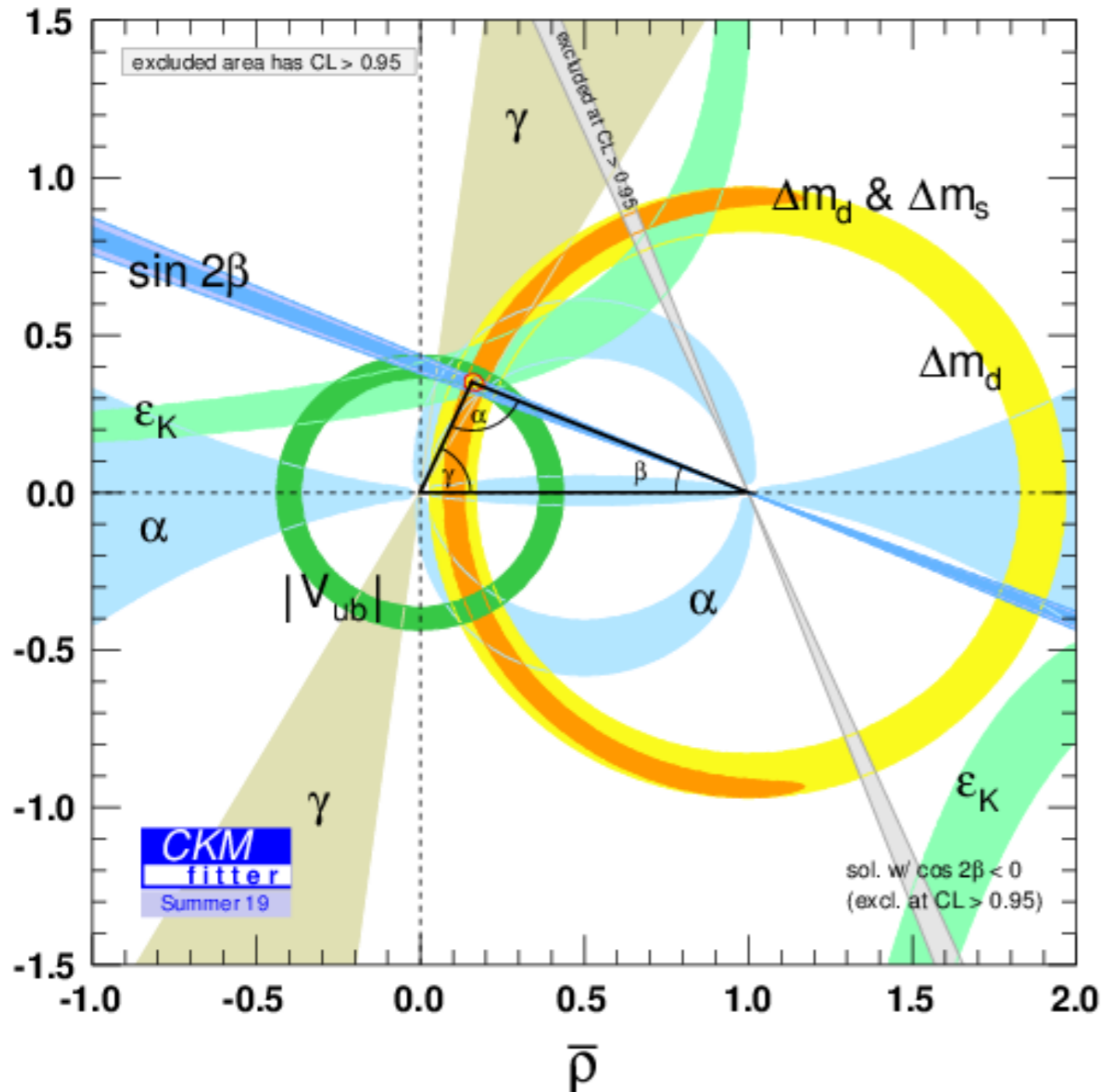
Are $\bar{\eta}$ and $\bar{\rho}$ universal?

Is the CKM matrix unitary?

cf. CPV (yes?)
to CP conserving (no?!)
tests...

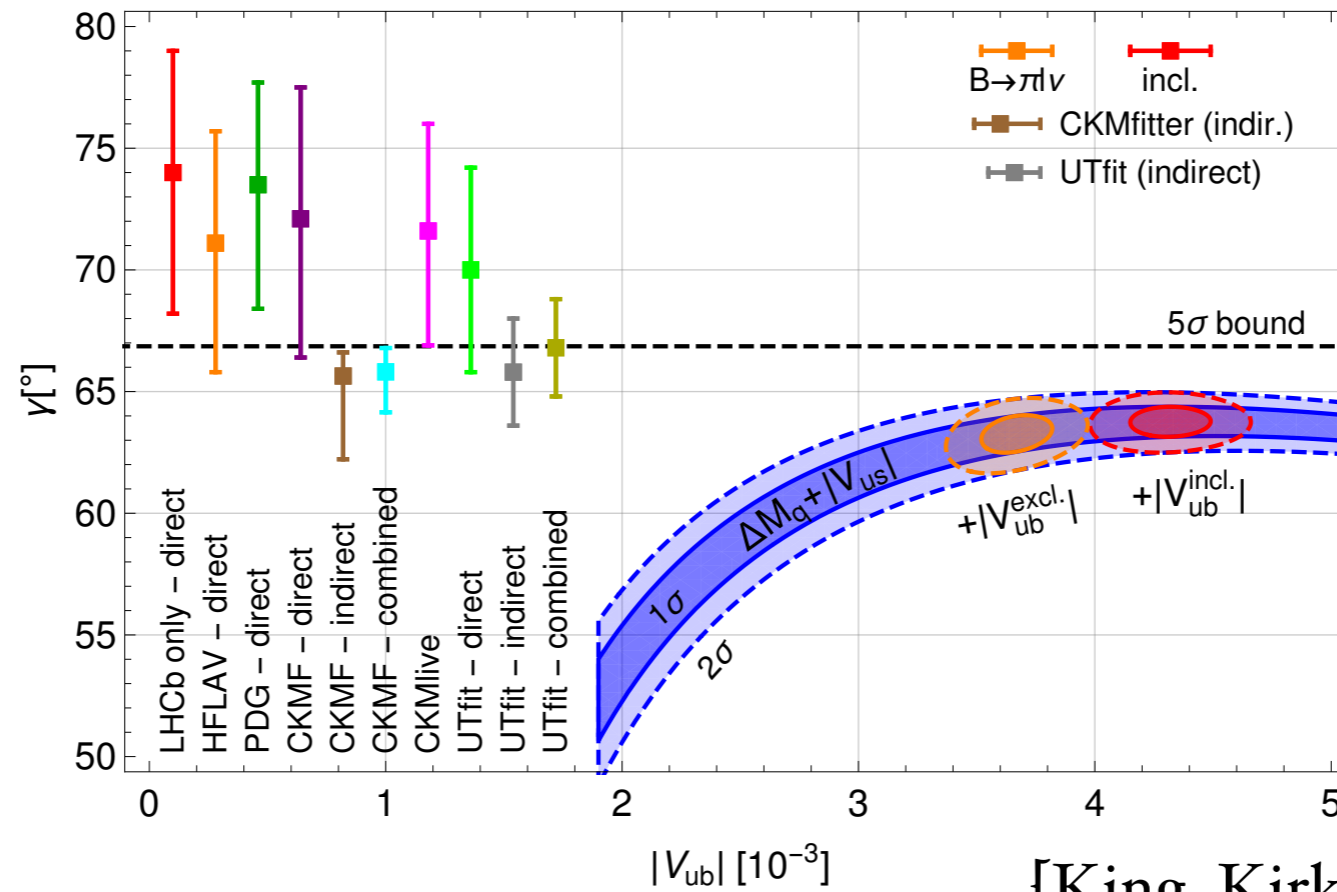
Expect much improved tests from LHCb & Belle II!

N.B. lattice QCD plays a key role!

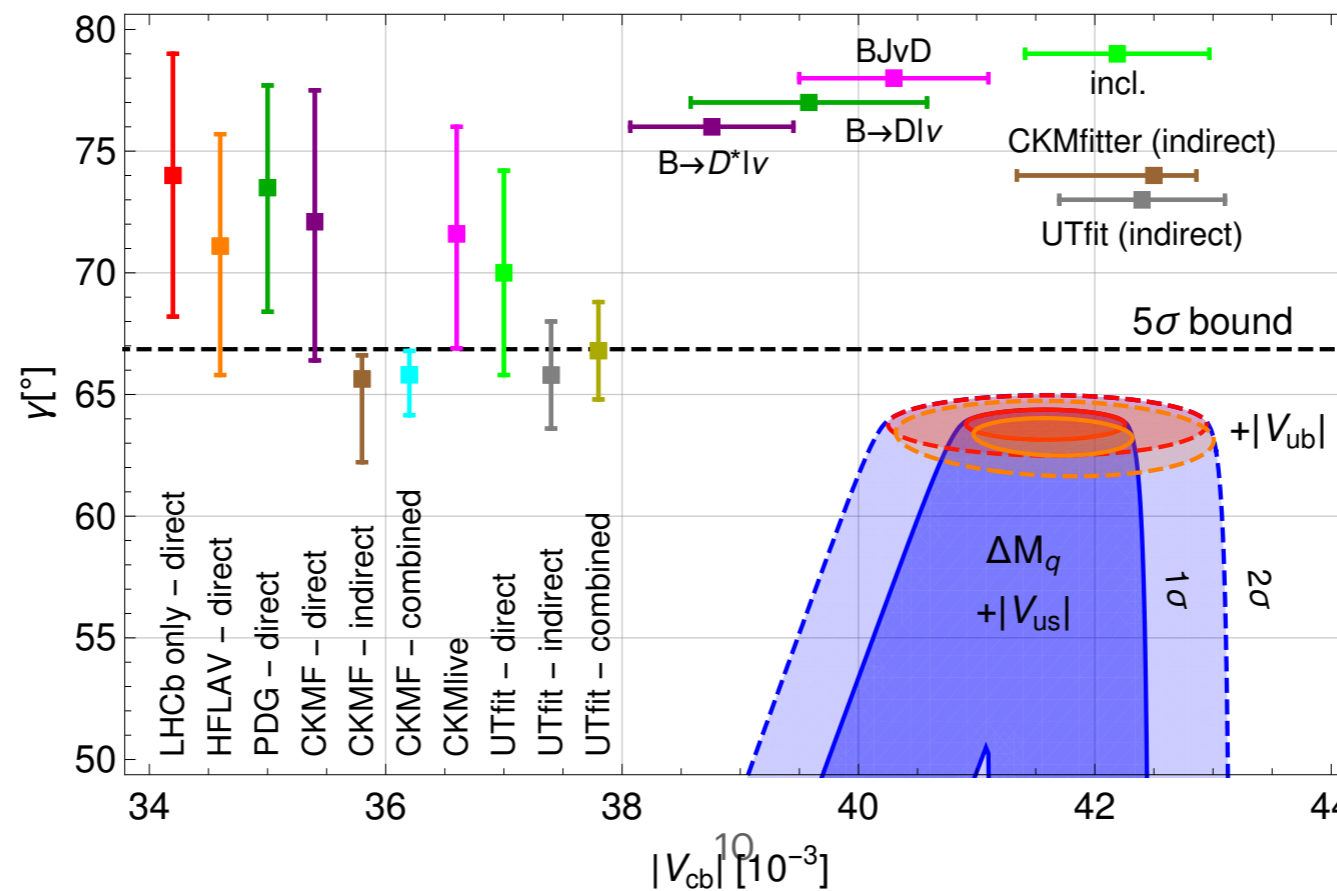


[CKM Fitter: Charles et al., 1501.05013]

Stress Testing the Relationships



[King, Kirk, Lenz, & Rauh, 1911.07856]

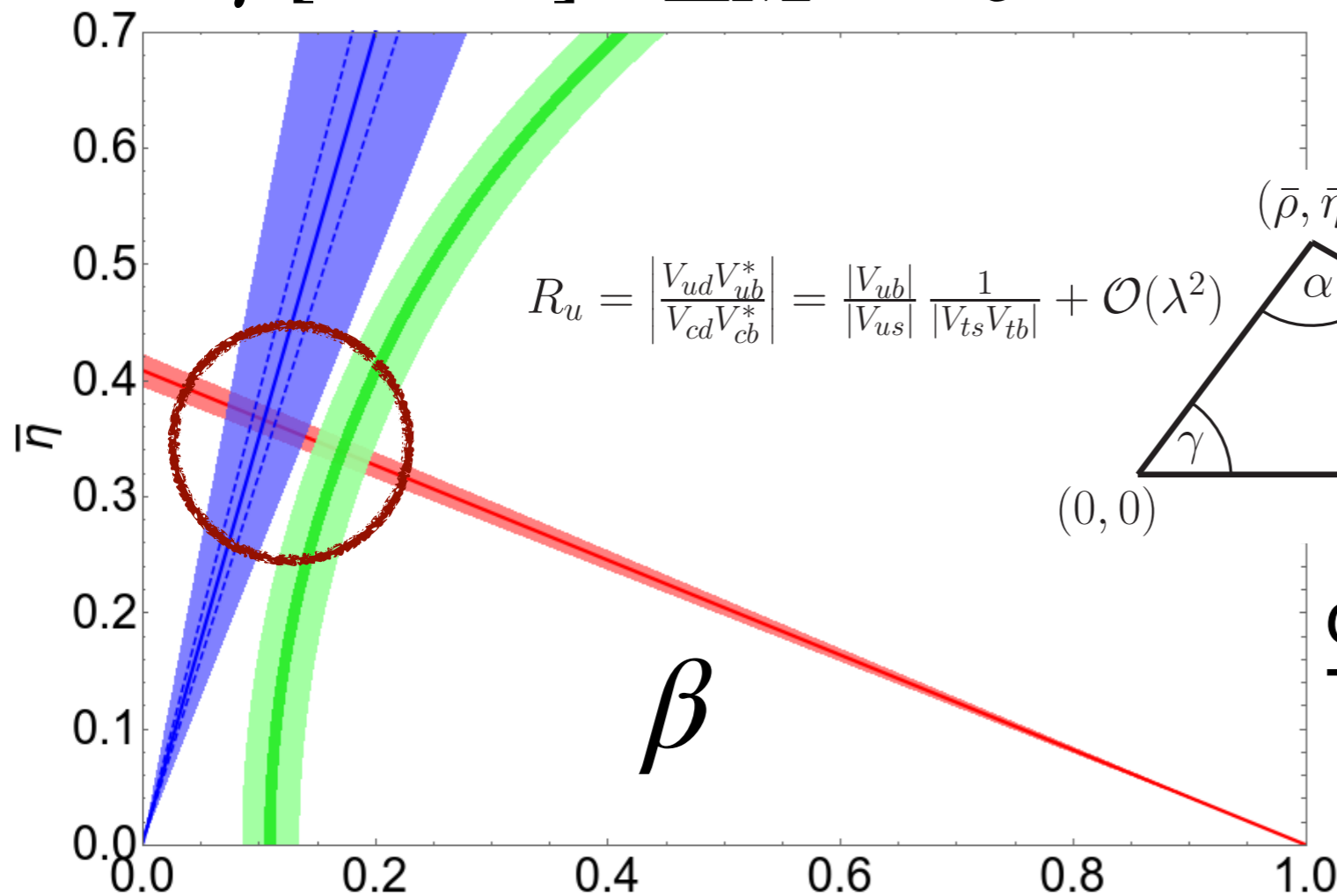


Note reliance on $|V_{us}|$
[PDG 2018]

Stress Testing the Relationships

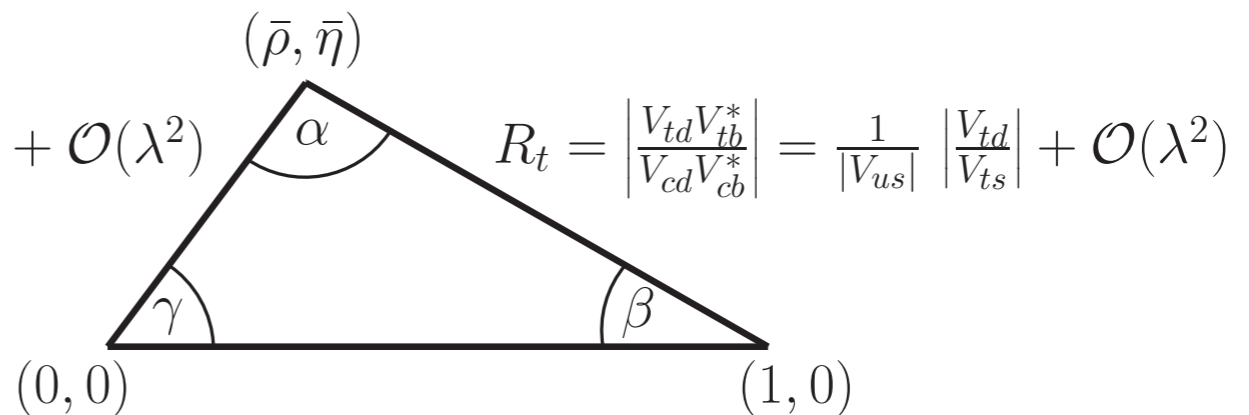
Are $\bar{\eta}$ and $\bar{\rho}$ universal? Is the CKM matrix unitary?

γ [LHCb]* ΔM [King et al., 1911.07856; also Blanke and Buras, 2019]



$$R_u = \left| \frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right| = \frac{|V_{ub}|}{|V_{us}|} \frac{1}{|V_{ts}V_{tb}|} + \mathcal{O}(\lambda^2)$$

Note “apex” study:



cf. sides to angles...

The triangle may not close?

* $\gamma = (67 \pm 4)^\circ$ [LHCb $\bar{\rho}$ - CONF - 2020 - 003]

Is β universal? Study penguin-dominated β modes...
 $B \rightarrow \eta' K_S, \phi K_S$ (SM effects in QCDf) [Belle II]

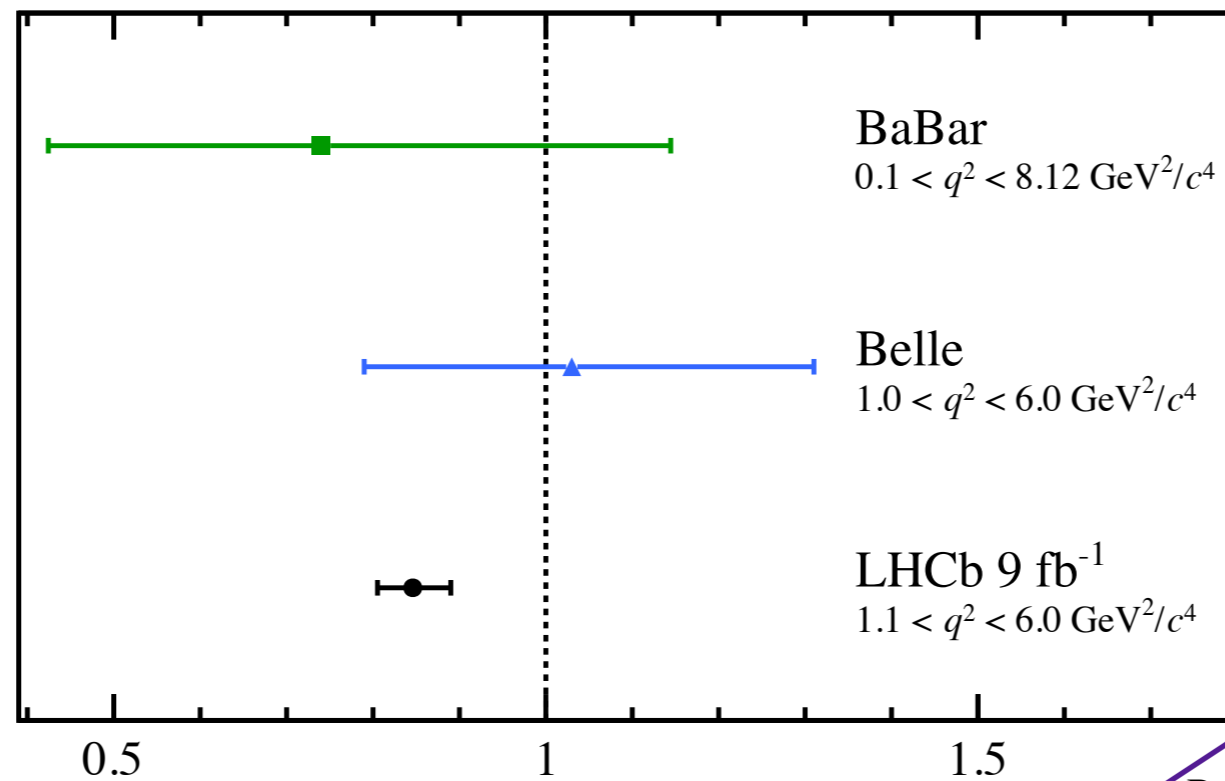
Note also CPC test: [Seng et al.¹¹, 2020] $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 \neq 1$ (!)

Stress Testing the Relationships

Does lepton flavor universality (LFU) hold?

$$R_K = \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow J/\psi (\rightarrow \mu^+ \mu^-) K^+)} \bigg/ \frac{\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)}{\mathcal{B}(B^+ \rightarrow J/\psi (\rightarrow e^+ e^-) K^+)}$$

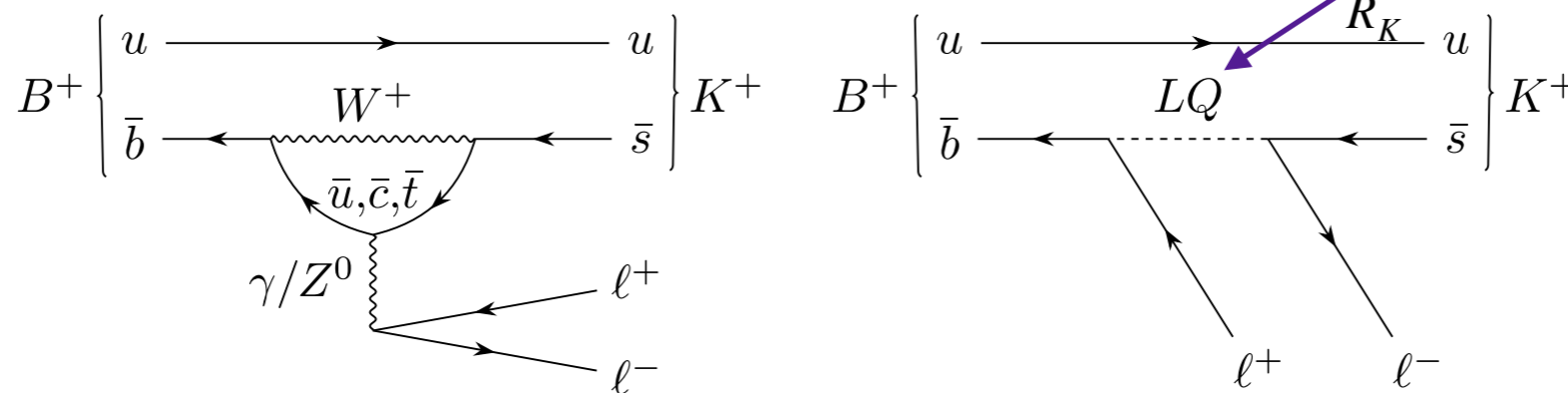
$\sim 3.1 \sigma$
Anomaly



[LHCb, 2103.11769]

N.B. also $R_{D^{(*)}}$ anomalies at similar significance... further studies planned at Belle II

“Leptoquark”



Now turn to lepton moments; hints of LFU violation?

Electric & Magnetic Dipole Moments

A permanent EDM breaks parity (P) & time-reversal (T)

$$\mathcal{H} = -\vec{\mu} \cdot \vec{B} - \vec{d} \cdot \vec{E}$$

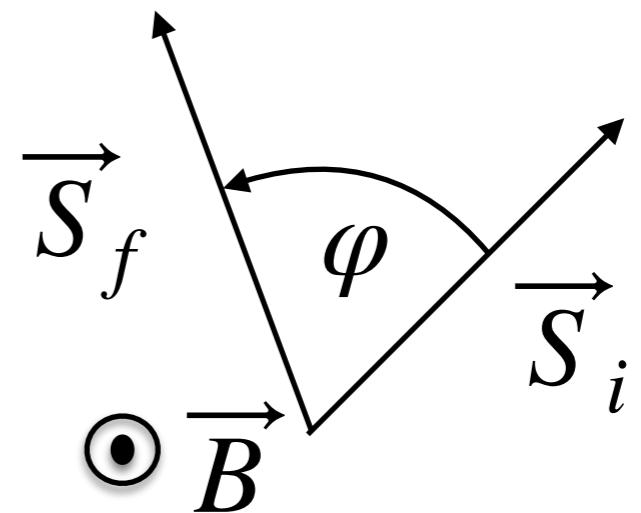
Intrinsic property: $\vec{\mu}, \vec{d} \propto \vec{S}$ [spin]

Maxwell Equations... $-\vec{\mu} \cdot \vec{B}$ is P even, T even
 $-\vec{d} \cdot \vec{E}$ is P odd, T odd

Note if T is broken so is CP [CPT unbroken]

Classically, the spin precesses if there is a torque:

$$\vec{\tau} = \frac{d\vec{S}}{dt} = \vec{\mu} \times \vec{B}$$



Electric & Magnetic Dipole Moments

Taken relativistically for fermion f with charge $-e$

$$\mathcal{H} = e\bar{\psi}_f\gamma^\mu\psi_f A_\mu + a_f\frac{1}{4}\bar{\psi}_f\sigma^{\mu\nu}\psi_f F_{\mu\nu} + d_f\frac{i}{2}\bar{\psi}_f\sigma^{\mu\nu}\gamma_5\psi_f F_{\mu\nu}$$

photon field A_μ $F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$

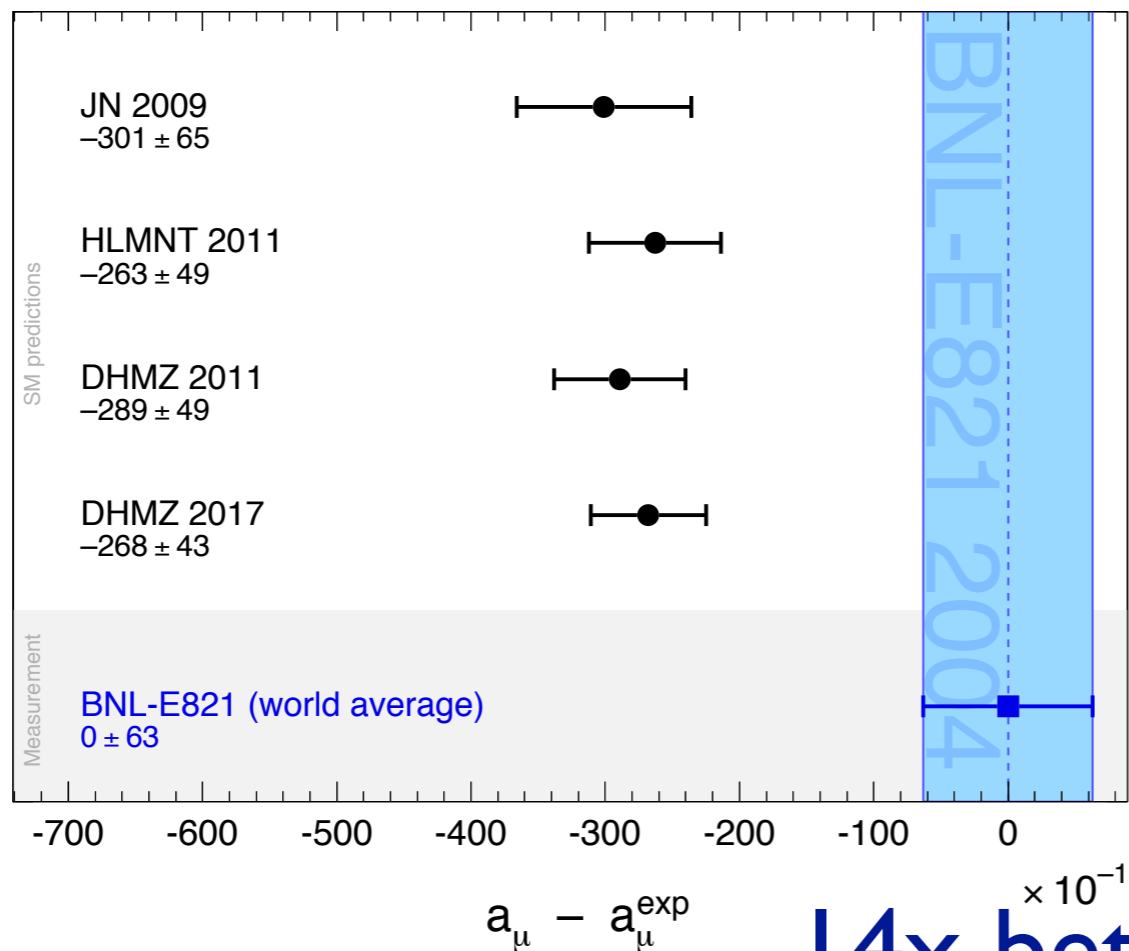
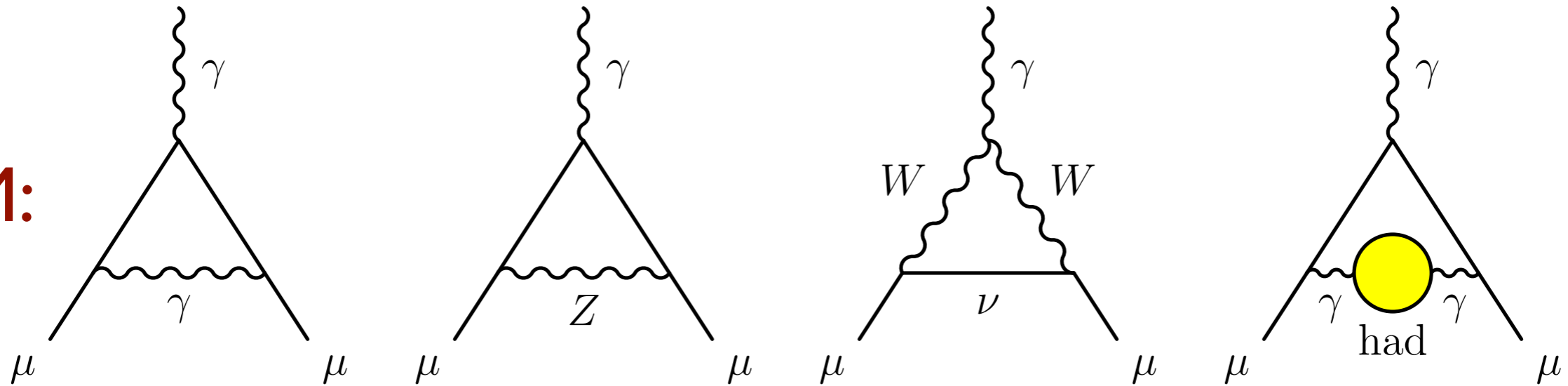
$$\mu_f = g_f \frac{e}{2m_f} \quad g_f = 2 + 2a_f$$

a_f is an anomalous magnetic moment

For an elementary fermion a_f and d_f can only be generated through loop corrections (N.B. $D > 4$)

The μ Magnetic Moment Anomaly

SM:



(Biggest Uncertainty)

$\Delta a_\mu \sim 3.5\sigma$
 “interesting but not conclusive”

4x better than in 1970's (CERN)

[Hoecker & Marciano, in RPP, PDG, 2018]

New $(g-2)_\mu$ Experiment at Fermilab



Aim:
4x better
than
BNL-E821
(2004) !

But there
is a $(g-2)_e$
anomaly
also...

Lepton Magnetic Moments & α

a_f in QED perturbation now known to $(\alpha/\pi)^5$!

[Aoyama, Hayakawa, Kinoshita, Nio, 2012; Aoyama, Kinoshita, Nio, 2018 & 2019]

SM: $a_f = a_f(\text{QED}) + a_f(\text{weak}) + a_f(\text{hadron})$

Very small

0.026 ppb 1.47 ppb [electron]

Using $a_e(\text{expt}) = 1\ 159\ 652\ 180.73\ (28) \times 10^{-12}$

[Hanneke, Fogwell, Gabrielse, 2008]

This, with a_e in the SM, yields

$\alpha^{-1}(a_e) = 137.035\ 999\ 1496\ (13)\ (14)\ (330)$

(Expt!)

New Paths to α

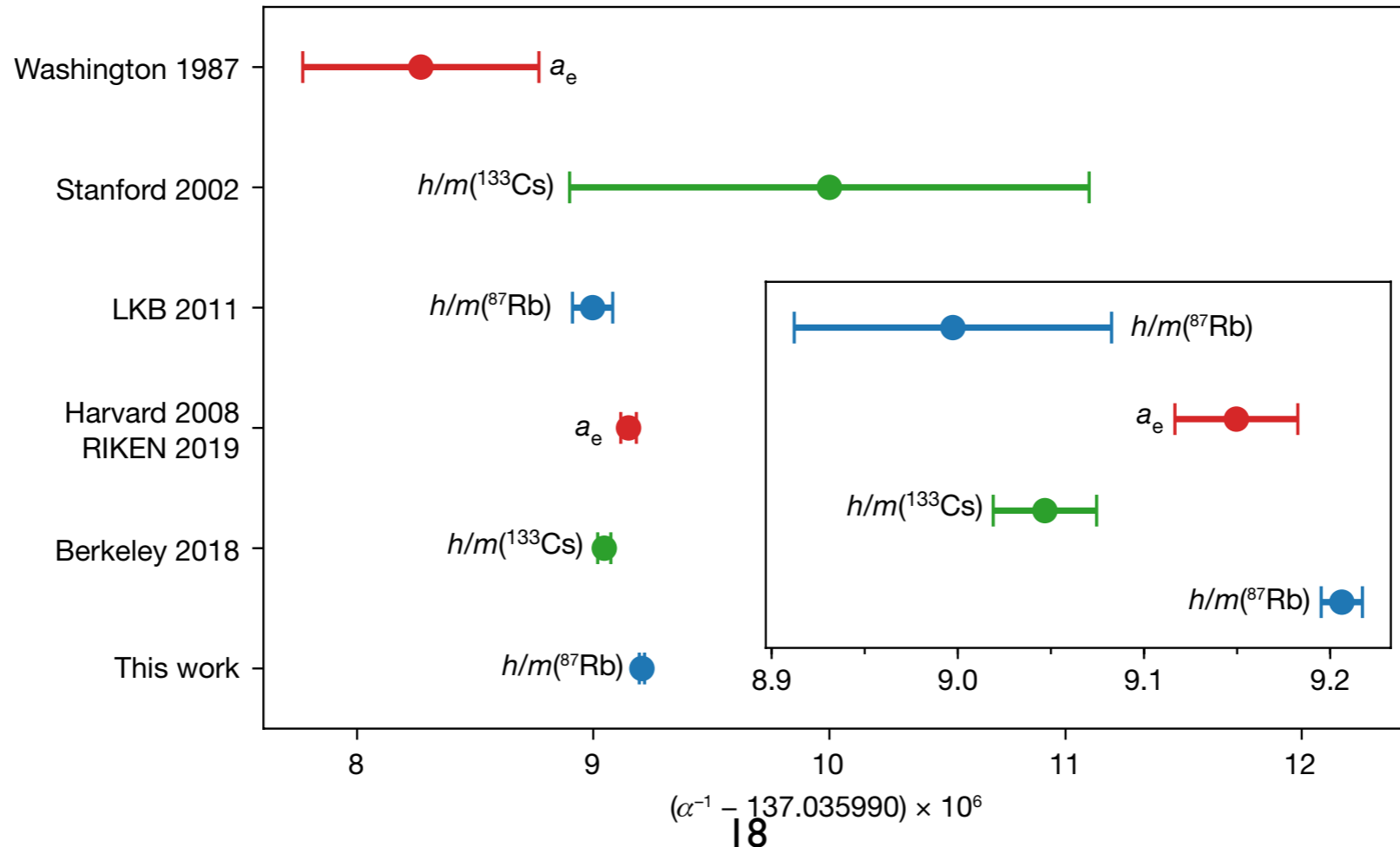
The measurement of $a_e \equiv (g-2)_e/2$ was once the only way to determine the fine-structure constant α precisely

[... Hanneke, Fogwell, Gabrielse, 2008]

Now with h/M_X (for $X=\text{Rb}$ or Cs) from **atom interferometry**

we have another precise way of determine α

[Bouchendira et al., 2011 [Rb]; Parker et al., 2018 [Cs]; Morel et al., 2020 [Rb]]



a_μ and a_e Probe Physics Beyond the SM

[Aoyama, Kinoshita, Nio, 2019]

$$a_e^{\text{EXP}} - a_e^{\text{SM}} [\text{Rb, 2011}] = (-131 \pm 77) \times 10^{-14}$$

$$a_e^{\text{EXP}} - a_e^{\text{SM}} [\text{Rb, 2020}] = (+48 \pm 30) \times 10^{-14}$$

$\sim 1.6 \sigma$

$$a_e^{\text{EXP}} - a_e^{\text{SM}} [\text{Cs, 2018}] = (-88 \pm 36) \times 10^{-14}$$

$\sim 2.4 \sigma$

$$a_\mu^{\text{EXP}} - a_\mu^{\text{SM}} = (2.74 \pm 0.73) \times 10^{-9} \quad (!)$$

$\sim 3.7 \sigma$

Both the relative sign and size are important.

A viable new-physics solution cannot distinguish μ and e only by their mass! (Δa_e [Cs] is 10x too big!)

a_μ & a_e Signal Lepton Flavor Universality (LFU) Violation

“LFU” means that μ and e differ only in their mass

$$(\delta a_f)_{\text{new}} \sim m_f^2 / M_{\text{new}}^2$$

Note $m_\mu^2/m_e^2 \sim 4.2 \times 10^4$

Thus Δa_e [Cs,Rb] implies a Δa_μ that is too large
w.r.t. BNL E821!

Perhaps LFU is violated

If so, this also suggests the appearance of
“light” new physics

Interpreting Δa_μ & Δa_e

Challenging to explain both at once

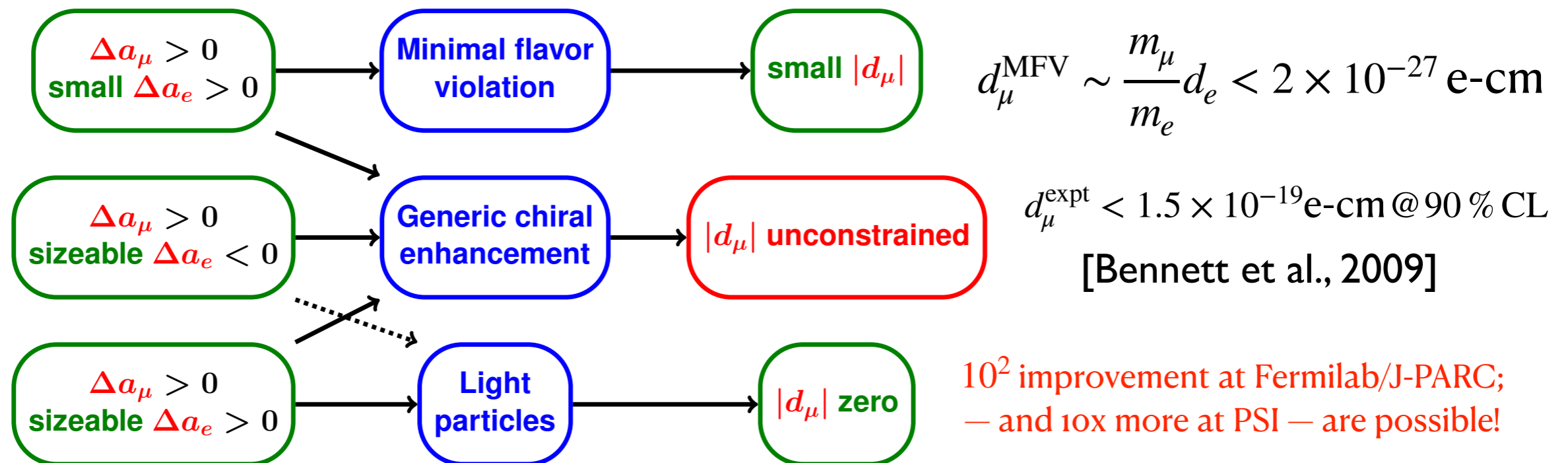
BSM solutions ($t < 2020$) treat μ and e differently

[Davoudiasl & Marciano, 2018] [Liu, Wagner, Wang, 2018] [Crivellin and Hoferichter, 2018]
 [Hiller et al., 2019] [Fayet, 2007; Kahn et al., 2017] [SG & Yan, 2020]

Enter EFT treatment; severe limit

$\text{Br}(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13}$ @ 90 % CL [MEG: Baldini et al., 2016]

decouples e and μ sectors, so d_μ need not be set by d_e !



EDMs & Sensitivity to New Physics

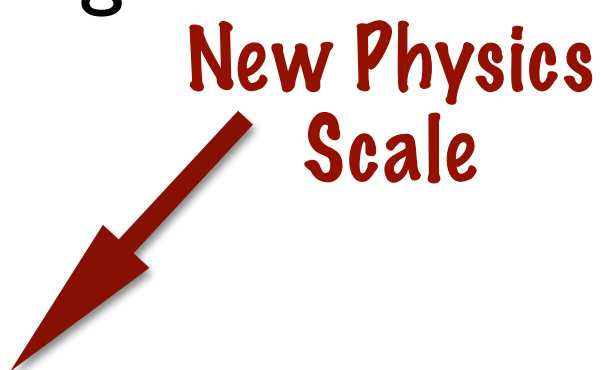
The electric and (anomalous) magnetic moments change chirality

$$\bar{\psi}\sigma^{\mu\nu}\psi = (\bar{\psi}_L\sigma^{\mu\nu}\psi_R + \bar{\psi}_R\sigma^{\mu\nu}\psi_L)$$

$$\bar{\psi}\sigma^{\mu\nu}\gamma_5\psi = (\bar{\psi}_L\sigma^{\mu\nu}\gamma_5\psi_R + \bar{\psi}_R\sigma^{\mu\nu}\gamma_5\psi_L)$$

By dimensional analysis we infer the scaling

$$d_f \sim e \frac{\alpha}{4\pi} \frac{m_f}{\Lambda^2} \sin \phi_{\text{CP}}$$

$$d_{d \text{ quark}} \sim 10^{-3} e \frac{m_d(\text{MeV})}{\Lambda(\text{TeV})^2} \sim 10^{-25} \frac{1}{\Lambda(\text{TeV})^2} e \text{ -- cm}$$


New Physics
Scale

Neutron: $d_n < 1.8 \times 10^{-26}$ e-cm [90 % C.L.] [Abel et al., 2020]

EDM experiments have (at least) TeV scale sensitivity

Applied electric fields can be enormously enhanced
in atoms and molecules: world's best EDM limit ^{199}Hg

[Graner et al., 2016]

EDMs in the SM

The contribution from the CKM matrix first appears in **three-loop order!**

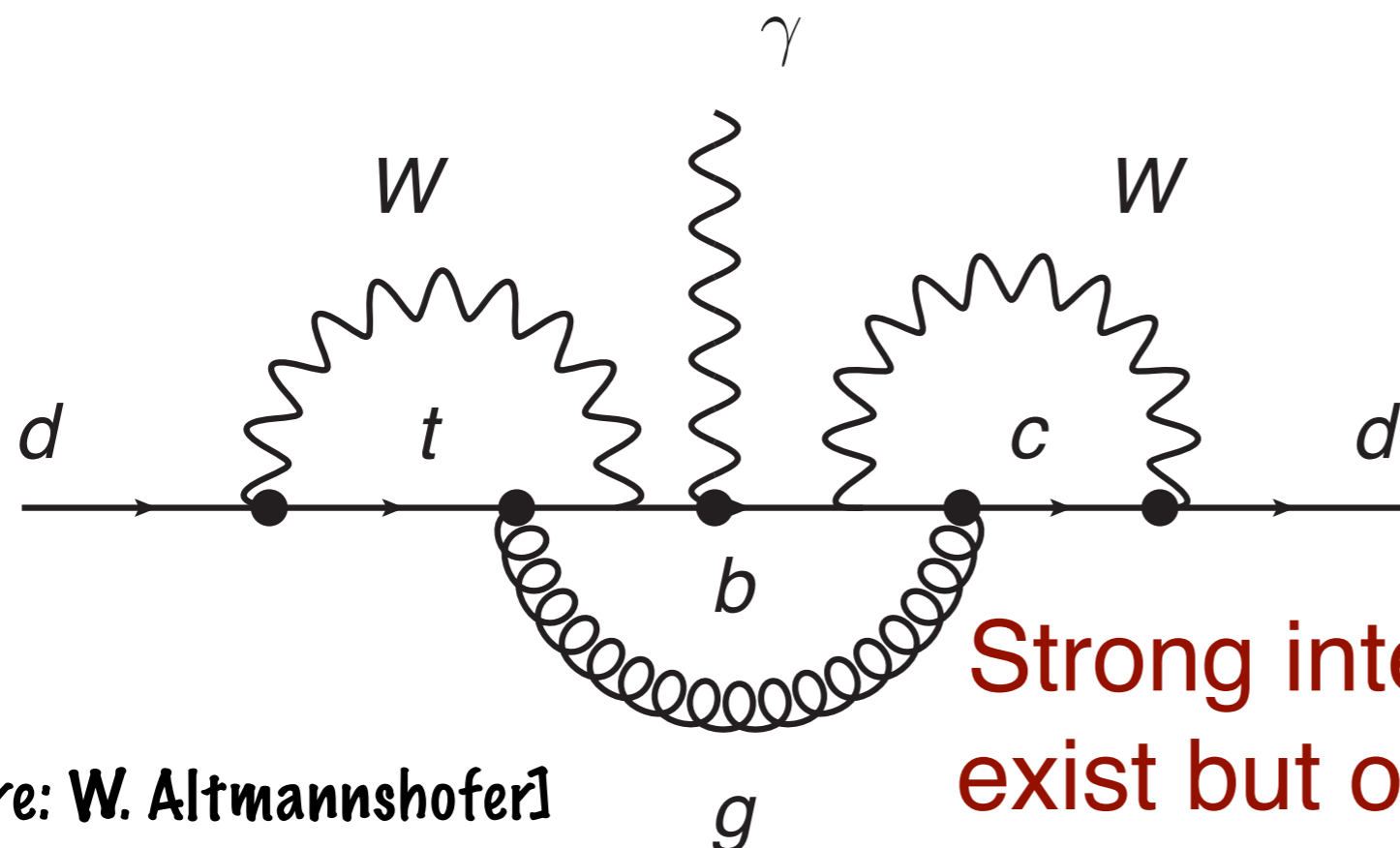
The EDM is flavor diagonal, so that...

at one-loop order no “Im V...” piece survives

at two-loop order the “Im V...” piece vanishes [Shabalin, 1978]

at three-loop order the gluon-mediated terms dominate

[Khriplovich, 1986]



$$|d_d| \sim 10^{-34} \text{ e-cm}$$

[Czarnecki & Krause, 1997]

Inaccessibly small!

Strong interaction enhancements exist but only by 10^2 or 3 in neutron

[figure: W. Altmannshofer]

[Gavela et al., 1982; Khriplovich & Zhitnitsky, 1982; Mannel & Uraltsev, 2012;... Seng, 2015]

Lepton EDMs in the SM

The contribution from the CKM matrix first appears in

cf. d_e^{eff} from CPV e - N four-loop order!

[Pospelov & Ritz, 2013]

$$d_e \sim 10^{-44} \text{ e-cm} \quad [\text{Khriplovich \& Pospelov, 1991}]$$

Majorana neutrinos can enhance a lepton EDM

[Ng & Ng, 1996]

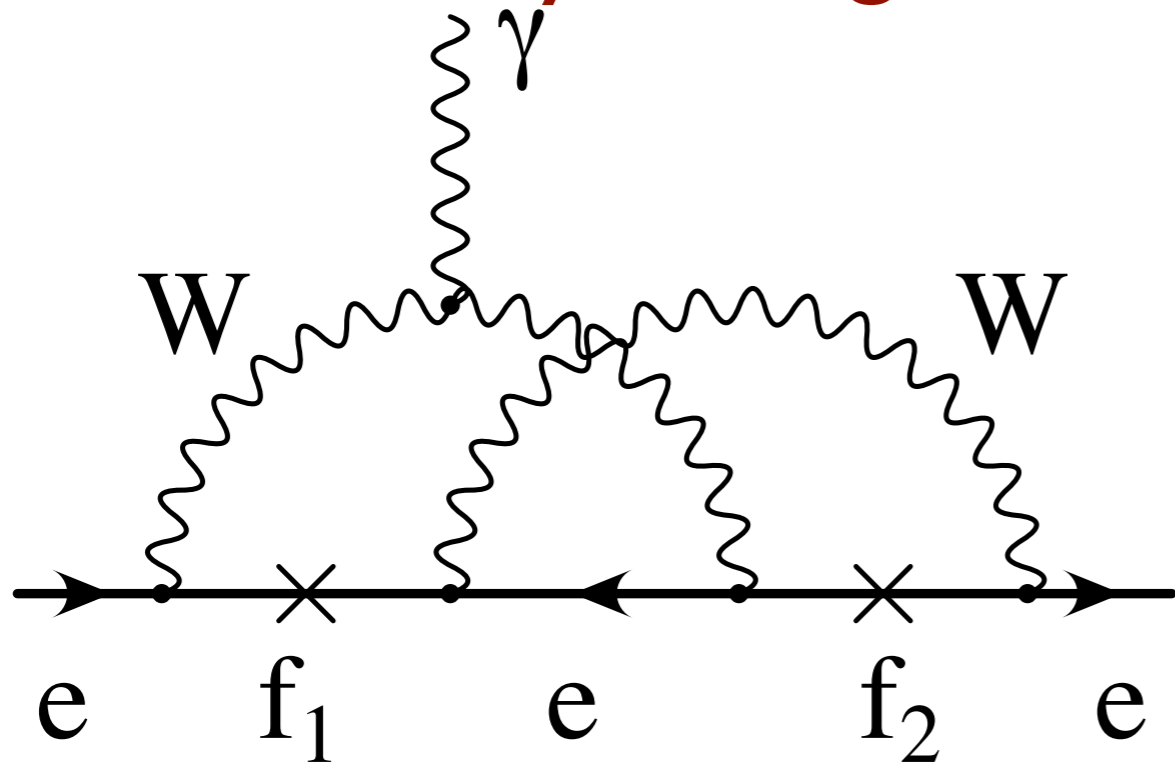
but **not nearly enough** to make it “visible”

For “fine tuned” parameters

$$d_e \lesssim 10^{-33} \text{ e-cm}$$

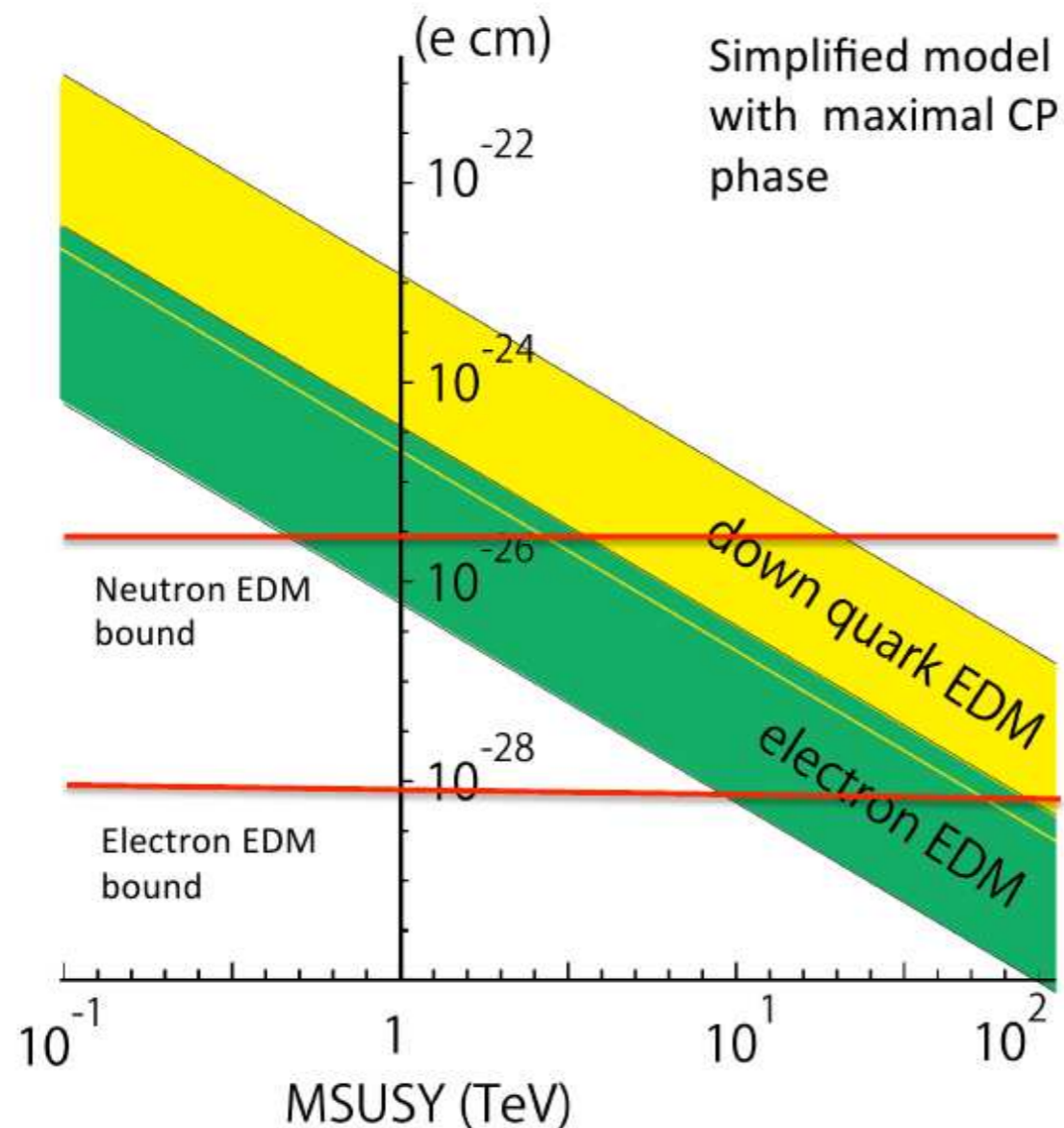
[Archambault, Czarnecki, & Pospelov, 2004]

Look to CPV in ν oscillations to probe leptogenesis!



EDMs & the SUSY CP Problem

Models with $O(1)$ CP phases & weak scale supersymmetry



(Hisano @ Moriond EW 2014)

[Figure: W. Altmannshofer]

An EDM can now appear at one loop!

EDM bounds push super partner masses far above the TeV scale!
Different models can make the pertinent CP phases effectively small...

LHC results now suggest “decoupling” is a partial answer

Model Independent Analysis Framework

Suppose new physics enters at an energy scale

$$E > \Lambda$$

Then for $E < \Lambda$ we can extend the SM as per

$$\mathcal{L}_{\text{SM}} \implies \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i}{\Lambda^{D-4}} \mathcal{O}_i^D,$$

where the new operators have mass dimension $D > 4$
and we impose $SU(2)_L \times U(1)$ gauge invariance

on the operator basis [Buchmuller & Wyler, 1986;
Grzadkowski et al., 2010]

**We can consider all the CP-violating terms that appear
at a fixed D**

Operator Analysis of EDMs

The flavor-diagonal effective Lagrangian at ~ 1 GeV

$$\mathcal{L}_{\text{dim } 4} \supset \bar{\theta} \alpha_s G \tilde{G} \quad \leftarrow \text{can appear in the IR even if an axion acts [Chien et al., arXiv:1510.00725, JHEP 2016]}$$

$$\mathcal{L}_{\text{“dim 6”}} \supset \sum_{q=u,d,s} \left(d_q \bar{q} F \sigma \gamma_5 q + \tilde{d}_q \bar{q} G \sigma \gamma_5 q \right) + \sum_{l=e,\mu} d_l \bar{l} F \sigma \gamma_5 l$$

$$\mathcal{L}_{\text{dim 6}} \supset w g_s^3 G G \tilde{G} + \sum_{f,f',\Gamma} C'_{ff'} (\bar{f} \Gamma f')_{LL} (\bar{f} \Gamma f')_{RR}$$

$$\mathcal{L}_{\text{“dim 8”}} \supset \sum_{q,\Gamma} C_{qq} \bar{q} \Gamma q \bar{q} \Gamma i \gamma_5 q + C_{qe} \bar{q} \Gamma q \bar{e} \Gamma i \gamma_5 e + \dots$$

[Ritz, CIPANP, 2015]

Many sources: note effective hierarchy imposed by $SU(2) \times U(1)$ gauge invariance (chirality change!)

Limits on new CPV sources often taken “one at a time”

Operator Analysis of EDMs

Connecting from high to low scales

A single TeV scale CPV source may give rise to multiple GeV scale sources

Explicit studies of operator mixing & running effects are now available

[Chien et al., arXiv:1510.00725, JHEP 2016; Cirigliano, Dekens, de Vries, Merenghetti, 2016 & 2016]

Lattice QCD studies of apropos single-nucleon matrix elements

Enter isoscalar & isovector tensor charges... & more!

[Bhattacharya et al., 2015 & 2016; Gupta et al., arXiv:1801.03130...]

Determining the parameters of the low energy effective

Lagrangian experimentally is a distinct problem

Can all the low-energy CPV sources be determined?

★ Need to interpret EDM limits in complex systems: atoms, molecules, and nuclei — or not?! (p, d)

Note talks today by Rob Timmermans and Rajan Gupta!

A Vast Range of Dark Matter Candidates

Particle Masses

Fits in Galaxy

Elementary Part.

10^{-22} eV 1 eV 1 keV 1 GeV 100 TeV 10^{19} GeV



“Fuzzy DM”

“WIMPs”

Exotics

“Black Holes”

$$n_{\text{DM}} \lambda_{\text{dB}}^3 \gg 1$$

$$n_{\text{DM}} \lambda_{\text{dB}}^3 \ll 1$$

Behaves like
a classical field

Rare collisions

Study in underground expts!

Cosmology!

Uncertainty Principle

washes out cosmic short-scale structure

New probes!! [GPS networks, atomic clocks...]

[A. Derevianko,...]

Ultralight Dark Matter

Cosmic history constraints

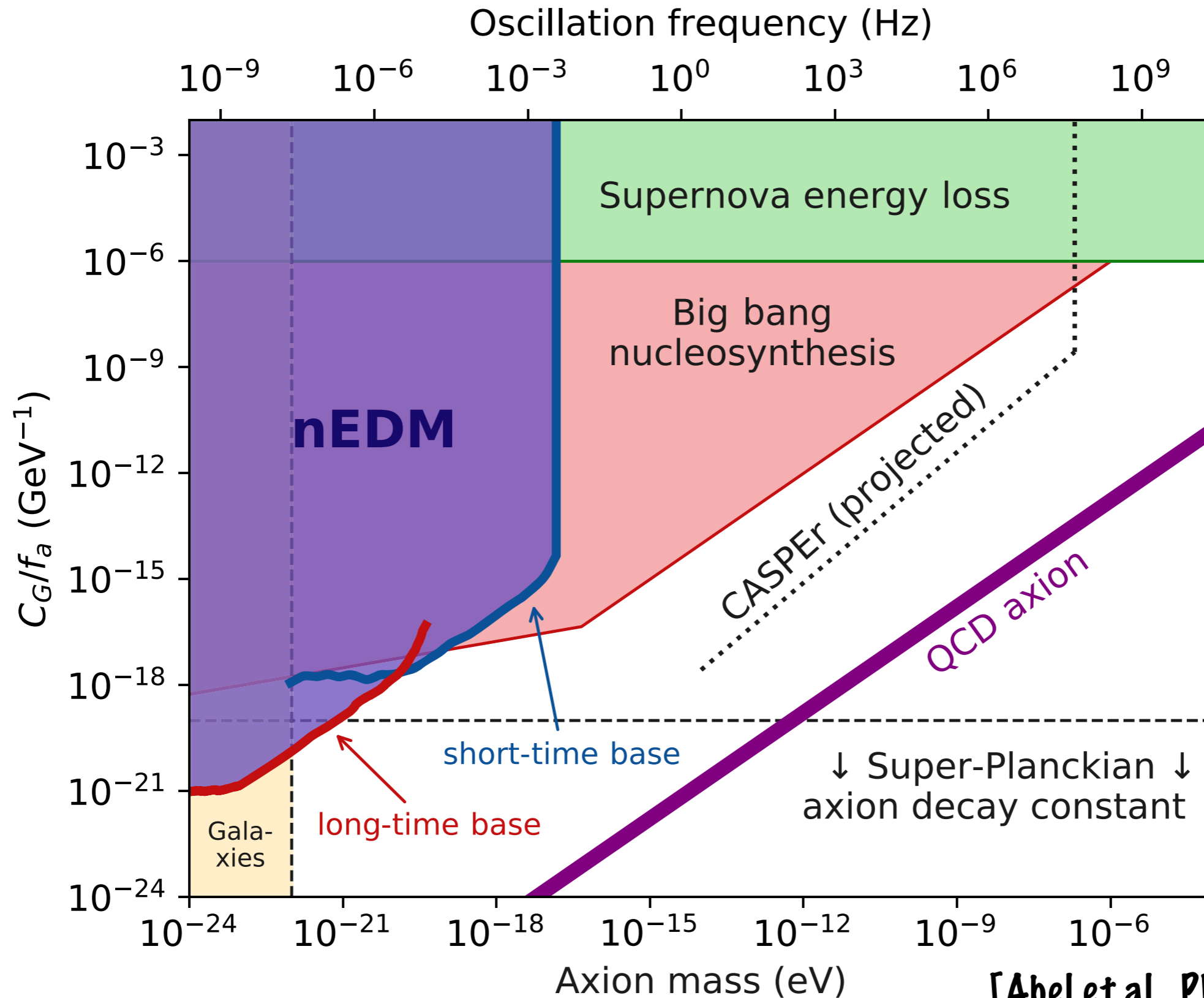
Observations of the CMB power spectrum constrain the ratio of tensor (gravitational wave) to scalar (density fluctuations) power r

$$r < 0.07 \text{ at } 95\% \text{ C.L.} \quad [\text{Ade et al., PRL } 116 \text{ (2016) } 0313021 \text{ (BICEP2 + Keck + Planck)}]$$

This quantity has not been detected making ultralight (axion-like) dark matter ($m_a \sim 10^{-22}$ eV) “fuzzy (quantum wave) dark matter” possible....

[Hu, Barkana, Gruzinov, PRL 85 (2000) 1158;
Schive, Chiueh, Broadhurst, Nat. Phys. 10 (2014) 496...;
Graham & Rajendran, PRD 84 (2011) 055013,... for direct detection prospects 1

Direct Detection: Ultralight Dark Matter



[Abel et al., PRX, 2017]

Note talk today by Peter Graham!

Summary

Through new and continuing efforts in the study of CP violation worldwide (with focus on relationships!) cracks in the SM are beginning to show!

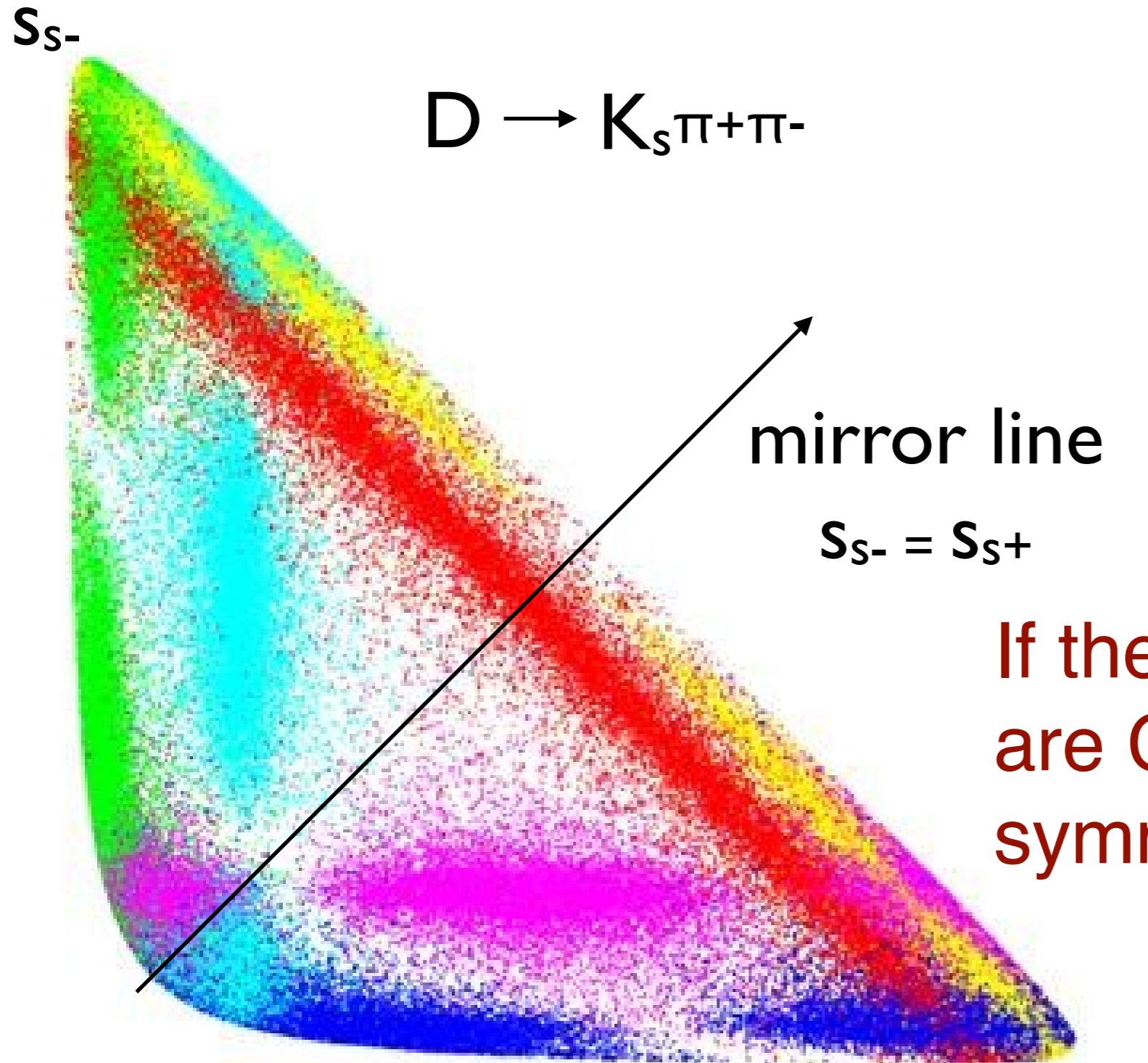
EDM experiments continue to be uniquely sensitive to new sources of CP violation; direct study of d_n vs. d_p (and d_d) yields relationships between new CPV sources....

The possibility of significant improvements in d_μ may shed light on the Δa_e & Δa_μ puzzles

EDM experiments can also be used to limit the appearance of ultralight (axion-like) dark matter &....

Dalitz Studies of CP Violation

Apropos to both heavy and light flavor decays



Consider population asymmetry about the mirror line in neutral 0^- decay

If the initial and final states are C definite, then mirror symmetry is also a CP test

[SG & Tandean, 2004]

[Image Credit: Tom Latham [Tim Gershon]]

Dalitz Studies of CP Violation

For $|\Delta F|=1$ decays

- In untagged $B \rightarrow \pi^+ \pi^- \pi^0$ decay CPV appears in the SM
- All such dimension six operators can be rewritten as C definite combinations, the asymmetry is C and CP odd

To realize C violation in dimension six
 $|\Delta F|=1$ operators are necessary

[Jun Shi, Ph.D UK 2020; SG & Jun Shi, 2021, in preparation]

For $|\Delta F|=0$ decays [Enter η decays!]

N.B. mirror symmetry breaking in the $\eta \rightarrow \pi^+ \pi^- \pi^0$ Dalitz plot is a C odd and CP odd observable (by CPT this is a T odd, P even test)!

[SG & Jun Shi, PRD 2020]

C violation first appears in dimension eight (in SM EFT),
in distinction to the dimension six operators for EDMs

Note old “C odd” papers [TD Lee & L Wolfenstein, 1965; Lee, 1965; Nauenberg, 1965]

[Bernstein, Feinberg, & Lee, 1965; Barshay, 1965]

Backup Slides

A Cosmic Baryon Asymmetry (BAU)

Assessments in two different epochs agree!



[George Gamow, AIP]

Big-Bang Nucleosynthesis (BBN)

“ α , β , γ ”

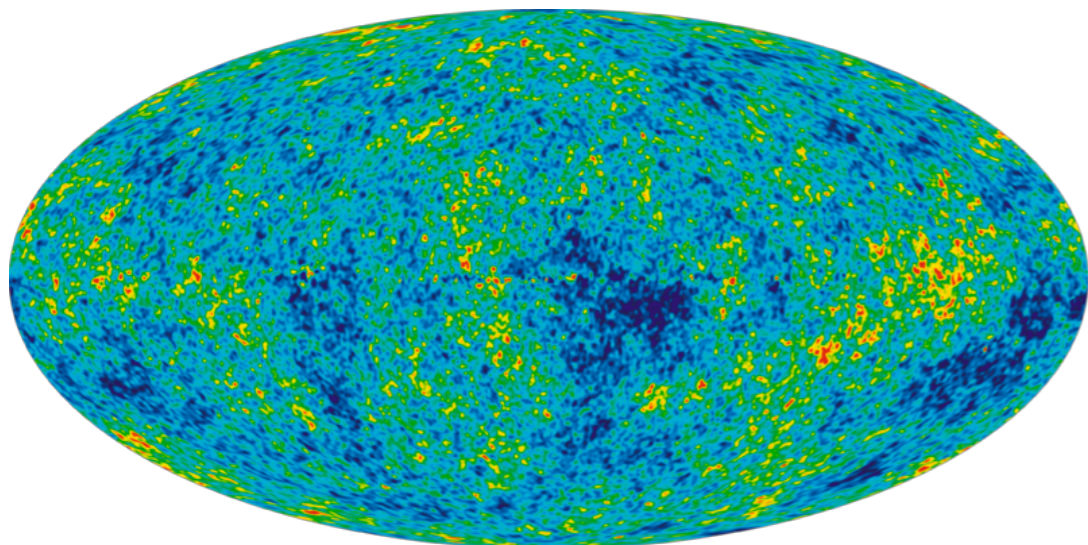
Alpher, Bethe, Gamow, “The Origin of the Chemical Elements,” 1948

Lightest Elements are made in the Big-Bang,
but prediction depends on the BAU

Cosmic Microwave Background (CMB)

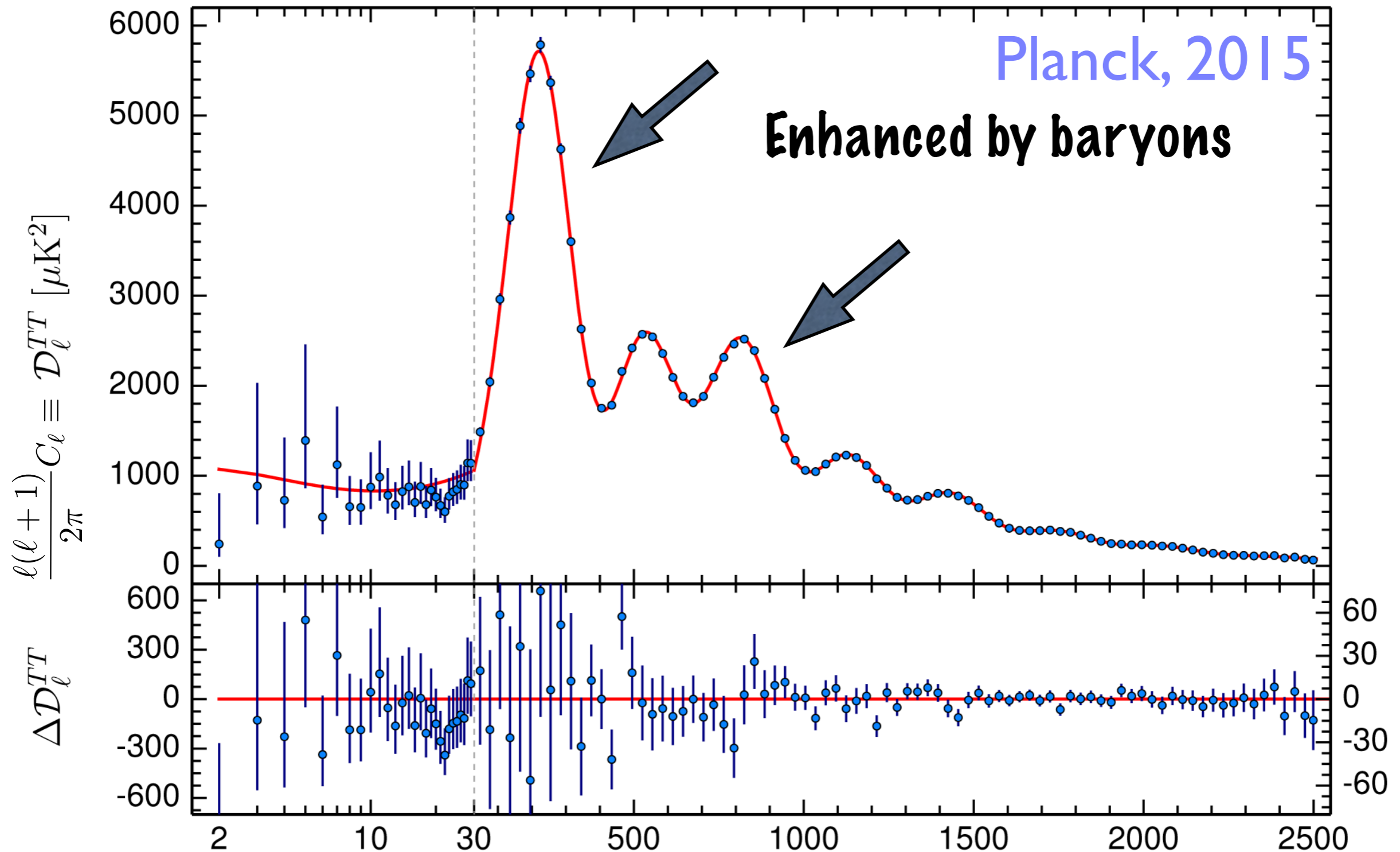
Dicke, Peebles, Roll, & Wilkinson, 1965;
Penzias & Wilson, 1965

Pattern of Acoustic Peaks
reveals baryonic matter

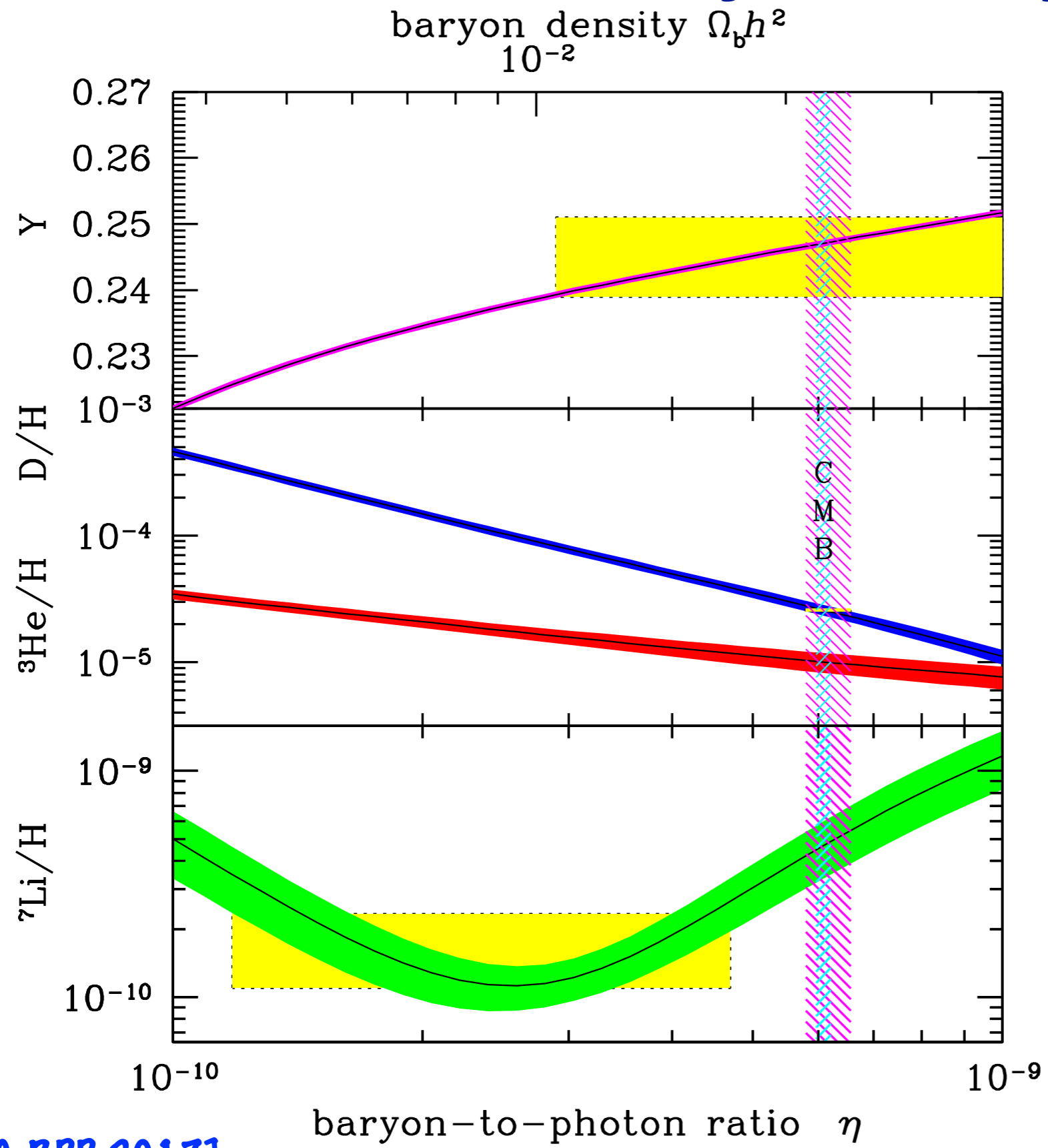


A Cosmic Baryon Asymmetry

Patterns of acoustic waves reveal net baryon number!



A Cosmic Baryon Asymmetry



BAU from BBN & observed D/H & $^4\text{He}/\text{H}$ concordance

BAU from CMB is more precise

[Both @ 95% CL]