

The electric dipole moment of light nuclei in effective field theory

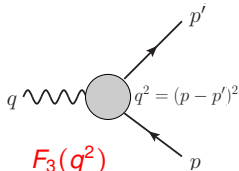
Jülich-Bonn Collaboration (JBC):

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David Minossi, Andreas Nogga, Jordy de Vries, A.W.

Permanent EDMs and Form Factors

- $\langle f(p') | J_{\text{em}}^\mu | f(p) \rangle = \bar{u}_f(p') \Gamma^\mu(q^2) u_f(p)$

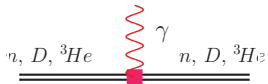


$$\Gamma^\mu(q^2) = \gamma^\mu F_1(q^2) - i\sigma^{\mu\nu} q_\nu \frac{F_2(q^2)}{2m_f} + \sigma^{\mu\nu} q_\nu \gamma_5 \frac{F_3(q^2)}{2m_f} + (\not{q} q^\mu - q^2 \gamma^\mu) \gamma_5 F_a(q^2) / m_f^2$$

Dirac $F_1(q^2)$, Pauli $F_2(q^2)$, **electric dipole $F_3(q^2)$** , and anapole $F_a(q^2)$ FFs
(here for a fermion of mass m_f with spin $s = 1/2$)

$$d := \lim_{q^2 \rightarrow 0} \frac{F_3(q^2)}{2m_f}, \quad (q \equiv p - p', \text{ electron charge } e < 0)$$

EDMs from ~~CP~~ Formfactor $F_3(q^2=0)/(2m)$



Outline:

- **CP-violation** beyond CKM matrix in the SM: \mathcal{L}_{QCD} θ -term (dim. 4)
 - EDM of the deuteron / EDM of helium-3
 - strategies of testing the $\bar{\theta}$ -term

- **CP-violation** from physics beyond the SM: SUSY, multi-Higgs, ...
 - dim. 6 sources: qEDM, qCEDM, gCEDM, 4qEDMs
 - EDM of the deuteron / EDM of helium-3
 - disentangling dim. 6 sources

The $\mathcal{L}_{\text{QCD}} \theta$ -Term

topologically non-trivial vacuum \rightarrow ~~CP~~ term in \mathcal{L}_{QCD} :

$$\mathcal{L} = \mathcal{L}_{\text{QCD}}^{\text{CP}} + \theta \frac{g_S^2}{32\pi^2} G_{\mu\nu}^a \tilde{G}^{a,\mu\nu}$$

$$\dots + \theta \frac{g_S^2}{32\pi^2} G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} \xrightarrow{U_A(1)} \dots - \bar{\theta} m^* \sum_{f=u,d} \bar{q}_f i\gamma_5 q_f$$

with $\bar{\theta} = \theta + \arg \text{Det } \mathcal{M}$, naive dim. analysis (NDA): $\bar{\theta} \sim \mathcal{O}(1)$

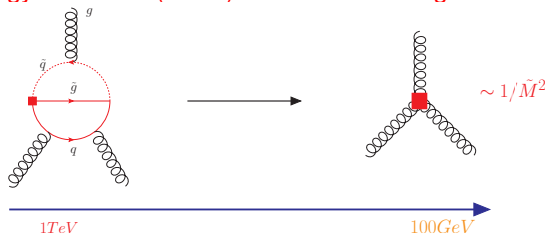
\mathcal{M} : quark mass matrix, $m^* = \frac{m_u m_d}{m_u + m_d}$

New Physics Beyond Standard Model (BSM)

SUSY, multi-Higgs, Left-Right-Symmetric models, ...

Effective field theory approach:

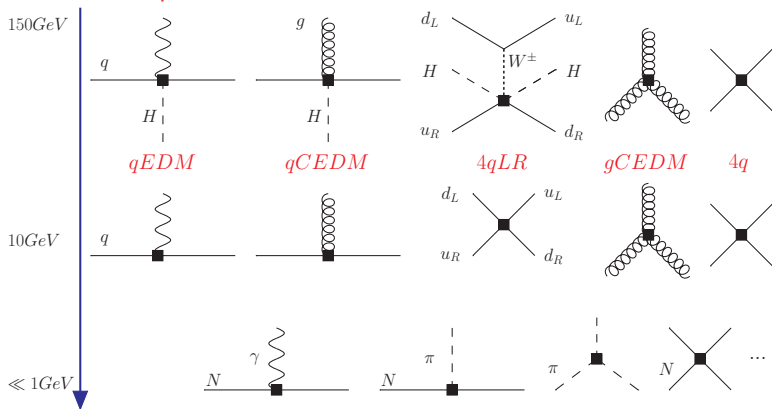
- All degrees of freedom beyond a specified scale are integrated out:
 \hookrightarrow Only SM degrees of freedom remain: q, g, H, W^\pm, \dots
- Relics of eliminated BSM physics 'remembered' by the values of the low-energy constants (LECs) of the CP-violating contact terms, e.g.



BSM physics continued: CP-violating dim. 6 sources

Removal of the Higgs and transition to hadronic fields (plus mixing)

Add to SM all possible T- and P-odd contact interactions



θ -Term on the Hadronic Level

hadronic level: non perturbative techniques required: e.g. 2-flavor ChPT

- Symmetries of QCD preserved by the effective field theory (EFT)

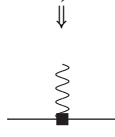
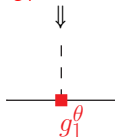
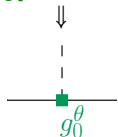
$$\mathcal{L}_{QCD}^\theta = -\bar{\theta} m^* \sum_f \bar{q}_f i \gamma_5 q_f: \quad \mathcal{CP}, I \quad \Leftrightarrow \quad \mathcal{M} \rightarrow \mathcal{M} + \bar{\theta} m^* i \gamma_5 \quad m^* = \frac{m_u m_d}{m_u + m_d}$$

\mathcal{CP}, I

\mathcal{CP}, I

$\mathcal{CP}, I + I$

$$\mathcal{L}_\theta^{ChPT} = g_0^\theta N^\dagger \vec{\pi} \cdot \vec{\tau} N \quad + \quad g_1^\theta N^\dagger \pi_3 N \quad + \quad N^\dagger (b_0 + b_1 \tau_3) S^\mu \nu^\nu F_{\mu\nu} N \quad + \dots$$



dominating
for n, p & ${}^3\text{He}$

dominating
for D

important for
 n, p

Lebedev et al. (2004), Mereghetti et al. (2010), Bsaisou et al. (2013)

θ -term: \mathcal{CP} πNN vertices determined from LECs

Leading g_0^θ coupling (from c_5)

Crewther et al. (1979);
 Ottnad et al. (2010); Mereghetti et al. (2011);
 de Vries et al. (2011); Bsaisou et al. (2013)

g_0^θ : $N^\dagger \vec{\pi} \cdot \vec{\tau} N$ -vertex

$$\mathcal{L}_{\pi N} = \dots + c_5 2B N^\dagger \left((m_u - m_d) \tau_3 + \frac{2m^* \bar{\theta}}{F_\pi} \vec{\pi} \cdot \vec{\tau} \right) N + \dots$$

$$\delta M_{np}^{str} = 4B(m_u - m_d)c_5 \quad \rightarrow \quad g_0^\theta = \bar{\theta} \delta M_{np}^{str} (1 - \epsilon^2) \frac{1}{4F_\pi \epsilon}$$

$$\delta M_{np}^{em} \quad \rightarrow \quad \delta M_{np}^{str} = (2.6 \pm 0.5) \text{MeV} \quad \text{Walker-Loud et al. (2012)}$$

$$\rightarrow \quad g_0^\theta = (-0.018 \pm 0.007) \bar{\theta}$$

$$\epsilon = (m_u - m_d)/(m_u + m_d), \quad 4Bm^* = M_\pi^2(1 - \epsilon^2), \quad m^* = \frac{m_u m_d}{m_u + m_d}$$

θ -term: subleading g_1^θ coupling (from c_1 LEC)

g_1^θ : $\pi_3 NN$ -vertex

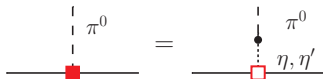
$$\epsilon := (m_u - m_d)/(m_u + m_d)$$

$$\mathcal{L}_{\pi N} = \dots + c_1 4B N^\dagger \left((m_u + m_d) + \frac{(\delta M_\pi^2)_{QCD} (1 - \epsilon^2) \bar{\theta}}{2BF_\pi \epsilon} \pi_3 \right) N + \dots$$

1 $c_1 \longleftrightarrow \sigma_{\pi N}$: $c_1 = (-1.0 \pm 0.3) \text{ GeV}^{-1}$

Compilation: Baru et al. (2011)

2 $(\delta M_\pi^2)_{QCD} \approx \frac{\epsilon^2}{4} \frac{M_\pi^4}{M_K^2 - M_\pi^2}$



$$\longrightarrow g_1^\theta = (0.003 \pm 0.002) \bar{\theta}$$

Bsaisou et al. (2013)

$$\frac{g_1^\theta}{g_0^\theta} = -0.20 \pm 0.13 \sim \frac{M_\pi}{m_N}$$

Bsaisou et al. (2013)

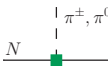
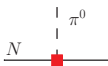


$$\gg \epsilon \frac{M_\pi^2}{m_N^2} \sim -0.01 \quad (\text{NDA})$$

de Vries et al. (2011)

$g_0^\theta (\delta M_{np}^{str})$ is unnaturally small!

Scalings of \mathcal{CP} hadronic vertices (from θ and BSM sources)

In BSM case: reliance on Naive Dimensional Analysis (NDA), lattice, ...

| | $g_0: \mathcal{CP}, I$ | $g_1: \mathcal{CP}, I$ | $d_0, d_1: \mathcal{CP}, I + I$ | $C_{3\pi}: \mathcal{CP}, I$ |
|---|---|---|--|---|
| $\mathcal{L}_{\text{EFT}}^{\mathcal{CP}}$: |  |  |  |  |
| θ -term: | $\mathcal{O}(1)$ | $\mathcal{O}(M_\pi/m_N)$ | $\mathcal{O}(M_\pi^2/m_N^2)$ | $\mathcal{O}(\epsilon M_\pi^2/m_N^2)$ |
| qEDM: | $\mathcal{O}(\alpha_{EM}/(4\pi))$ | $\mathcal{O}(\alpha_{EM}/(4\pi))$ | $\mathcal{O}(1)$ | $\mathcal{O}(\alpha_{EM}/(4\pi))$ |
| qCEDM: | $\mathcal{O}(1)$ | $\mathcal{O}(1)$ | $\mathcal{O}(M_\pi^2/m_N^2)$ | $\mathcal{O}(\epsilon M_\pi^2/m_N^2)$ |
| 4qLR: | $\mathcal{O}(M_\pi^2/m_n^2)$ | $\mathcal{O}(1)$ | $\mathcal{O}(M_\pi^2/m_N^2)$ | $\mathcal{O}(1)$ |
| gCEDM: | $\mathcal{O}(M_\pi^2/m_N^2)^*$ | $\mathcal{O}(M_\pi^2/m_N^2)^*$ | $\mathcal{O}(1)$ | $\mathcal{O}(\epsilon M_\pi^2/m_N^2)$ |
| 4q: | $\mathcal{O}(M_\pi^2/m_N^2)^*$ | $\mathcal{O}(M_\pi^2/m_N^2)^*$ | $\mathcal{O}(1)$ | $\mathcal{O}(\epsilon M_\pi^2/m_N^2)$ |

*: Goldstone theorem \rightarrow relative $\mathcal{O}(M_\pi^2/m_n^2)$ suppression of $N\pi$ interactions

θ -Term Induced Nucleon EDM

single nucleon EDM:



“controlled”

isovector

\approx

\ll

isoscalar



two “unknown” coefficients

Guo & Meißner (2012): also in SU(3) case

$$d_n|_{\text{loop}}^{\text{isovector}} = e \frac{g_{\pi NN} g_0^\theta}{4\pi^2} \frac{\ln(M_N^2/m_\pi^2)}{2M_N} \sim \bar{\theta} m_\pi^2 \ln m_\pi^2$$

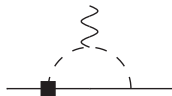
Crewther, di Vecchia, Veneziano & Witten (1979); Pich & de Rafael (1991); Otnad et al. (2010)

$$g_0^\theta = \frac{(m_n - m_p)^{\text{strong}} (1 - \epsilon^2)}{4F_\pi \epsilon} \bar{\theta} \approx (-0.018 \pm 0.007) \bar{\theta} \quad (\text{where } \epsilon \equiv \frac{m_u - m_d}{m_u + m_d})$$

$$\hookrightarrow d_n|_{\text{loop}}^{\text{isovector}} \sim -(2.1 \pm 0.9) \cdot 10^{-16} \bar{\theta} \text{ e cm} \quad \text{Otnad et al. (2010); Bsaisou et al. (2013)}$$

θ -Term Induced Nucleon EDM

single nucleon EDM:



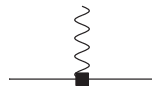
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But what about the two “unknown” coefficients of the contact terms?

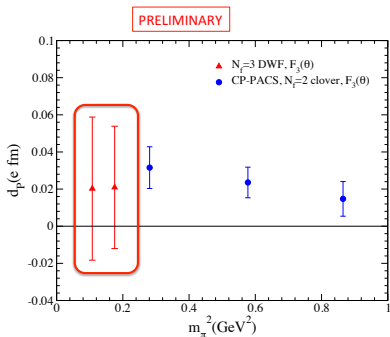
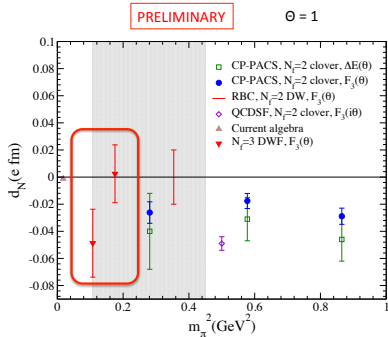
We'll always have ... the lattice

Don't mention the ... light nuclei

We'll always have ... the lattice

However, *It's a long way to Tipperary ...*

Results from *full* QCD calculations (no systematical errors!) for the
neutron EDM and **proton EDM**



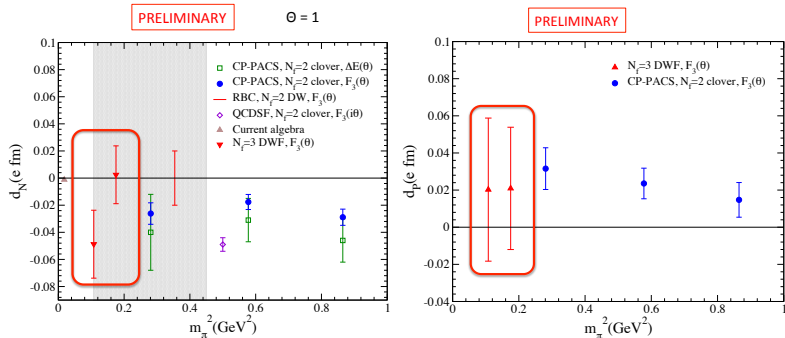
(adapted from Taku Izubuchi (BNL), *Lattice-QCD calculations for EDMs*, Fermilab, Feb. 14, 2013)

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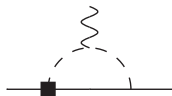
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θ -Term Induced Nucleon EDM:

Crewther, di Vecchia, Veneziano & Witten (1979); Pich & de Rafael (1991); Otnad et al. (2010)

single nucleon EDM:



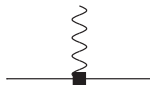
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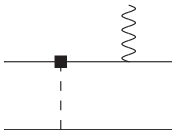
“unknown” coefficients

→ lattice QCD required

Guo, Meißner (2012)

two nucleon EDM:

Sushkov, Flambaum, Khriplovich (1984)



controlled

\gg

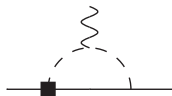


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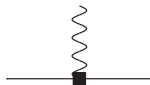
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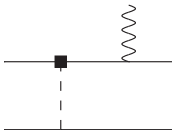
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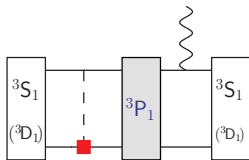
controlled

\gg



unknown coefficient

EDM of the Deuteron at LO: quantitative θ -term results



LO: $g_0^\theta N^\dagger \vec{\pi} \cdot \vec{\tau} N$ (\mathcal{CP}, I) \rightarrow Isospin excl.

NLO: $g_1^\theta N^\dagger \pi_3 N$ (\mathcal{CP}, I) \rightarrow "LO"

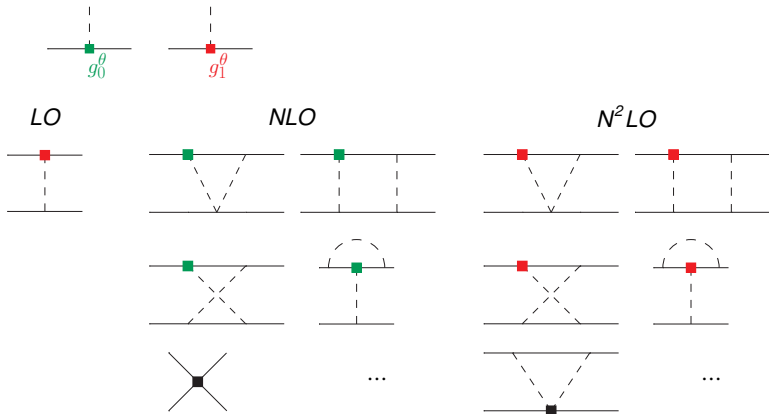
in units of $g_1^\theta e \cdot \text{fm} \cdot (g_A m_N / F_\pi)$

| Ref. | potential | no 3P_1 -int | with 3P_1 -int | total |
|--------------|-------------------------------|------------------------|------------------------|------------------------|
| JBC (2013)* | AV_{18} | -1.93×10^{-2} | $+0.48 \times 10^{-2}$ | -1.45×10^{-2} |
| JBC (2013) | CD Bonn | -1.95×10^{-2} | $+0.51 \times 10^{-2}$ | -1.45×10^{-2} |
| JBC (2013)* | ChPT (N^2 LO) [†] | -1.94×10^{-2} | $+0.65 \times 10^{-2}$ | -1.29×10^{-2} |
| Song (2013) | AV_{18} | - | - | -1.45×10^{-2} |
| Liu (2004) | AV_{18} | - | - | -1.43×10^{-2} |
| Afnan (2010) | Reid 93 | -1.93×10^{-2} | $+0.40 \times 10^{-2}$ | -1.43×10^{-2} |

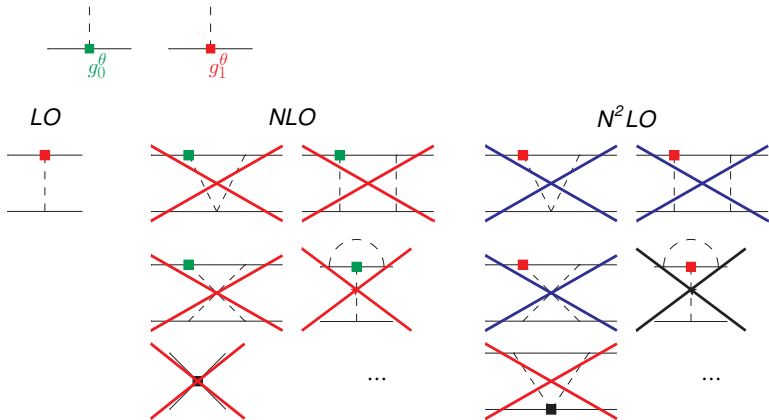
*: in preparation †: cutoffs at 600 MeV (LS) and 700 MeV (SFR)

BSM \mathcal{CP} sources: LO g_1 πNN -vertex also exists in qCEDM and 4qLR cases

EDM of the Deuteron: NLO - and N^2LO -Potentials

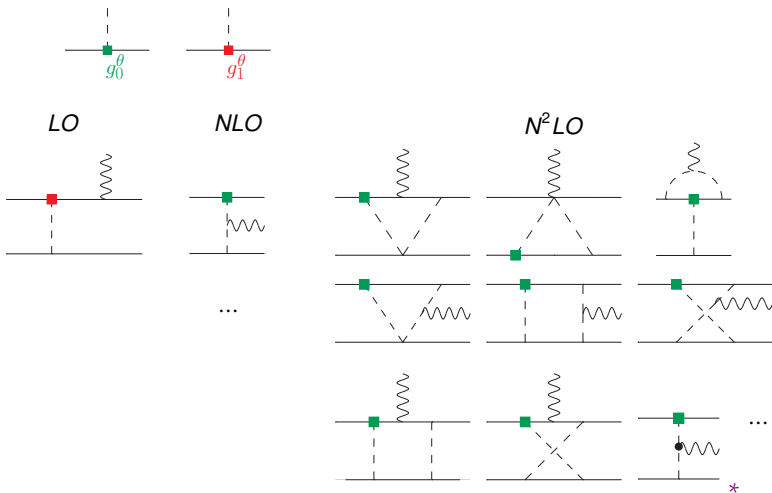


EDM of the Deuteron: NLO - and N^2LO -Potentials



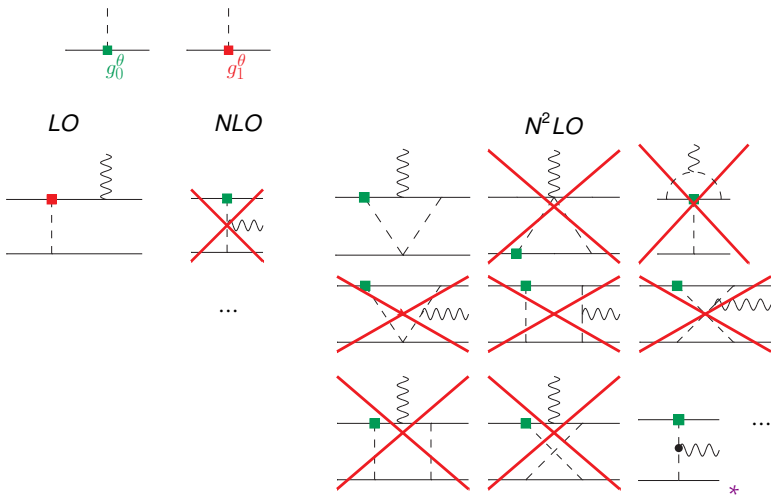
- ✗: vanishing by selection rules, ✗: sum of diagrams vanishes
✗: vertex correction

EDM of the Deuteron: NLO - and N^2LO -Currents



*: de Vries et al. (2011), Bsaisou et al. (2013)

EDM of the Deuteron: NLO - and N^2LO -Currents



*: de Vries et al. (2011), Bsaisou et al. (2013)

- \times : vanishing by selection rules, \times : sum of diagrams vanishes

Deuteron EDM from the $\bar{\theta}$ -term

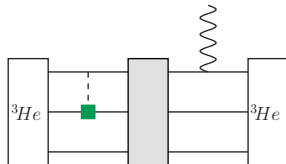
Bsaisou et al. (2013)

total deuteron EDM: $d_D = d_n + d_p + d_D(2N)$

- single-nucleon contribution: EFT *alone* has no predictive power
 → *Experiment or Lattice QCD* needed in addition
- two-nucleon contribution $d_D(2N)$: EFT *has* predictive power

$$d_D(2N) = \underbrace{-(0.59 \pm 0.39) \cdot 10^{-16} \bar{\theta} \text{ e cm}}_{\text{LO}} + \underbrace{(0.05 \pm 0.02) \cdot 10^{-16} \bar{\theta} \text{ e cm}}_{\text{N}^2\text{LO}}$$

^3He EDM: quantitative results for g_0 exchange



$$g_0 N^\dagger \vec{\pi} \cdot \vec{\tau} N \quad (\mathcal{CP}, I)$$

$$\theta\text{-term, qCEDM} \rightarrow \text{LO}$$

$$4\text{qLR} \rightarrow \text{N}^2\text{LO}$$

units: $g_0 (g_A m_N / F_\pi) \text{efm}$

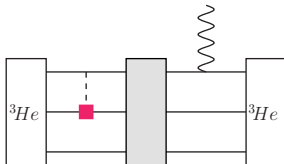
| author | potential | no int. | with int. | total |
|---------------|--------------------------------------|------------------------|------------------------|------------------------|
| JBC (2013)* | $A_{V_{18}}\text{UIX}$ | -0.45×10^{-2} | -0.13×10^{-2} | -0.57×10^{-2} |
| JBC (2013)* | CD BONN TM | -0.56×10^{-2} | -0.12×10^{-2} | -0.67×10^{-2} |
| JBC (2013)* | ChPT ($N^2\text{LO}$) [†] | -0.56×10^{-2} | -0.19×10^{-2} | -0.76×10^{-2} |
| Song (2013) | $A_{V_{18}}\text{UIX}$ | - | - | -0.59×10^{-2} |
| Stetcu (2008) | $A_{V_{18}}\text{UIX}$ | - | - | -1.21×10^{-2} |

*: in preparation †: cutoffs at 600 MeV (LS) and 700 MeV (SFR)

Results for ^3H also available (not shown)

Note: calculation finally under control !

^3He EDM: quantitative results for g_1 exchange



$$g_1 N^\dagger \pi_3 N \quad (\cancel{CP}, I)$$

$$\theta\text{-term} \quad \rightarrow \quad \text{NLO}$$

$$q\text{CEDM, } 4q\text{LR} \quad \rightarrow \quad \text{LO !}$$

units: $g_1 (g_{AMN}/F_\pi) efm$

| Ref. | potential | no int. | with int. | total |
|---------------|--------------------------------------|------------------------|------------------------|------------------------|
| JBC (2013)* | $A_{V_{18}}\text{UIX}$ | -1.09×10^{-2} | -0.02×10^{-2} | -1.11×10^{-2} |
| JBC(2013)* | CD BONN TM | -1.11×10^{-2} | -0.03×10^{-2} | -1.14×10^{-2} |
| JBC (2013)* | ChPT ($N^2\text{LO}$) [†] | -1.09×10^{-2} | -0.14×10^{-2} | -0.96×10^{-2} |
| Song (2013) | $A_{V_{18}}\text{UIX}$ | - | - | -1.08×10^{-2} |
| Stetcu (2008) | $A_{V_{18}} \text{UIX}$ | - | - | -2.20×10^{-2} |

*: in preparation †: cutoffs at 600 MeV (LS) and 700 MeV (SFR)

Results for ^3H also available (not shown)

In the pipeline: \cancel{CP} 3π -vertex contribution (4qLR: LO)

Quantitative EDM results in the θ -term scenario

Single Nucleon (with adjusted signs for consistency; note here $e < 0$):

$$\begin{aligned}
 -d_1^{\text{loop}} &\equiv \frac{1}{2}(d_n - d_p)^{\text{loop}} \\
 &= (2.1 \pm 0.9) \cdot 10^{-16} \bar{\theta} \text{ e cm} \quad (\text{Bsaisou et al. (2013)})
 \end{aligned}$$

$$d_n = +(2.9 \pm 0.9) \cdot 10^{-16} \bar{\theta} \text{ e cm} \quad (\text{Guo \& Meißner (2012)})$$

$$d_p = -(1.1 \pm 1.1) \cdot 10^{-16} \bar{\theta} \text{ e cm} \quad (\text{Guo \& Meißner (2012)})$$

Deuteron:

$$\begin{aligned}
 d_D &= d_n + d_p - [(0.59 \pm 0.39) - (0.05 \pm 0.02)] \cdot 10^{-16} \bar{\theta} \text{ e cm} \\
 &= d_n + d_p - (0.54 \pm 0.39) \cdot 10^{-16} \bar{\theta} \text{ e cm} \quad (\text{Bsaisou et al. (2013)})
 \end{aligned}$$

Helium-3:

$$\begin{aligned}
 d_{^3\text{He}} &= \tilde{d}_n + [(1.52 \pm 0.60) - (0.46 \pm 0.30)] \cdot 10^{-16} \bar{\theta} \text{ e cm} \\
 &= \tilde{d}_n + (1.06 \pm 0.67) \cdot 10^{-16} \bar{\theta} \text{ e cm} \quad (\text{JBC (2013)})
 \end{aligned}$$

$$\text{with } \tilde{d}_n = 0.88d_n - 0.047d_p \quad (\text{de Vries et al. (2011)})$$

Testing Strategies in the θ EDM scenario

Remember:

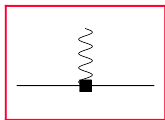
$$d_D = d_n + d_p - (0.54 \pm 0.39) \cdot 10^{-16} \bar{\theta} \text{ e cm} \quad (\text{Bsaisou et al. (2013)})$$

$$d_{^3\text{He}} = \tilde{d}_n + (1.06 \pm 0.67) \cdot 10^{-16} \bar{\theta} \text{ e cm} \quad (\text{JBC (2013)})$$

Testing strategies:

- plan A: measure d_n , d_p , and $d_D \xrightarrow{d_D(2N)} \bar{\theta} \xrightarrow{\text{test}} d_{^3\text{He}}$
- plan A': measure d_n , (d_p), and $d_{^3\text{He}} \xrightarrow{d_{^3\text{He}}(2N)} \bar{\theta} \xrightarrow{\text{test}} d_D$
- plan B: measure d_n (or d_p) + Lattice QCD $\rightsquigarrow \bar{\theta} \xrightarrow{\text{test}} d_D$
- plan B': measure d_n (or d_p) + Lattice QCD $\rightsquigarrow \bar{\theta} \xrightarrow{\text{test}} d_p$ (or d_n)

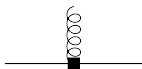
If $\bar{\theta}$ -term tests fail: use effective BSM dim. 6 sources de Vries et al. (2011)



$qEDM$

$$d_D \approx d_p + d_n$$

$$d_{^3He} \approx d_n$$



$qCEDM$

$$d_D > d_p + d_n$$

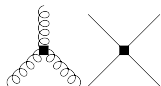
$$d_{^3He} > d_n$$



$4qLR$

$$d_D > d_p + d_n$$

$$d_{^3He} > d_n$$



$gCEDM + 4qEDM$

$$d_D \sim d_p + d_n$$

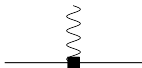
$$d_{^3He} \sim d_n$$

→ $g_0, g_1 \propto \alpha/(4\pi)$

2N contribution suppressed by photon loop!

here: only absolute values considered

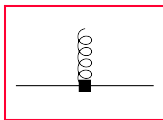
If $\bar{\theta}$ -term tests fail: use effective BSM dim. 6 sources de Vries et al. (2011)



$qEDM$

$$d_D \approx d_p + d_n$$

$$d_{3He} \approx d_n$$



$qCEDM$

$$d_D > d_p + d_n$$

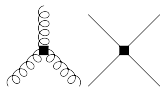
$$d_{3He} > d_n$$



$4qLR$

$$d_D > d_p + d_n$$

$$d_{3He} > d_n$$



$gCEDM + 4qEDM$

$$d_D \sim d_p + d_n$$

$$d_{3He} \sim d_n$$

→ g_0, g_1

$2N$ contribution enhanced!

here: only absolute values considered

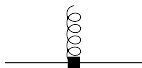
If $\bar{\theta}$ -term tests fail: use effective BSM dim. 6 sources de Vries et al. (2011)



$qEDM$

$$d_D \approx d_p + d_n$$

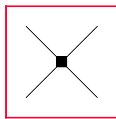
$$d_{3He} \approx d_n$$



$qCEDM$

$$d_D > d_p + d_n$$

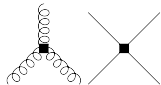
$$d_{3He} > d_n$$



$4qLR$

$$d_D > d_p + d_n$$

$$d_{3He} > d_n$$



$gCEDM + 4qEDM$

$$d_D \sim d_p + d_n$$

$$d_{3He} \sim d_n$$

→ $g_1 \gg g_0$; 3π -coupling (unsuppressed)

$2N$ contribution enhanced!

here: only absolute values considered

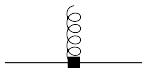
If $\bar{\theta}$ -term tests fail: use effective BSM dim. 6 sources de Vries et al. (2011)



$qEDM$

$$d_D \approx d_p + d_n$$

$$d_{3He} \approx d_n$$



$qCEDM$

$$d_D > d_p + d_n$$

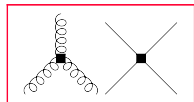
$$d_{3He} > d_n$$



$4qLR$

$$d_D > d_p + d_n$$

$$d_{3He} > d_n$$



$gCEDM + 4qEDM$

$$d_D \sim d_p + d_n$$

$$d_{3He} \sim d_n$$

→ $g_1, g_0, 4N$ – coupling

$2N$ contribution difficult to assess!

here: only absolute values considered

Summary and Outlook

- θ EDM: relevant low-energy couplings **quantifiable**

strategy A: measure $d_n, d_p, d_D \xrightarrow{d_D(2N)} \bar{\theta} \xrightarrow{\text{test}} d_{3He}$

strategy A': measure $d_n, (d_p), d_{3He} \xrightarrow{d_{3He}(2N)} \bar{\theta} \xrightarrow{\text{test}} d_D$

strategy B: measure d_n (or d_p) + Lattice QCD $\rightsquigarrow \bar{\theta} \xrightarrow{\text{test}} d_D$

strategy B': measure d_n (or d_p) + Lattice QCD $\rightsquigarrow \bar{\theta} \xrightarrow{\text{test}} d_p$ (or d_n)

- qEDM, qCEDM, 4QLR:

- **NDA required** to assess sizes of low-energy couplings
- disentanglement possible by measurements of d_n, d_p, d_D & d_{3He}

- gCEDM, 4quark chiral singlet:

controlled calculation/disentanglement difficult (lattice ?)

- Ultimate progress may eventually come from Lattice QCD

↪ the $\overline{CP} NN\pi$ couplings may be accessible even for dim-6 sources

↪ then **quantifiable** d_D (d_{3He}) EFT predictions feasible in BSM case

Conclusions

- (Hadronic) EDMs play a key role in probing new sources of CP
- Measurements of hadronic EDMs are **low-energy measurements**
 - ↳ Predictions have to be given in the *empirical language of hadrons*
 - ↳ only reliable methods predicting *uncertainties* as well:
ChPT/EFT and/(or ultimately) *Lattice QCD*
- EDMs of light nuclei provide **independent information** to nucleon EDMs and may be even larger and even simpler
- Deuteron and helium-3 nuclei serve as isospin filters for EDMs

At least the EDMs of p , n , d , and ${}^3\text{He}$
have to be measured
to disentangle the underlying physics
by applying methods of EFT and lattice QCD

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