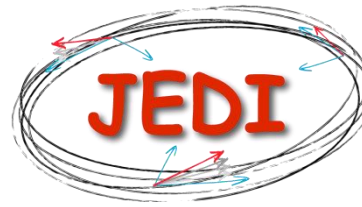




RWTHAACHEN
UNIVERSITY



Spin Tracking with COSY INFINITY and its Benchmarking

2015-05-05 | Marcel Rosenthal for the JEDI collaboration

➤ **Methods**

- Simulation toolbox
- New extension: Transfer maps for time-varying fields

➤ **Application I : RF-B Solenoid Driven Oscillations**

- Induced RF field spin resonance
- Benchmarking of measurement, analytical estimation and tracking

➤ **Application II: RF- $E \times B$ Wien filter Driven Oscillations**

- EDM method based on RF fields
- Benchmarking of tracking and analytical estimation
- Systematic limitations

➤ **Conclusion**

- Equation of spin motion for relativistic particles in electromagnetic fields:

$$\frac{d\vec{S}}{dt} = \vec{S} \times \vec{\Omega}_{\text{MDM}} + \vec{S} \times \vec{\Omega}_{\text{EDM}}$$

$$\vec{\Omega}_{\text{MDM}} = \frac{e}{\gamma m} \left[(1 + G\gamma)\vec{B} + \left(G\gamma + \frac{\gamma}{1 + \gamma} \right) \frac{\vec{E} \times \vec{\beta}}{c} - \frac{G\gamma^2}{\gamma + 1} \vec{\beta}(\vec{\beta} \cdot \vec{B}) \right]$$

$$\vec{\Omega}_{\text{EDM}} = \frac{e \eta}{m 2} \left[\frac{\vec{E}}{c} + \vec{\beta} \times \vec{B} - \frac{\gamma}{\gamma + 1} \vec{\beta} \left(\vec{\beta} \cdot \frac{\vec{E}}{c} \right) \right]$$

$$\vec{\mu} = 2(G + 1) \cdot \frac{e}{2m} \vec{S}$$

	G
Proton	1.792847357
Deuteron	-0.142561769

$$\vec{d} = \eta \cdot \frac{e}{2mc} \vec{S}$$

d	η
10 ⁻²⁴ e cm	~10 ⁻⁹
10 ⁻²⁹ e cm	~10 ⁻¹⁴

COSY Toolbox

COSY INFINITY

M. Berz, K. Makino et al.

- Calculator:
 - Optical functions
 - Closed orbit
 - Spin tune
- Tracker:
 - Static maps
 - RF maps

COSY Lattice

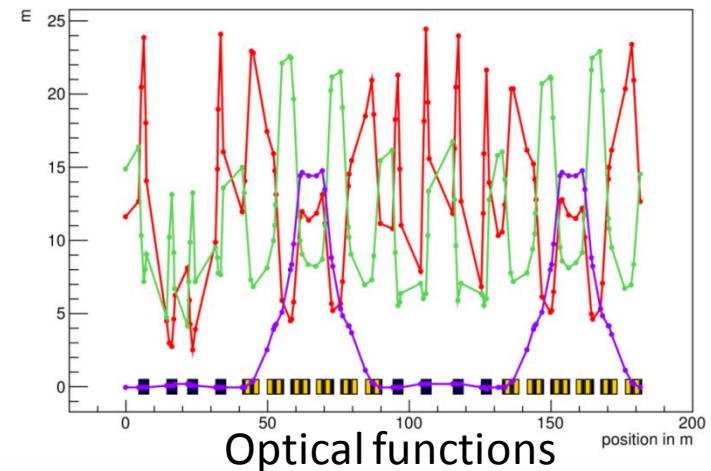
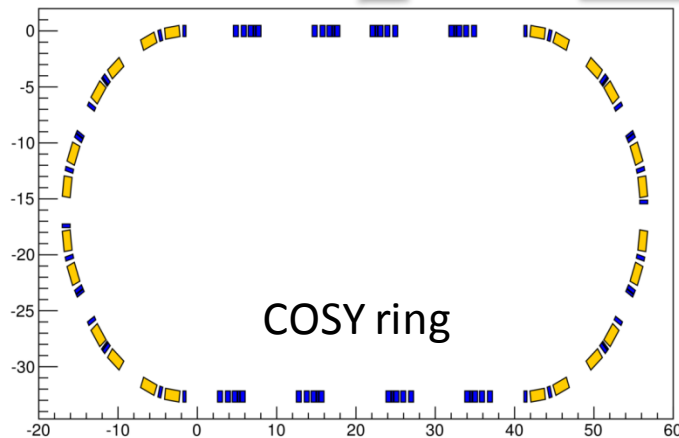
COSY Toolbox

Armadillo

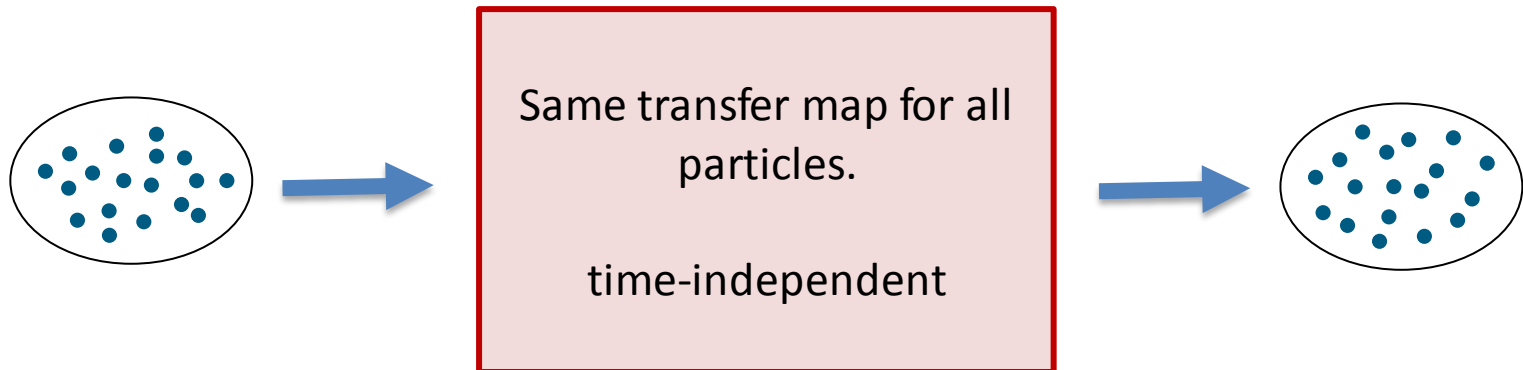
- linear algebra operations
- SVD, pseudo-inverse

ROOT

- plotting
- storage (ROOT files/trees)

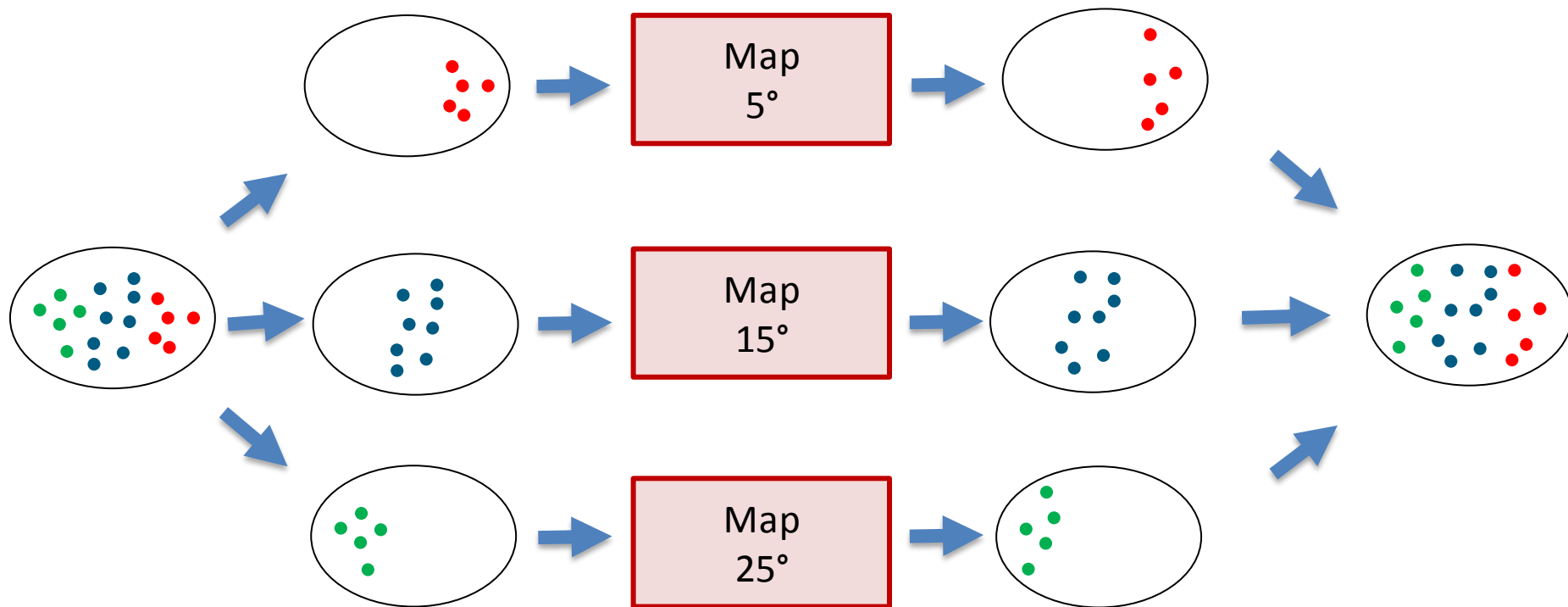


- Solutions for equations of motion to arbitrary order: $\mathcal{M}(\vec{z}_0)$, $\mathcal{A}(\vec{z}_0)$
- Relate phase space and spin coordinates before and after element
- Static fields:



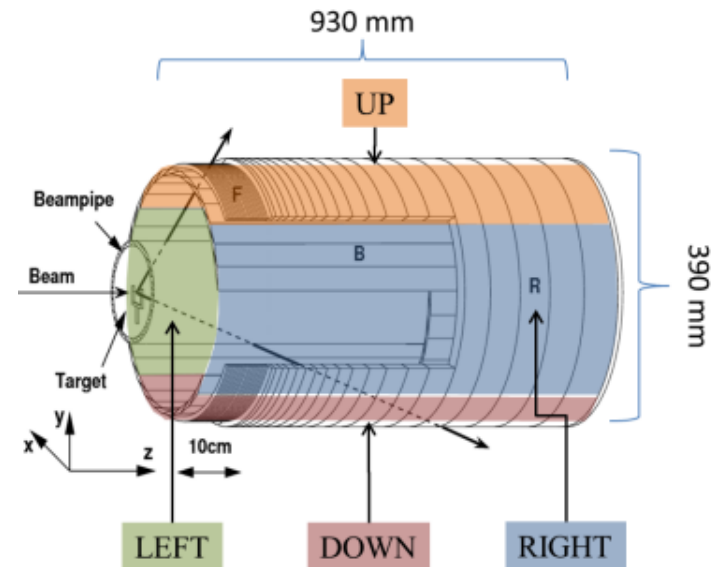
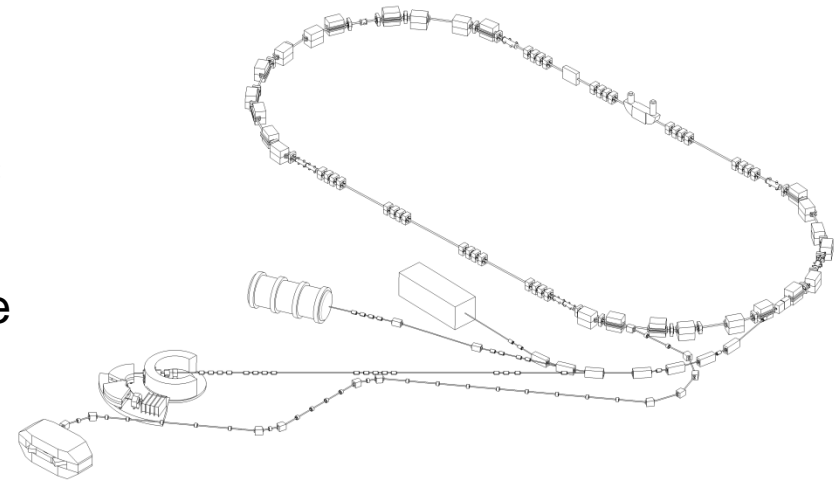
- What about time-varying fields?

- Radiofrequency fields:
 - Split element into N maps covering the 360° phase interval of the time-varying field (currently $N = 36$).



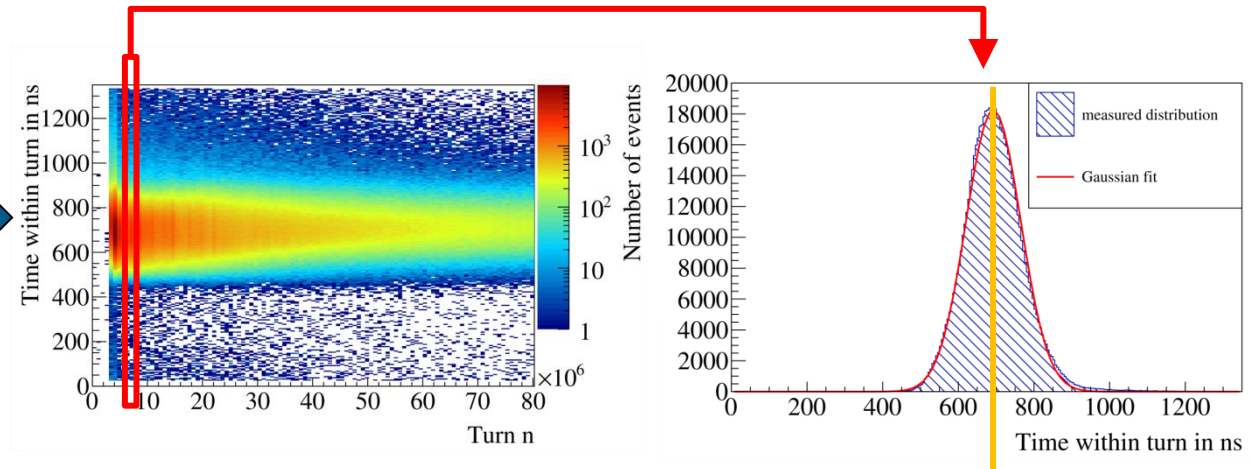
Experimental Setup for Studies

- Beam setup:
 - Polarized deuterons, 970 MeV/c
 - Electron cooled and bunched
 - Optimized Spin Coherence Time
- Idea:
 - Induce spin resonance by RF-B solenoid and measure characteristics of vertical polarization oscillations



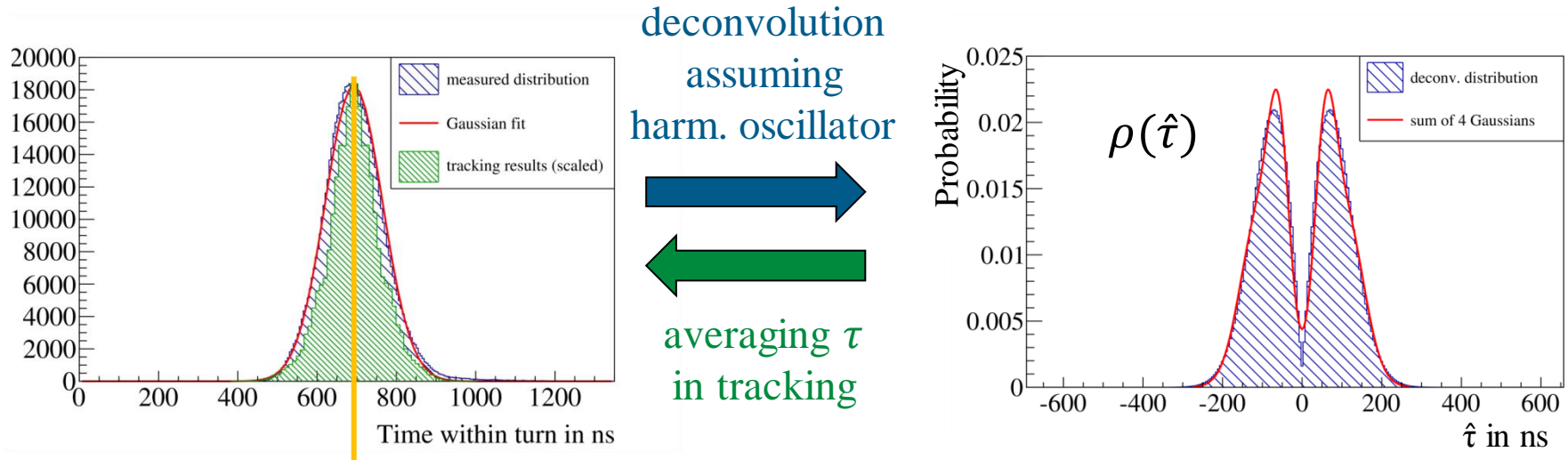
Time marking system allows for determination of event time with respect to RF cavity

Extraction of measured time distribution (τ -distribution) of particles in the bunch is possible.



Bunch center: $\tau = 0$

- Time marking system allows for determination of event time with respect to RF cavity
- Extraction of measured time distribution (τ -distribution) of particles in the bunch is possible.

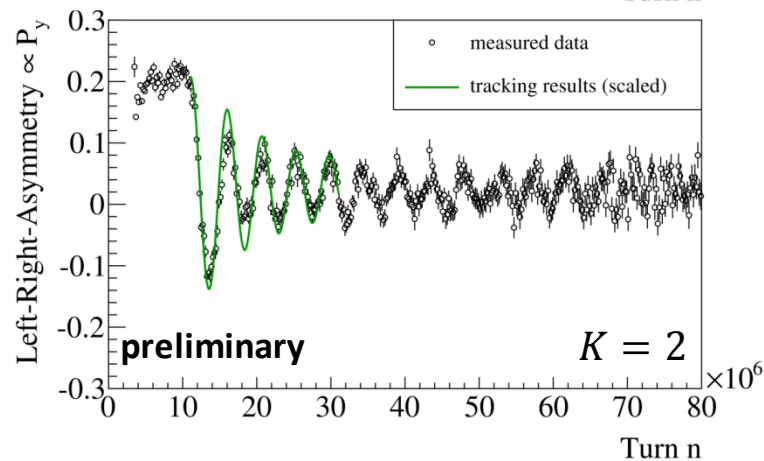
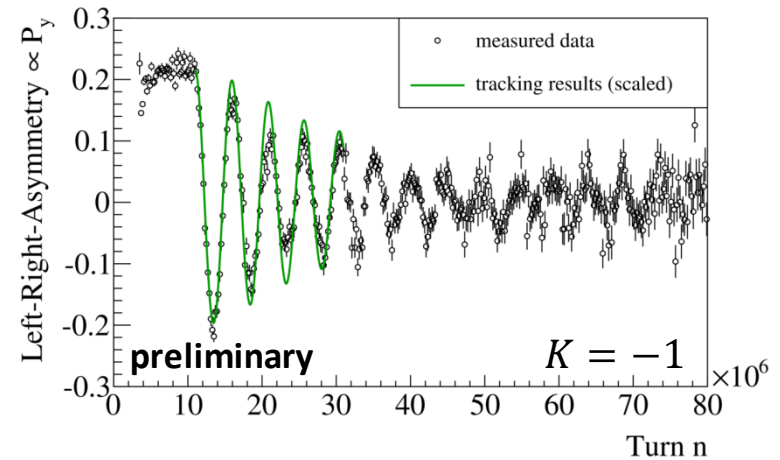
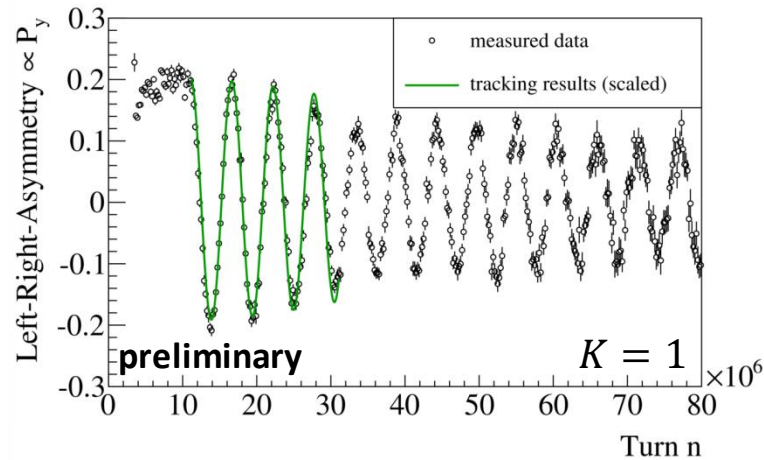


Bunch center: $\tau = 0$

- Initial longitudinal amplitude distribution required for analytical estimations and for tracking simulations.
- Assuming solution for an harmonic oscillator $\tau \approx \hat{\tau} \cdot \cos(2\pi\nu_{\text{sync}}n + \phi_{\text{sync}})$, the deconvolution results in the longitudinal synchrotron amplitude $\hat{\tau}$ -distribution.

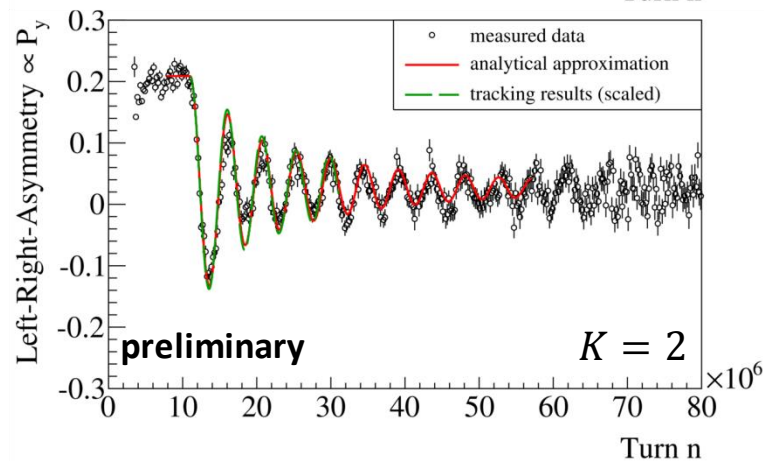
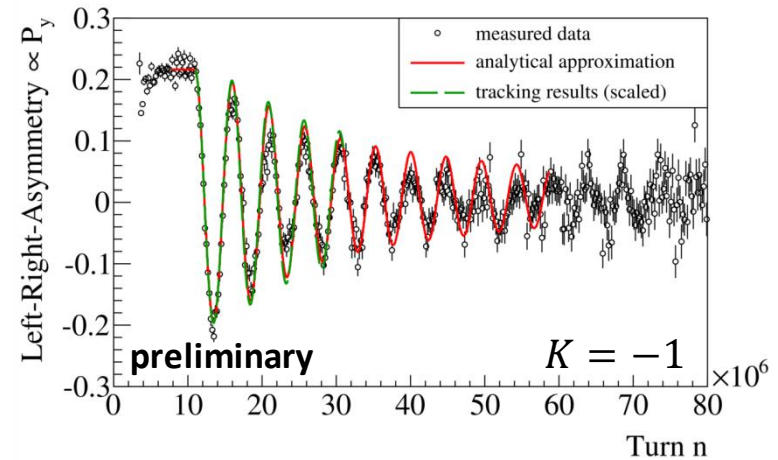
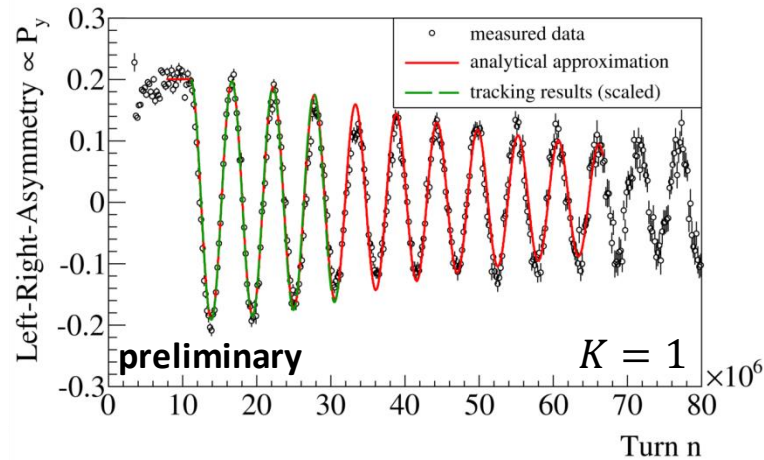
Benchmarking Results

- Radiofrequency field: $B_{\text{sol}} = \hat{B}_{\text{sol}} \cdot \cos(2\pi\nu_{\text{sol}} \cdot n + \phi_{\text{sol}})$ turned on at ~ 11 mio. turns.
- resonance condition: $\nu_{\text{sol}} = G\gamma + K, K \in \mathbb{Z}$



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Analytical estimation:

$$P_y(n) = \int_{-\infty}^{\infty} \rho(\hat{t}) S_y(n, \hat{t}) d\hat{t}$$

- Idea:
 - RF-E×B Wien filter with $\vec{B} \parallel \vec{e}_y$ on resonance induces buildup of vertical spin component for non-vanishing EDM.
 - Minimized impact on beam, but interaction on spin

- Analytical estimation for closed orbit and $S_z(0) = 1$:

$$\frac{dS_y}{dn} \approx -\frac{\alpha_0}{2} \left(n_y^2 \cdot n_z \cdot \sin(\phi_{WF}) + n_y \cdot n_x \cdot \cos(\phi_{WF}) \right) + \text{fast osc. terms}$$

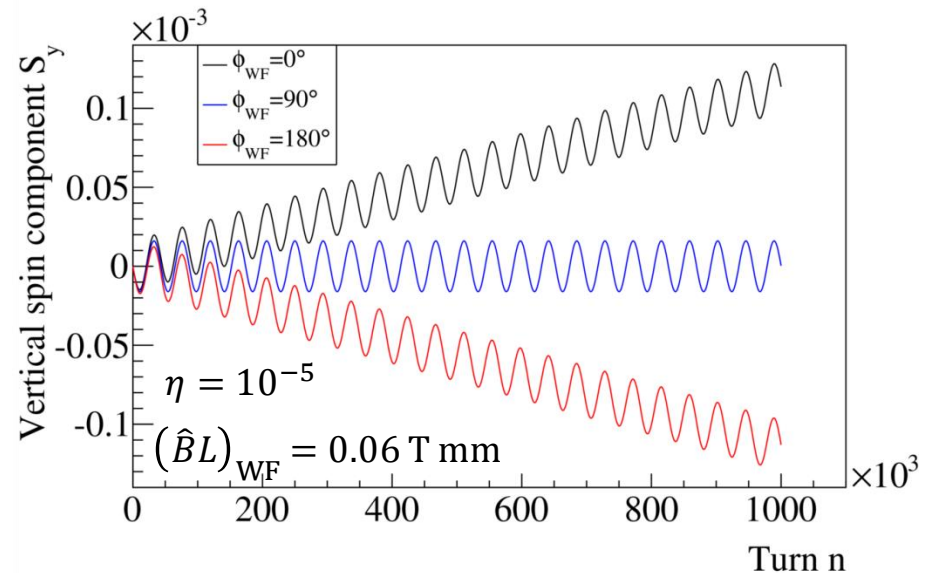
$$\alpha_0 = \frac{(1 + G)}{\gamma} \frac{q}{p} (\hat{B} \cdot L)_{WF}$$

$$B_{WF}(n) = \hat{B}_{WF} \cdot \cos(2\pi\nu_{WF} \cdot n + \phi_{WF})$$

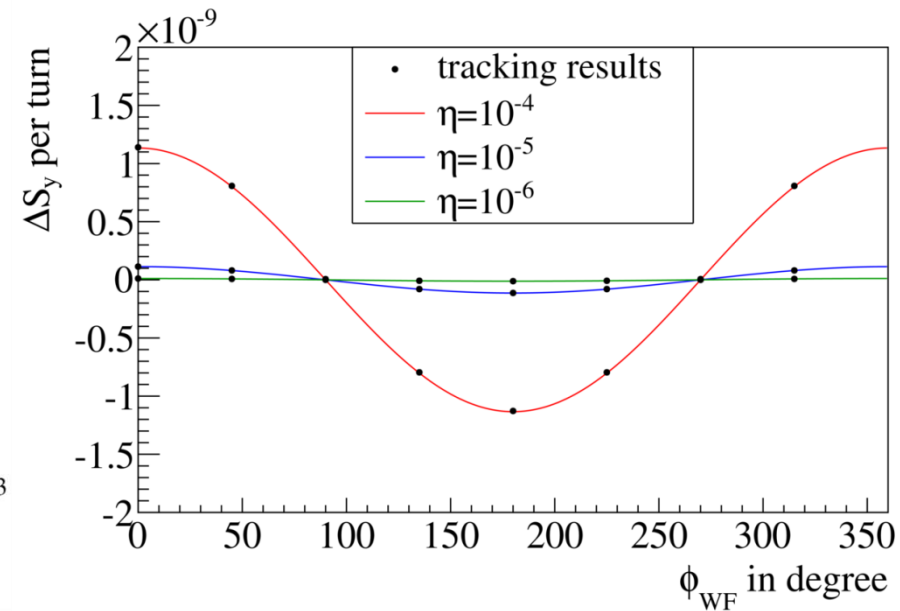
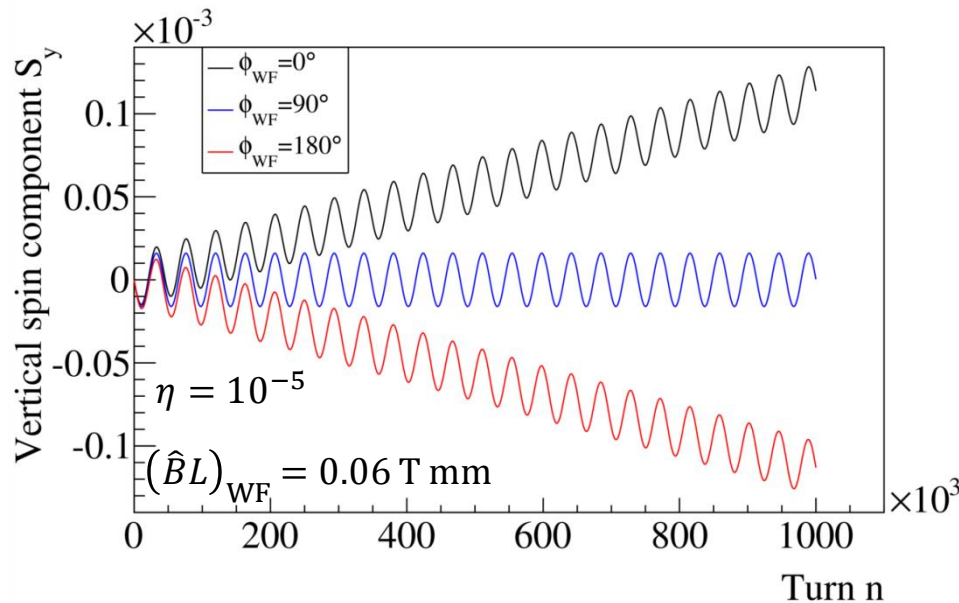
$$E_{WF}(n) = \beta c \cdot B_{WF}(n)$$

(n_x, n_y, n_z) :

spin closed orbit of static ring
@ RF Wien filter location

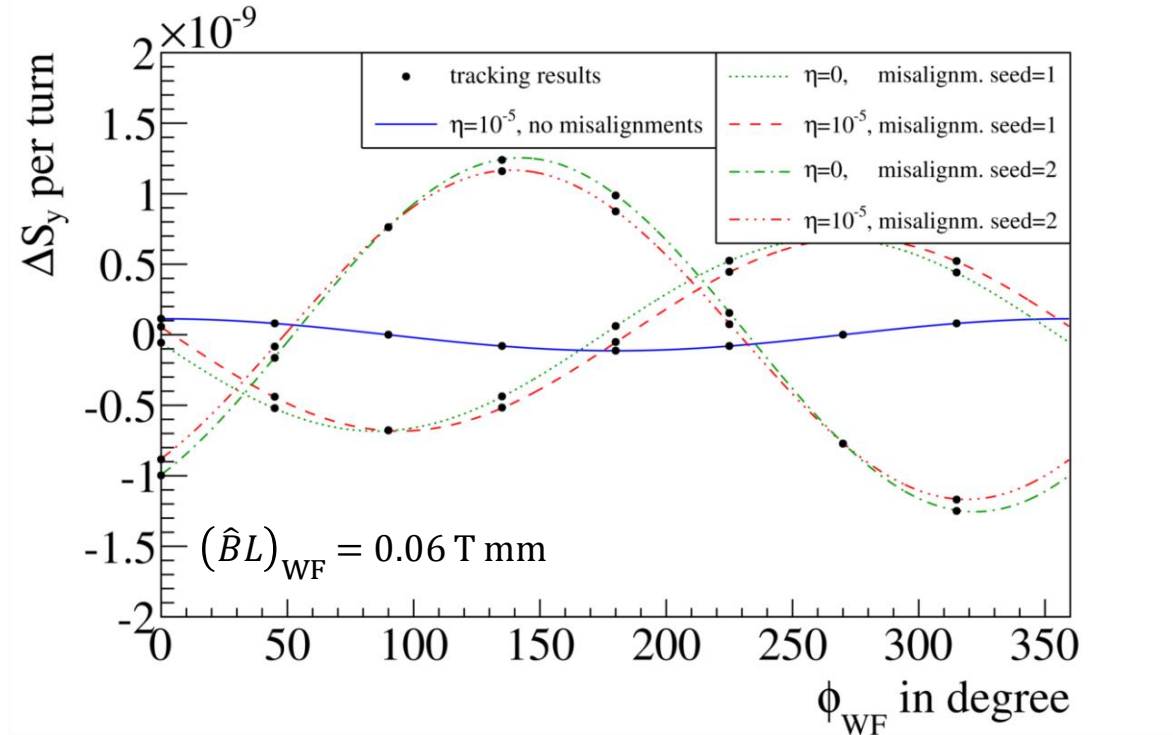


- Buildup scales linearly with EDM magnitude and depends on initial RF Wien filter phase



- Good agreement between analytical estimates and tracking results

- Introduce misalignments of the 56 lattice quadrupoles
- Gaussian distributed with $\sigma_{\text{mis}} = 0.1 \text{ mm}$

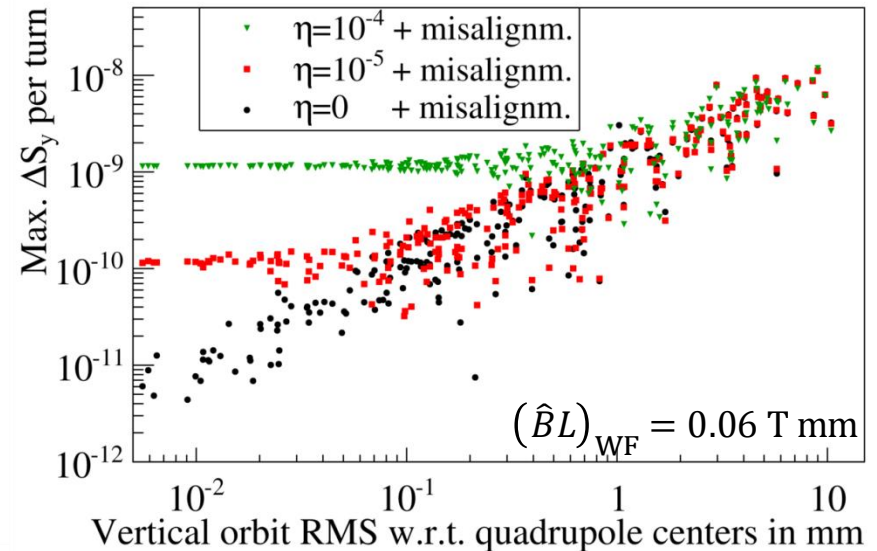
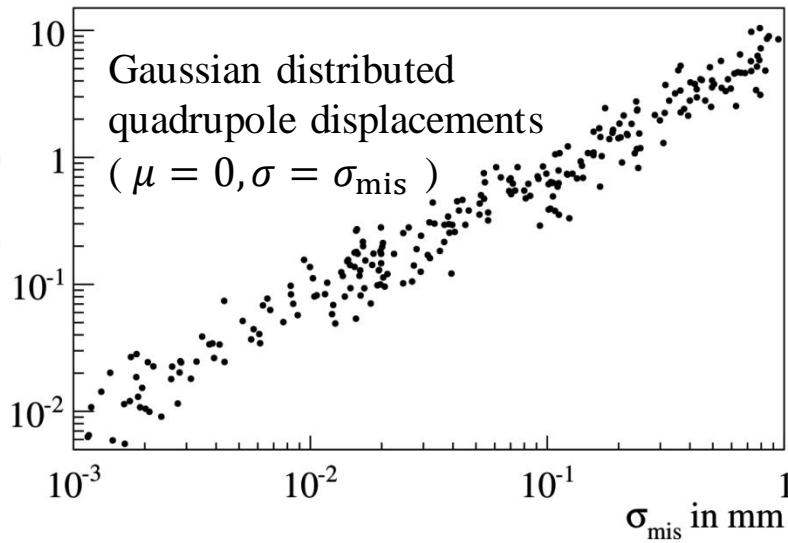


$$\frac{dS_y}{dn} \approx -\frac{\alpha_0}{2} \left(n_y^2 \cdot n_z \cdot \sin(\phi_{\text{WF}}) + n_y \cdot n_x \cdot \cos(\phi_{\text{WF}}) \right) + \text{fast osc. terms}$$

- Pure EDM: $n_x \neq 0$, misalignments: $n_x \neq 0$ and $n_z \neq 0$

- Main contribution from additional radial magnetic fields
- Besides spin motion, also beam motion is affected

Vertical orbit RMS w.r.t. quadrupole centers in mm



- Vertical buildup ΔS_y per turn for RMS of 1 mm similar to $\eta = 10^{-4}$
 $(d = 5 \cdot 10^{-19} \text{ e cm})$

➤ **Method:**

- Calculation of maps for time-varying elements implemented into COSY INFINITY extension

➤ **Application I: RF-B Solenoid**

- Successfully benchmarked with analytical estimates and measured data for RF-B solenoid induced resonance
- Dependence of oscillation damping on solenoid frequency has been reproduced

➤ **Application II: RF- $E \times B$ Wien filter**

- Tracking results for EDM related buildup match with analytical calculations.
- Gaussian distributed quadrupole displacements which introduce an vertical orbit RMS of 1 mm lead to a buildup similar to an EDM of $d \approx 5 \cdot 10^{-19}$ e cm

Questions? THPF031 (m.rosenthal@fz-juelich.de)