



Studies of systematic limitations in the EDM searches at COSY

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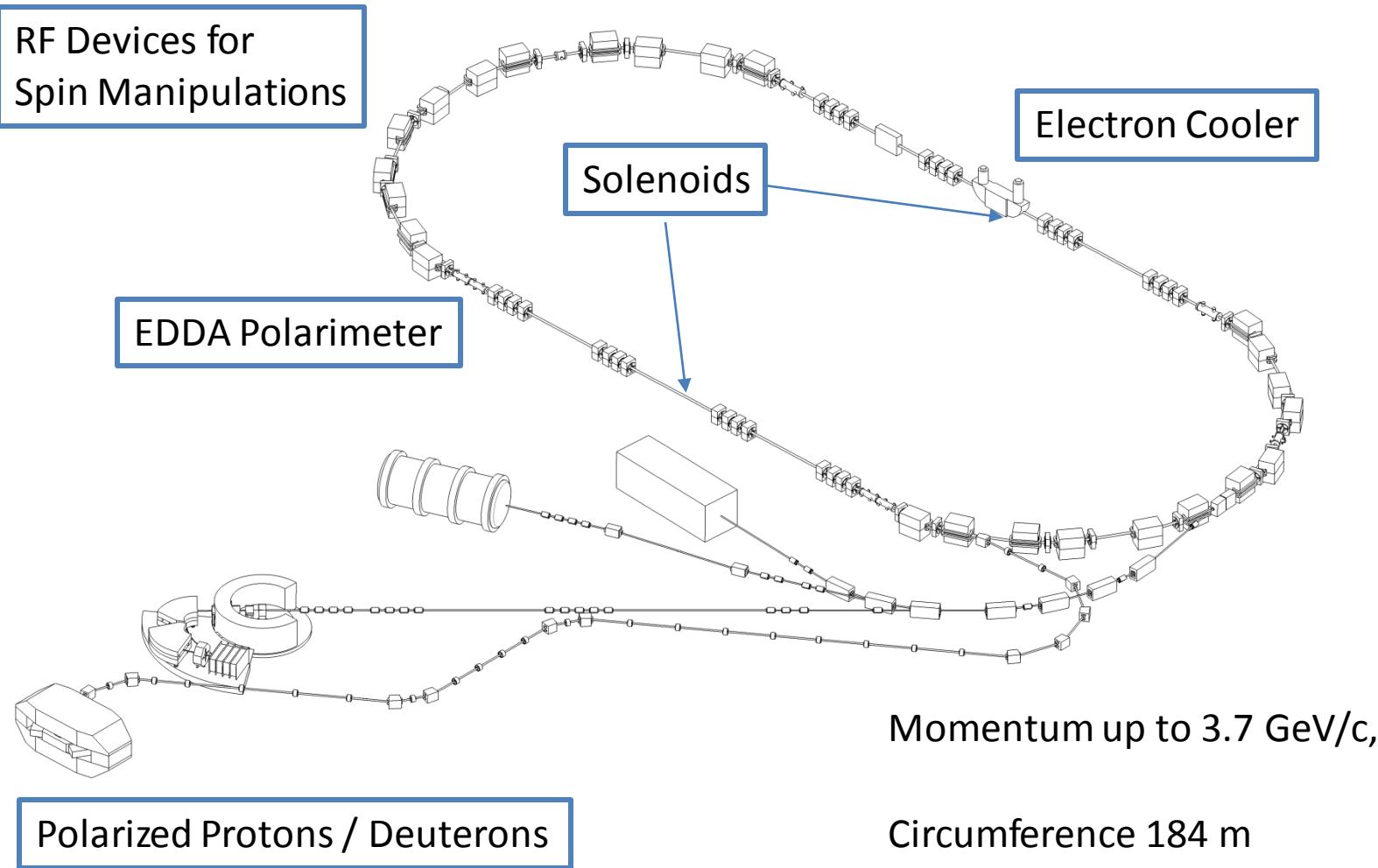
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Outline

- Exploring the COSY ring for Electric Dipole Moment (EDM) studies (JEDI - Jülich Electric Dipole moment Investigations)
- Imperfection background to EDM spin precession
- Mapping the spin tune with static solenoids
- Summary

Cooler Synchrotron COSY in Jülich



Spin Motion in Storage Ring

- *Thomas BMT eqn. for the Magnetic Dipole Moment (MDM)*

$$\frac{d\vec{S}}{dt} = \vec{S} \times \vec{\Omega}_{MDM}$$

$$\vec{\Omega}_{MDM} = \frac{q}{m} \left(\textcolor{blue}{G} \vec{B} - \left(G - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} - \frac{G\gamma}{\gamma + 1} \vec{\beta} (\vec{\beta} \cdot \vec{B}) \right)$$

Spintune := Number of spin turns relative to particle turns,
for the ideal pure magnetic ring like COSY:

$$\nu_s := \frac{|\vec{\Omega}_{MDM}|}{\omega_{rev}} = \frac{\frac{q}{m} GB}{\frac{q}{m\gamma} B} = \gamma G$$

Spin Precession by EDM in Pure Magnetic Ring

- If particle has $d \neq 0$, T-BMT equation takes form

$$\frac{d\vec{S}}{dt} = -\frac{q}{m} (G\vec{B} + \eta(\vec{\beta} \times \vec{B})) \times \vec{S}(t)$$

- Interaction of the EDM with the motional E-field tilts the stable spin axis (or “spin closed orbit”):

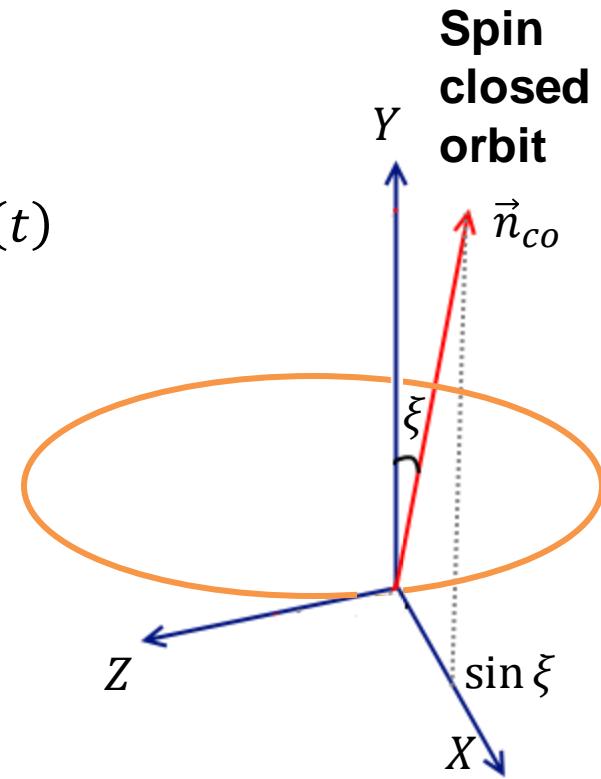
$$\vec{n}_{co} = (\vec{e}_x \sin \xi + \vec{e}_y \cos \xi)$$

$$\tan \xi = -\frac{\eta}{G} \beta \quad \eta = d \frac{m}{q}$$

- Observable spin evolution:

$$\vec{S}(t) = \hat{R}(\vec{n}_{co}, \nu_s) \vec{S}(0)$$

- The JEDI Collaboration aims at a first direct measurement of the deuteron and proton Electric Dipole Moment (EDM) at COSY



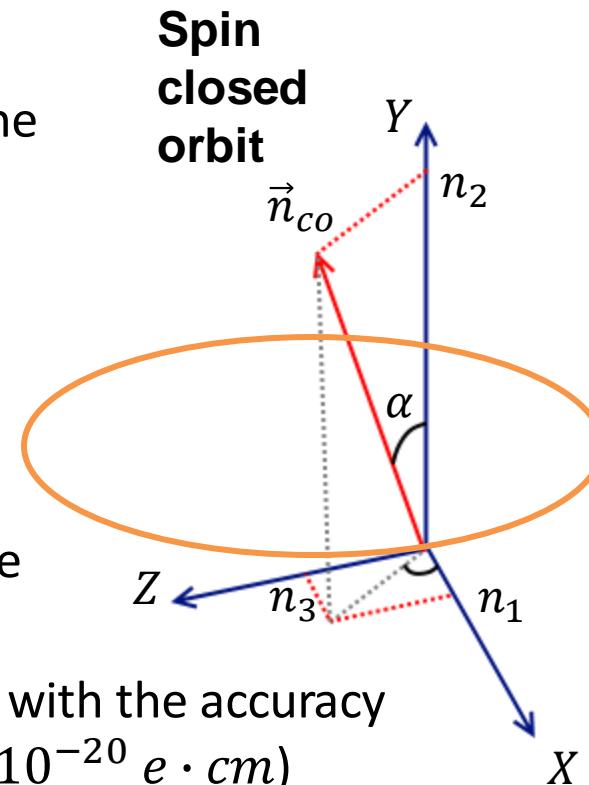
Imperfection In-plane Fields

- A current task for JEDI: exploring the EDM dynamics and systematic limitations of the EDM searches at all magnetic rings
- Misalignment of any magnetic elements produces the in-plane imperfection magnetic fields
- Imperfection spin kicks perturb \vec{n}_{co} and v_s :

$$\vec{n}_{co} = (\vec{e}_x n_1 + \vec{e}_y n_2 + \vec{e}_z n_3)$$

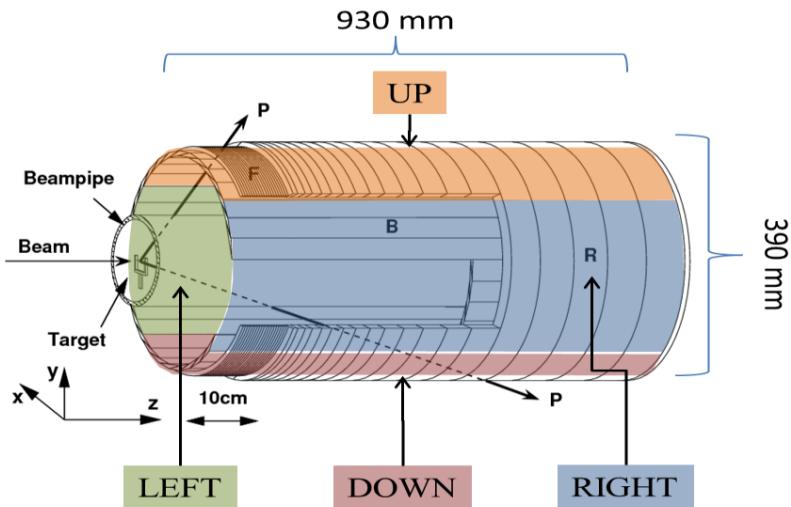
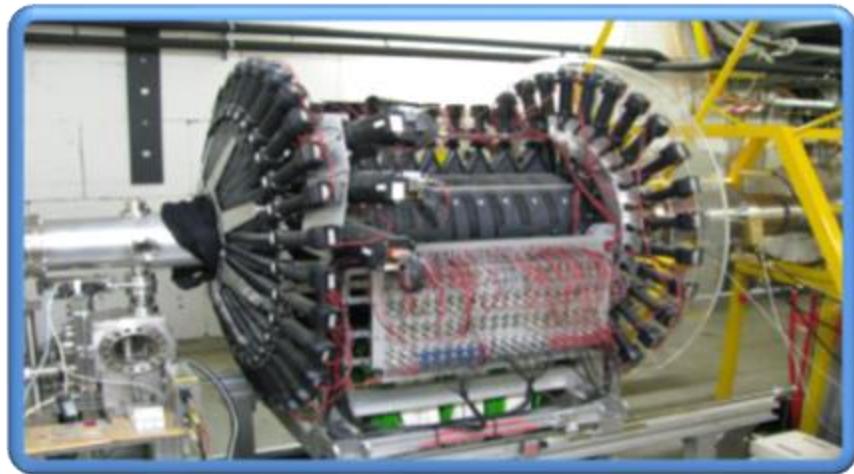
$$v_s = G\gamma + O(a^2)$$
- The nonvanishing n_1 and n_3 generate a background to the EDM-signal of the ideal imperfection-free case

$$n_1 = \sin \xi, \quad n_3 = 0$$
- The challenge is to control background (for example with the accuracy $n_1 \sim 10^{-6} \text{ rad}$ would amount to sensitivity for $d = 10^{-20} e \cdot \text{cm}$)



EDDA Polarimeter

- **Left-Right** asymmetry
⇒ **vertical** polarization
$$P_V \propto \epsilon_{ver} = \frac{N_l - N_r}{N_l + N_r}$$
- **Up-Down** asymmetry
⇒ **horizontal** polarization
$$P_H \propto \epsilon_{hor} = \frac{N_{up} - N_{dn}}{N_{up} + N_{dn}}$$



Spin Tune Measurement

- Spin vector precesses with $f_{\text{Spin}} = \nu_s f_{\text{rev}}$ in the horizontal plane around spin closed orbit \vec{n}_{co}
- Asymmetry is given by:

$$\epsilon_{hor}(t) = \frac{N_{up} - N_{dn}}{N_{up} + N_{dn}} \approx AP(t) \sin(2\pi\nu_s f_{\text{rev}} t + \phi)$$

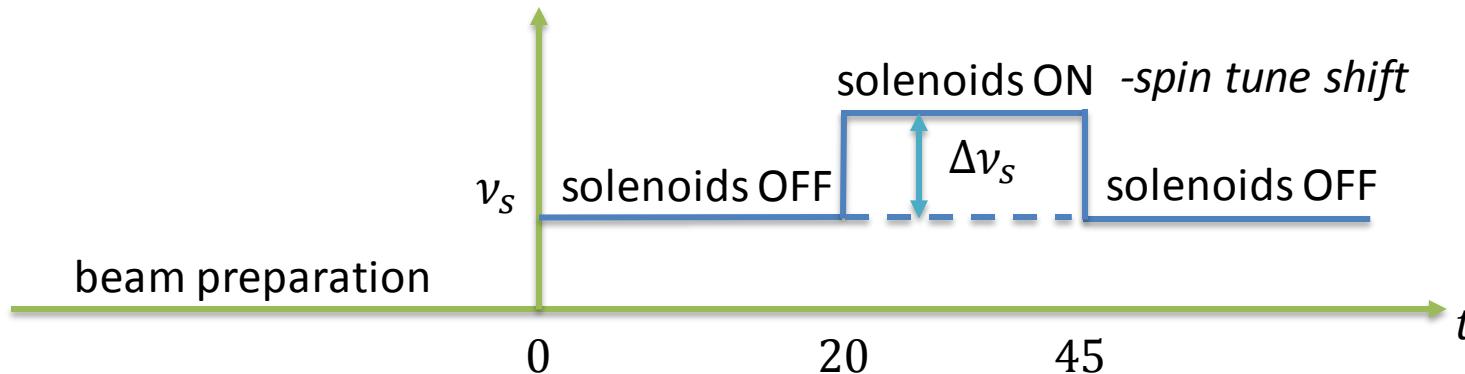
- What do we expect? (Deuterons, $p = 0.97 \text{ GeV}/c$)
 $\nu_s \approx 0.16, \quad f_{\text{rev}} = 750 \text{ kHz}$
- Spin precession frequency: $\nu_s \cdot f_{\text{rev}} \approx 120 \text{ kHz}$
- Special spin tune analysis software resolves ν_s with an accuracy 10^{-8} in 1-second interval

Spin Tune Response to the Artificial Imperfections

- The spin tune is perturbed by spin kicks in the ring imperfection fields:

$$\nu_s = G\gamma + O(n_1^2, n_3^2)$$
- The idea is to probe the in-plane imperfection fields by introducing well-known *artificial imperfections*.
- Artificial imperfections: spin kicks χ_1 and χ_2 by compensation solenoids from e-coolers in straight sections

$$\nu_s + \Delta\nu_s = G\gamma + O(n_1^2, n_3^2, \chi_1^2, \chi_2^2)$$
- Perform the measurement:

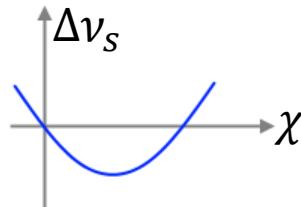


Probing the ring imperfections

- Parabolic dependency of spin tune w.r.t. artificial imperfection spin kick χ , depends on the ring \vec{n}_{co} at the point of the applied kick
- If spin kick is from pure solenoid field, then:

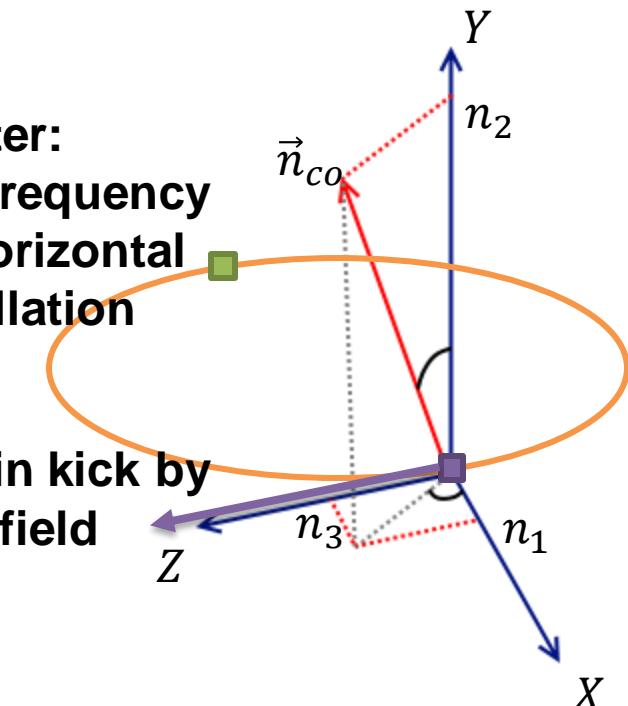
$$\cos \pi(\nu_s + \Delta\nu_s) = \cos \pi\nu_s \cos \frac{\chi}{2} + n_3 \sin \pi\nu_s \sin \frac{\chi}{2}$$

- where $\Delta\nu_s$ is spin tune shift:



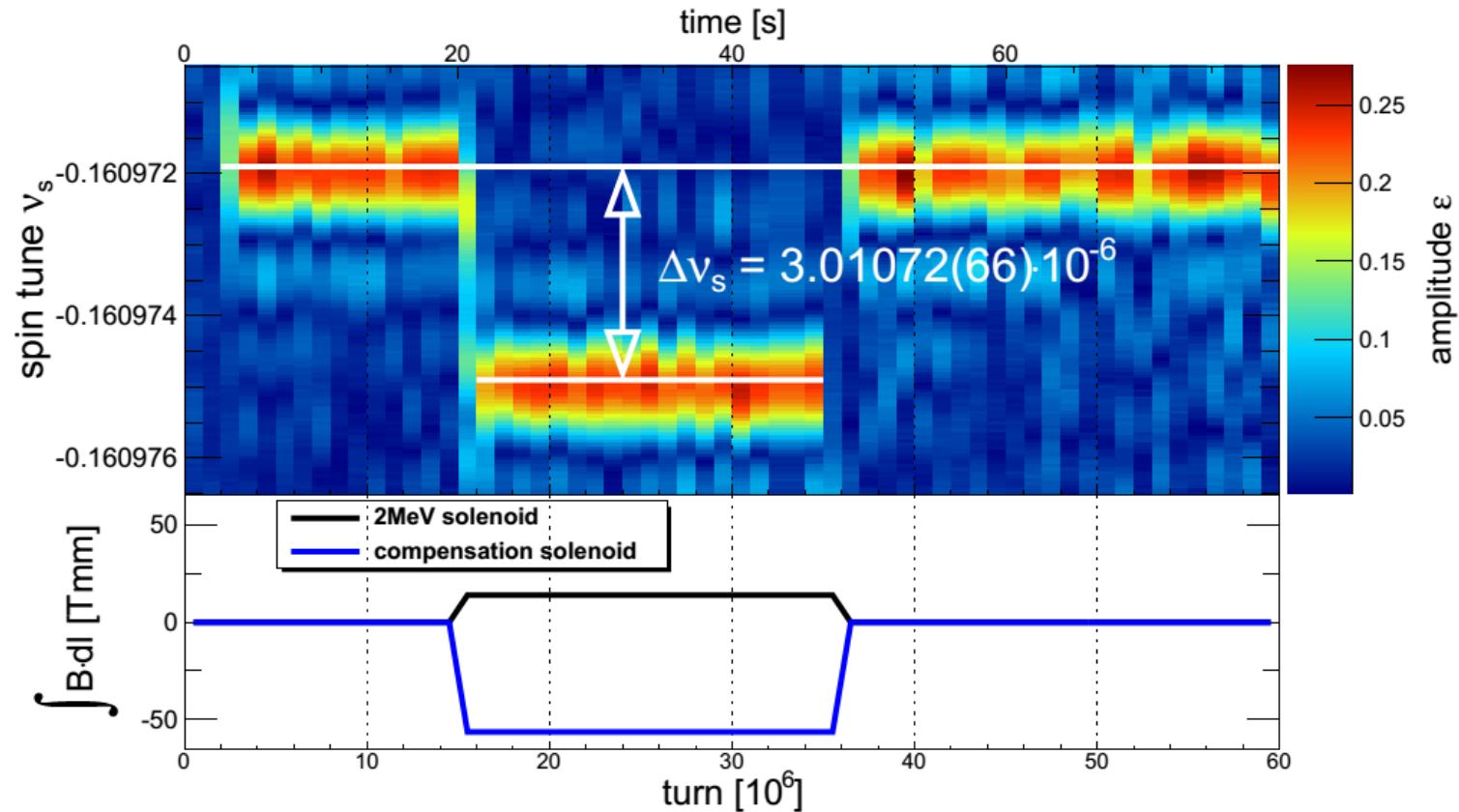
Polarimeter:
 observe frequency
 shift in horizontal
 spin oscillation

Apply spin kick by
 solenoid field



Measurement of Spin Tune Shift

- Spin tune shift registered in the data analysis:



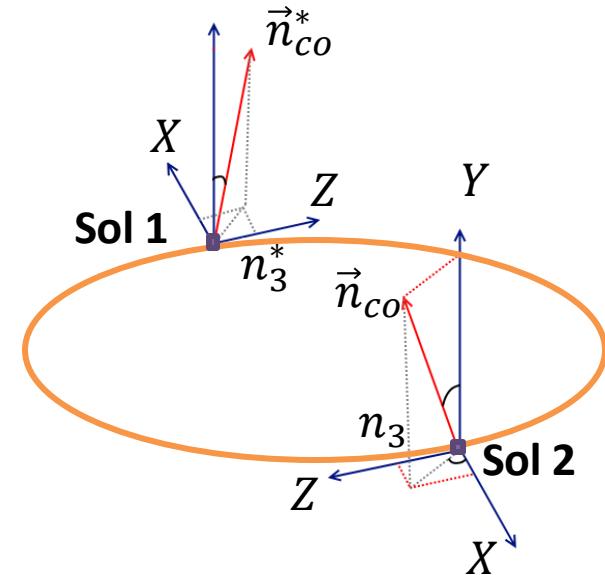
- The spin tune shift was observed at $t = [20, 45]$ s

Two solenoids probe \vec{n}_{co} at 2 points of the ring

- When 2 solenoids turned on simultaneously:

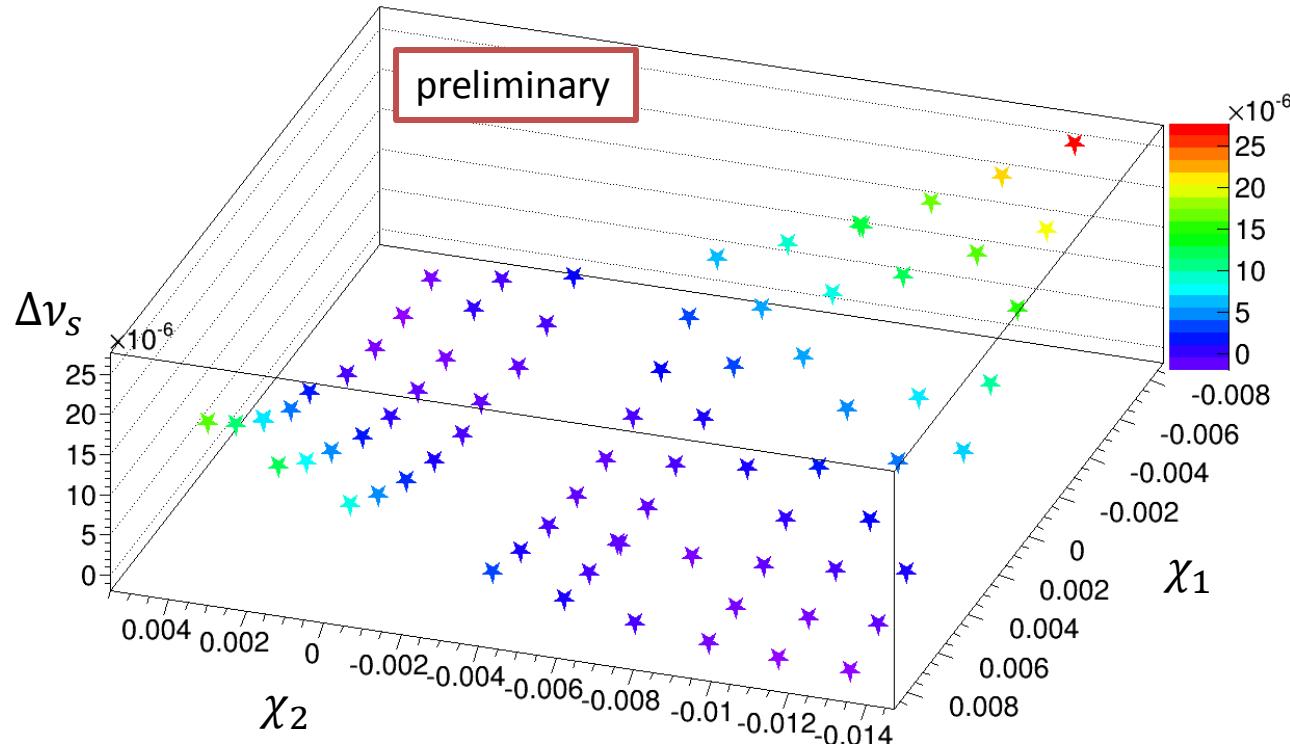
$$\begin{aligned} \cos \pi(\nu_s + \Delta\nu_s) = & \cos \pi\nu_s \cos \frac{\chi_1}{2} \cos \frac{\chi_2}{2} - \sin \pi\nu_s n_3^* \sin \frac{\chi_1}{2} \cos \frac{\chi_2}{2} \\ & - E \sin \frac{\chi_1}{2} \sin \frac{\chi_2}{2} - \sin \pi\nu_s n_3 \sin \frac{\chi_2}{2} \cos \frac{\chi_1}{2} \end{aligned}$$

- ν_s - base spin tune
- $\Delta\nu_s$ - a spin tune shift
- $E \approx 1$
- Any deviation from $\Delta\nu_s(\chi_1, \chi_2)$ -dependence is related to field errors and orbit perturbation



The Spin Tune Mapping

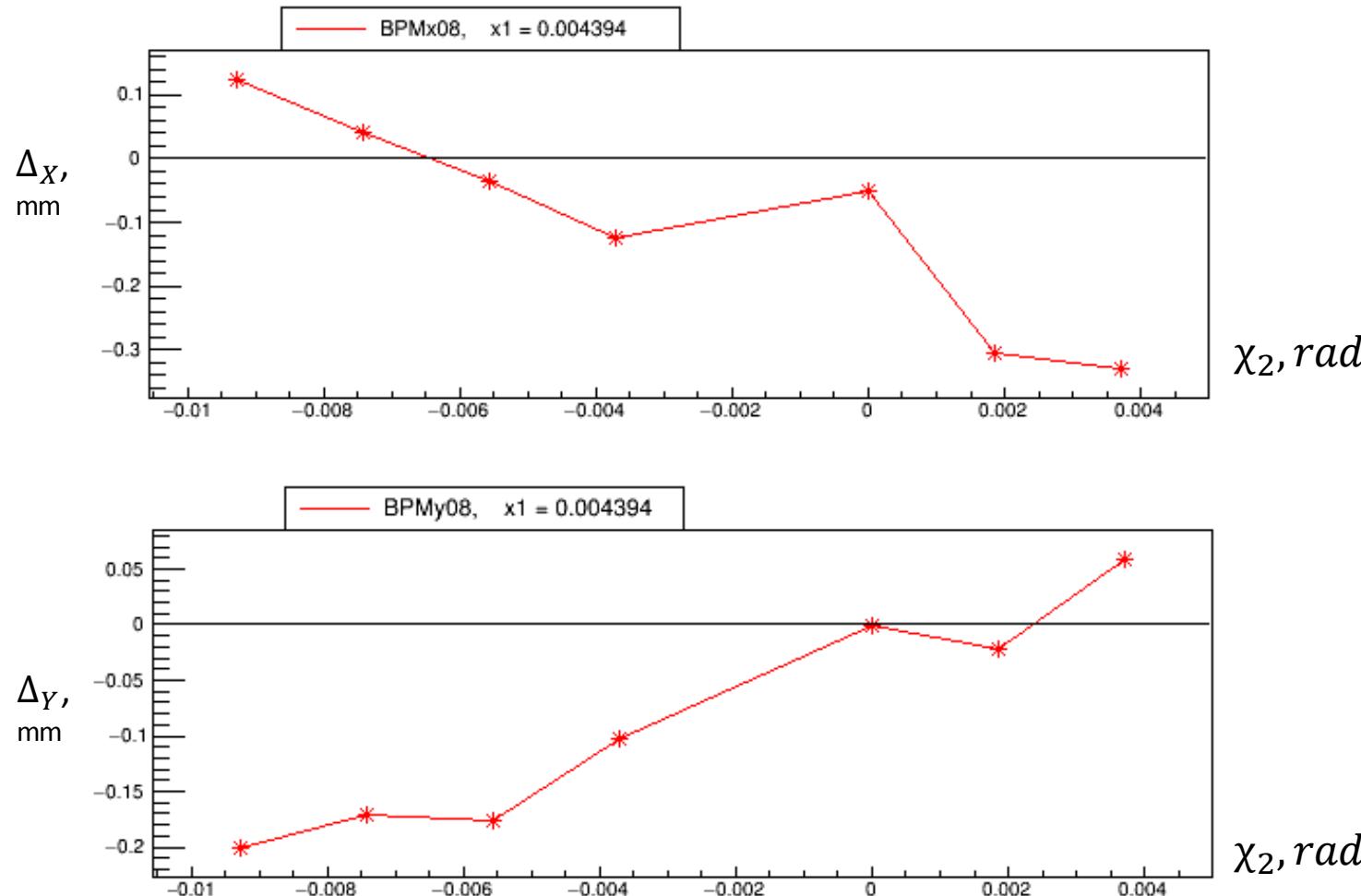
Take multiple measurements with different χ_1, χ_2 and build a spin tune map $\Delta\nu_s(\chi_1, \chi_2)$:



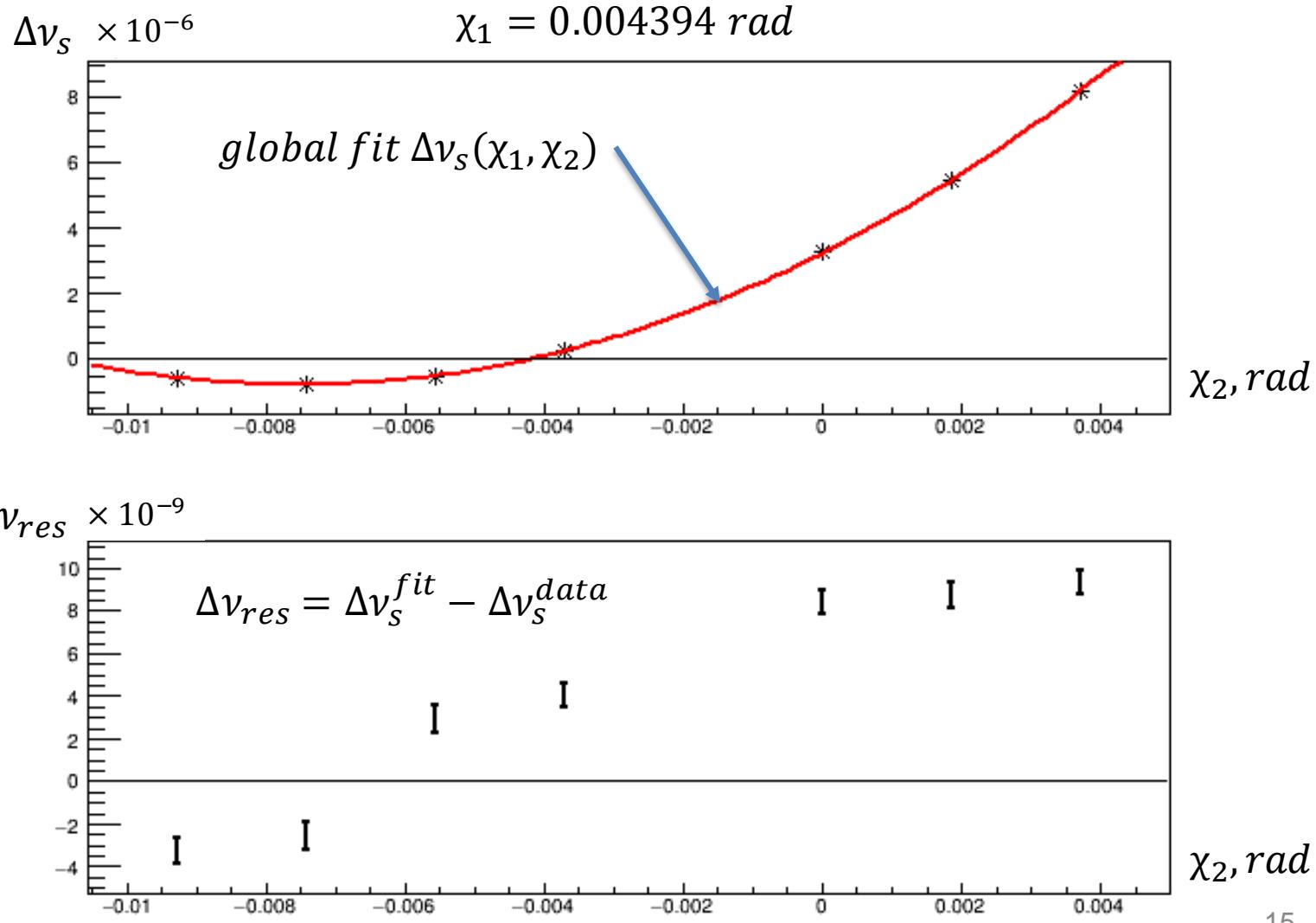
- Spin tune shift w.r.t. the solenoid spin kicks, $\Delta\nu_s \sim \chi_1^2, \Delta\nu_s \sim \chi_2^2$

The orbit perturbation by solenoid

- Relative orbit shift measured by one of the BPMs when solenoids are turned on:



The spin tune perturbation by solenoid



The Spin Tune Mapping

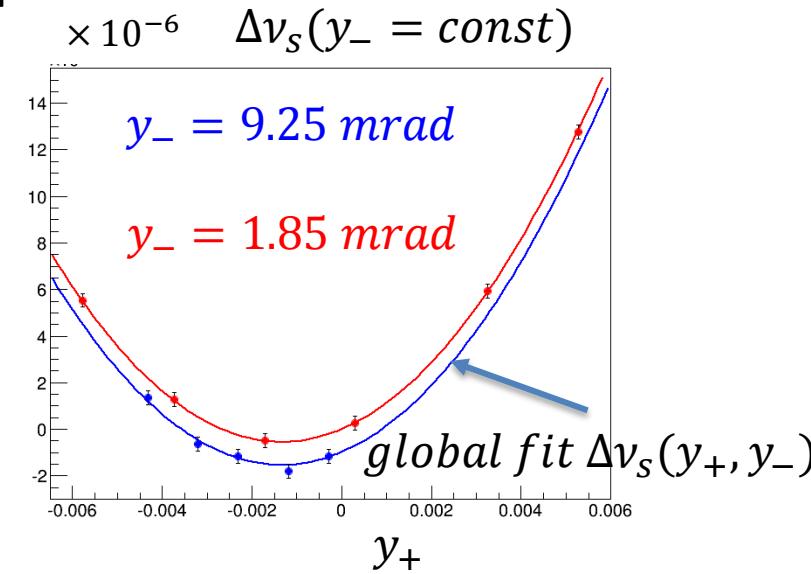
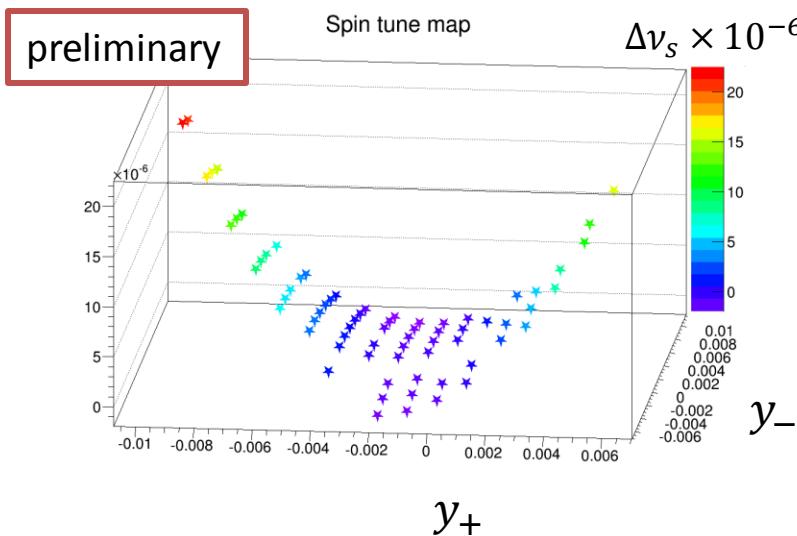
- If the kicks are translated to:

$$y_+ = \frac{1}{2}(\chi_1 + \chi_2) \quad y_- = \frac{1}{2}(\chi_1 - \chi_2)$$

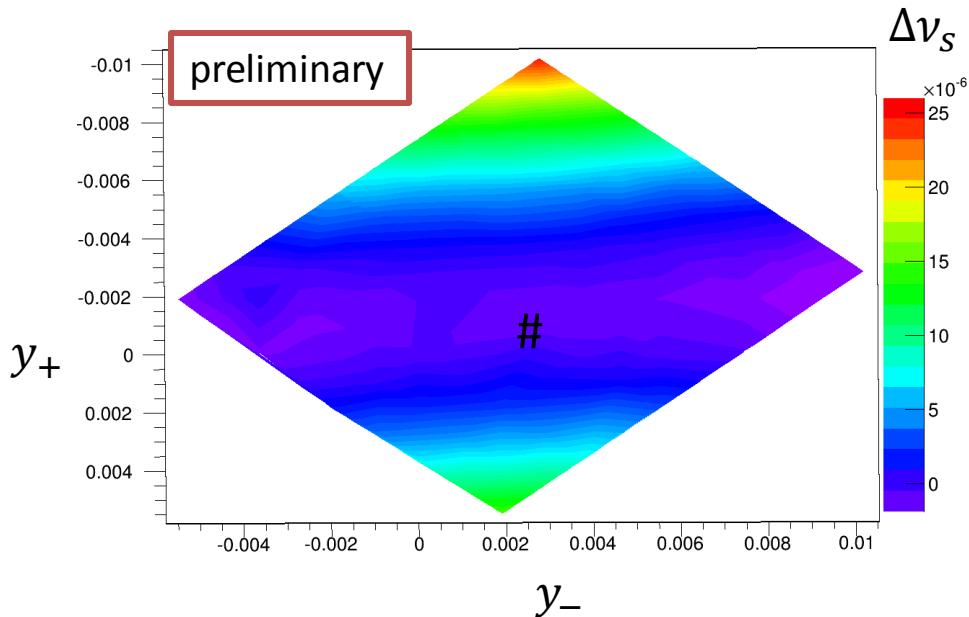
- then

$$\Delta\nu_s \propto -(y_- - a_-)^2, \quad \Delta\nu_s \propto (y_+ - a_+)^2$$

- The distributions of the data points in y_{\pm} dimension share common parabolic features : equal curvature and extremum a_{\pm}
- It is a sign that the solenoids work as anticipated



Imperfection Strength



The fitted saddle point at #:

$$a_+ = -0.00111077 \pm 6.1 * 10^{-8} \text{ rad}$$

$$a_- = 0.00244326 \pm 2.1 * 10^{-7} \text{ rad}$$

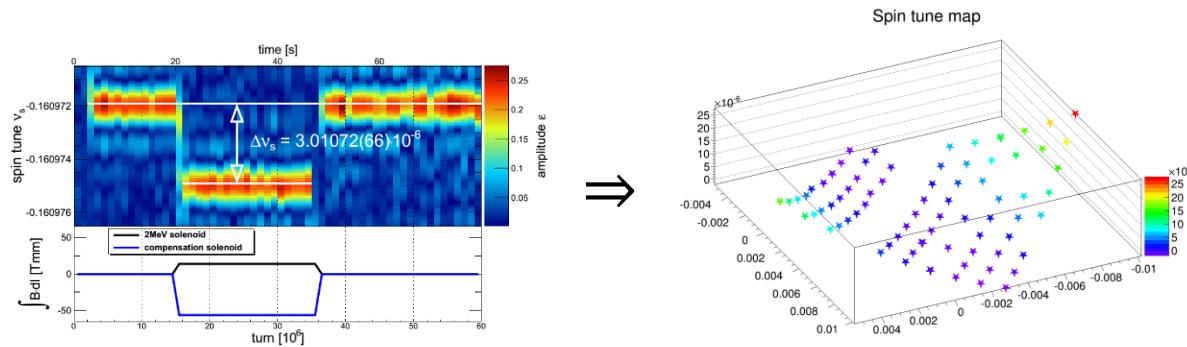
$$n_3 = -0.00299124 \pm 1.8 * 10^{-7}$$

$$n_3^* = -0.00163653 \pm 7.1 * 10^{-8}$$

- Position of the saddle point measures projections of SCO, n_3 and n_3^*
- Strength of imperfection fields in the ring is at the level of $\approx 3 \text{ Tmm}$
- For an ideal ring, the saddle point would be at $a_{\pm} = 0$

Summary

- The technique of spin tune measurement appears as a precision tool for the systematic analysis of the ring imperfections
- First high precision measurement of the imperfection fields at COSY



- ❖ The ultimate goal of the JEDI: to understand the EDM dynamics in storage rings as a prerequisite to the construction of the dedicated storage ring for the EDM searches

More Details About Spin Tune Analysis

Sorting the Events

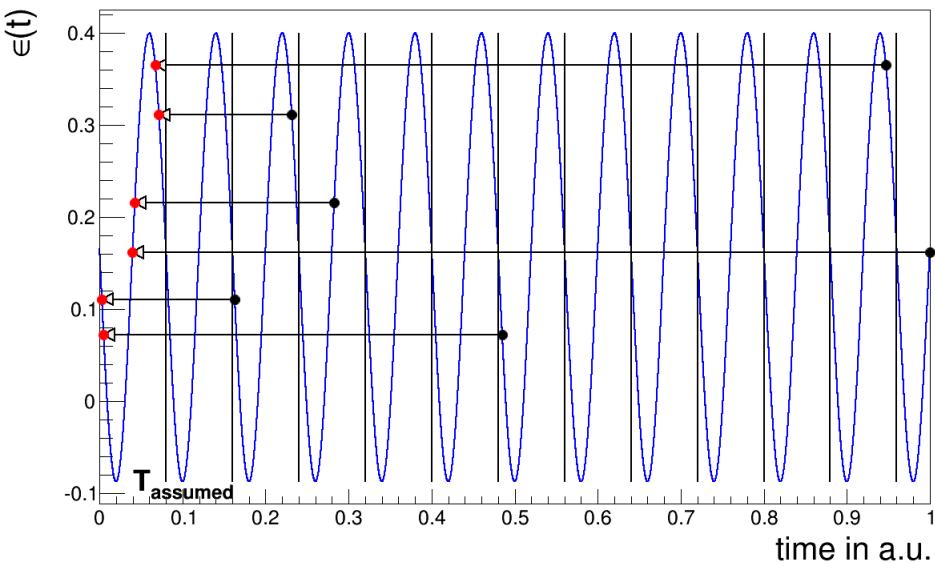
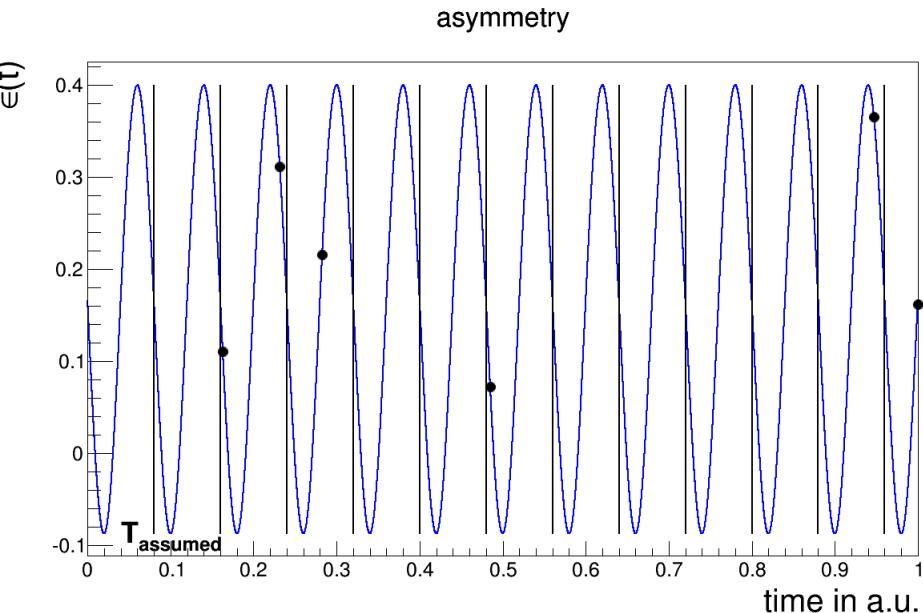
1. Assume Spin Tune $\nu_{assumed}$

$$T_{assumed} = \frac{2\pi}{\nu_{assumed} f_{rev}}$$

2. Map all events of a macroscopic time interval (2s) in first period:

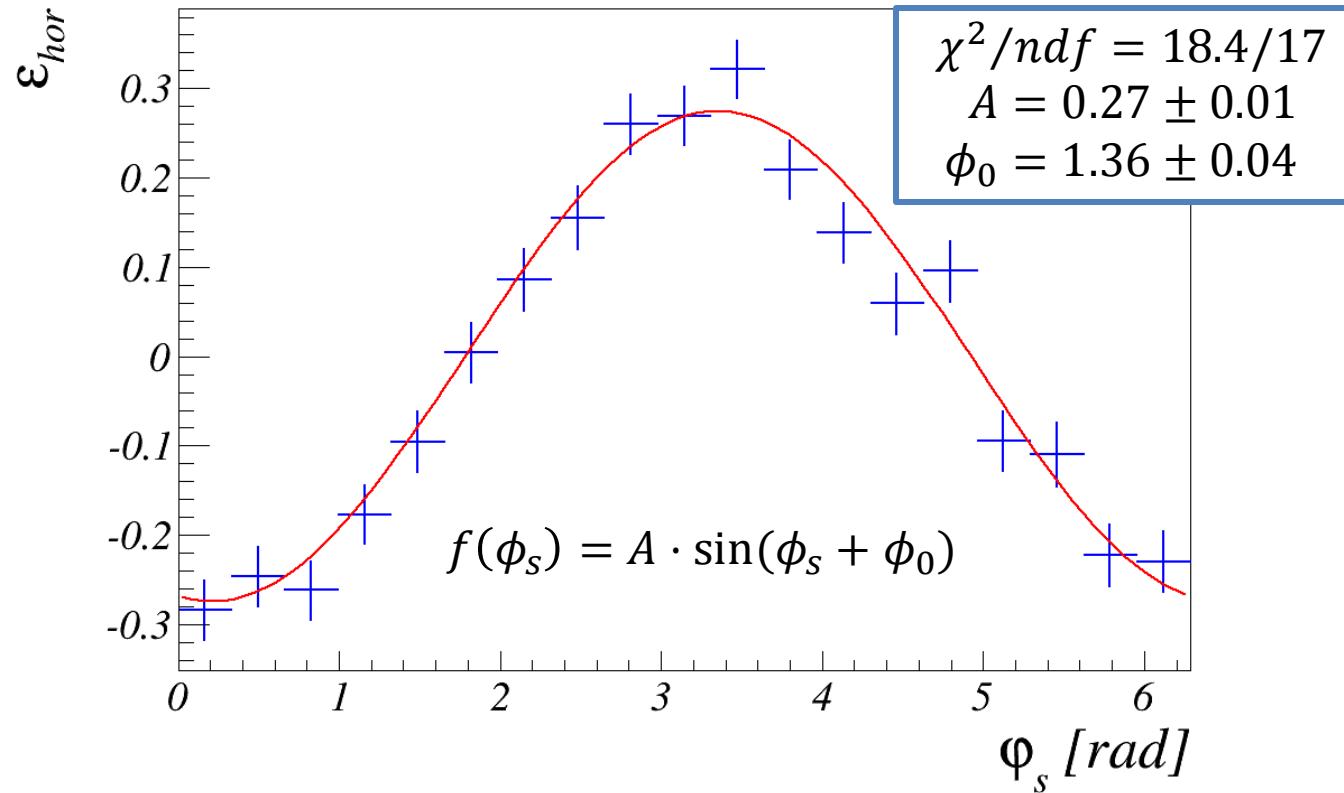
$$t' = \text{mod}(t, T_{assumed})$$

3. Fit asymmetry to first period



Fit Asymmetry to First Period

1. $T_{assumed}$
2. Mapping events
3. Fit asymmetry to first period

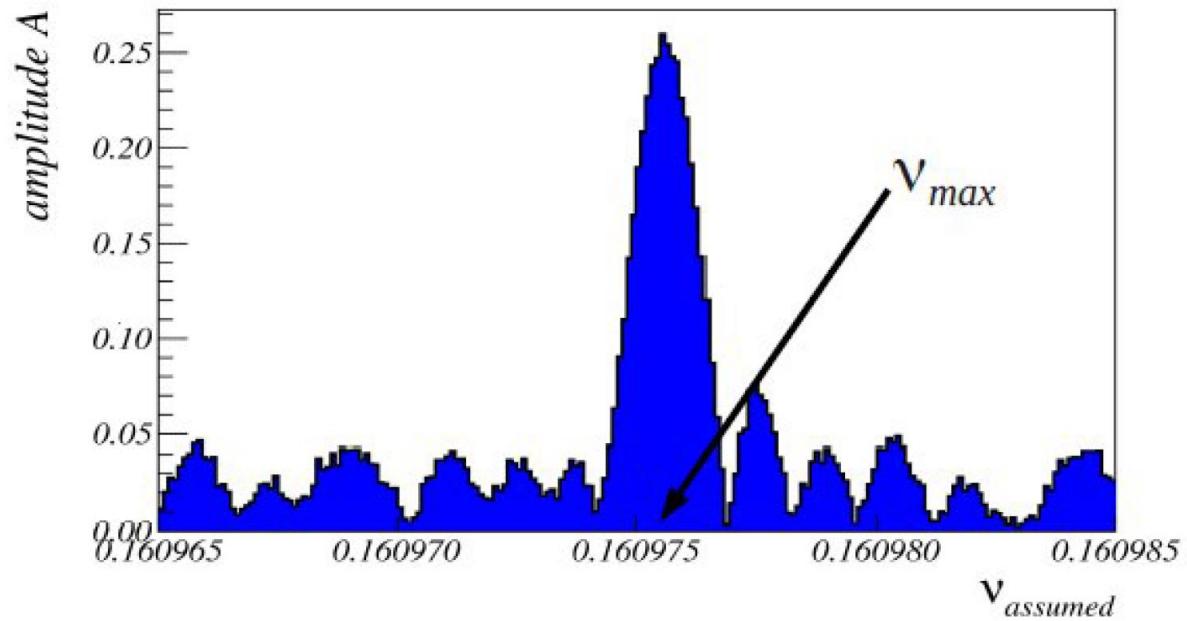


Extract amplitude $A \propto$ Polarisation

Find Correct Spin Tune

1. $T_{assumed}$
2. Sorting events
3. Fit asymmetry to first period

- Vary $T_{assumed}$ and repeat steps 1 to 3
- Plot extracted parameter A vs $\nu_{assumed}$



- ν_{max} is correct spine tune in macroscopic time interval (2 s)
- $\nu_{max} = 0.160975 \pm 10^{-6}$