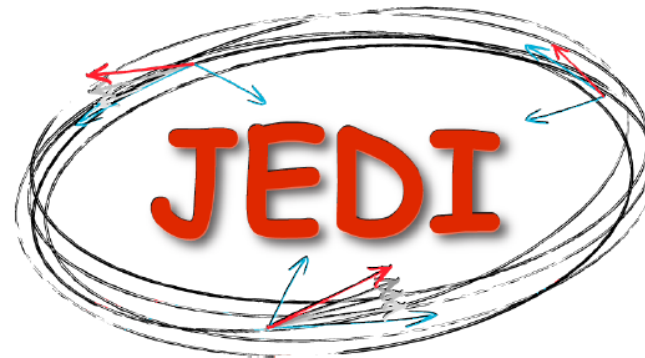


# Status of a Design Study for a Proton EDM Ring

Martin Gaißer on behalf of the

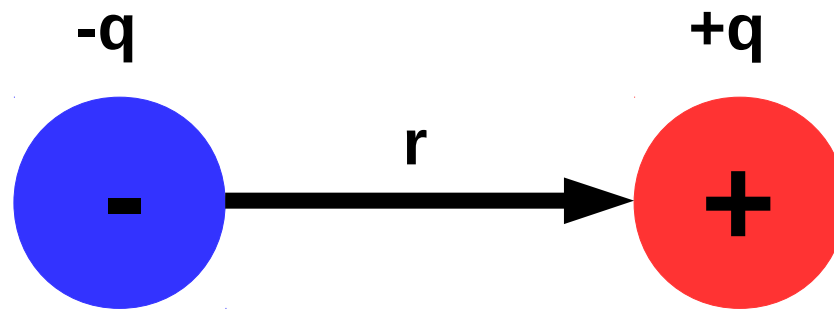


collaboration



**European Research Council**

Established by the European Commission



$$\vec{d} = q\vec{r}$$

- **Permanent** electric dipole moments of elementary particles **along spin direction** violate parity (P) and time reversal (T) symmetry
- Via CPT theorem: EDMs are source of CP violation

In rest frame: 
$$\frac{d\vec{S}}{d\tau} = \vec{\mu} \times \vec{B}^* + \vec{d} \times \vec{E}^*$$

Transform fields into rest frame. use equation of motion

→ get T-BMT Equation,  $G = \frac{g-2}{2}$ ,  $\eta \approx 10^{-15}$  for  $|\vec{d}| = 10^{-29} e \cdot \text{cm}$

$$\frac{d\vec{S}}{dt} = \vec{S} \times (\vec{\Omega}_{MDM} + \vec{\Omega}_{EDM})$$

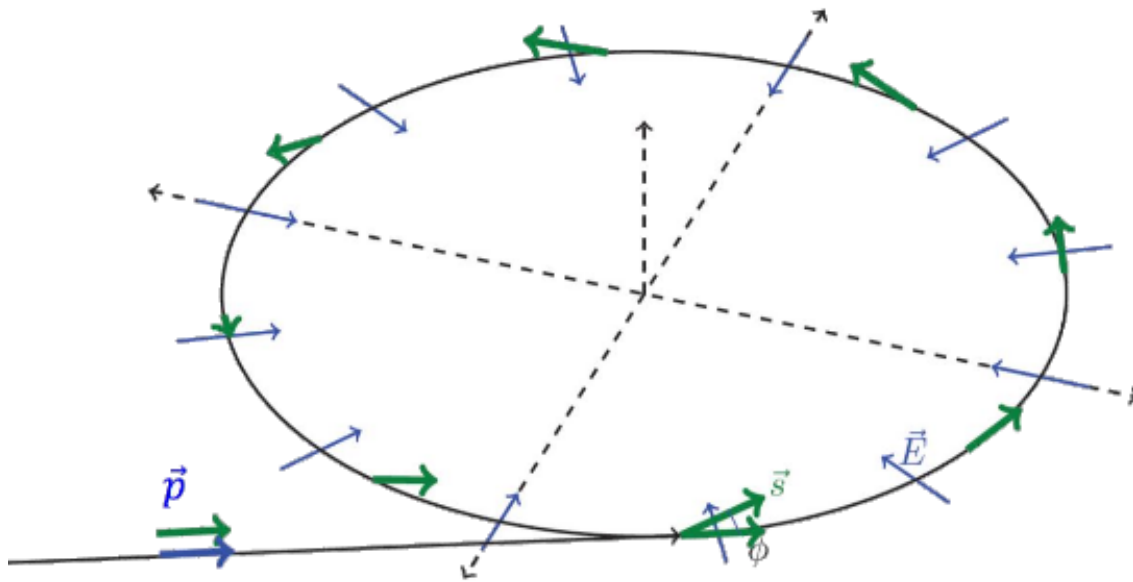
$$\vec{\Omega}_{MDM} = \frac{q}{m} \left( G\vec{B} - \frac{\gamma G}{\gamma+1} \vec{\beta}(\vec{\beta} \cdot \vec{B}) - \left( G - \frac{1}{\gamma^2-1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right)$$

$$\vec{\Omega}_{EDM} = \frac{\eta q}{2mc} \left( \vec{E} - \frac{\gamma}{\gamma+1} \vec{\beta}(\vec{\beta} \cdot \vec{E}) + c\vec{\beta} \times \vec{B} \right)$$

$|\Omega_{EDM}| \ll |\Omega_{MDM}| \Rightarrow$  want  $\Omega_{MDM} = 0$

- Possible for  $\vec{B} = 0$ ,  $p = \frac{mc}{\sqrt{G}} \approx 0.7 \text{ GeV}/c$  (for protons)

- Have  $\Omega_{EDM} \propto E \rightarrow$  **want strong electric field!**



- Inject longitudinal polarized beam
- Run in frozen spin mode
- Observe build-up of vertical polarization

$$(|\vec{E}| = 10 \text{ MV/m}, \eta = 10^{-15})$$

**Expected build-up rate** for protons (all electric ring):

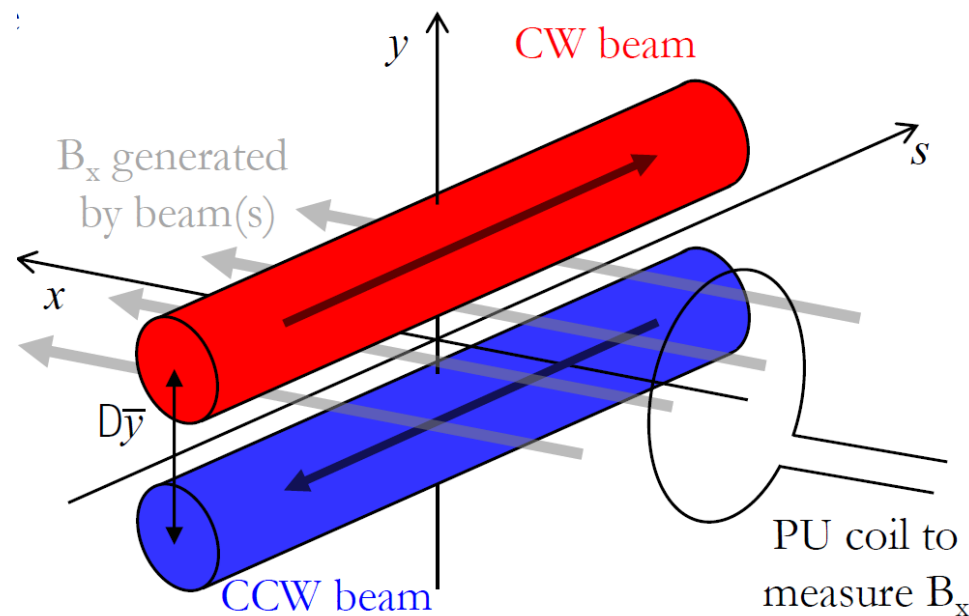
$$|\vec{\Omega}_{EDM}| \approx 1.6 \cdot 10^{-9} \text{ rad/s}$$

→ **requires long (polarization) lifetime, at least 1000s**

**Bending radius** (beam):  $R \approx 42 \text{ m}$

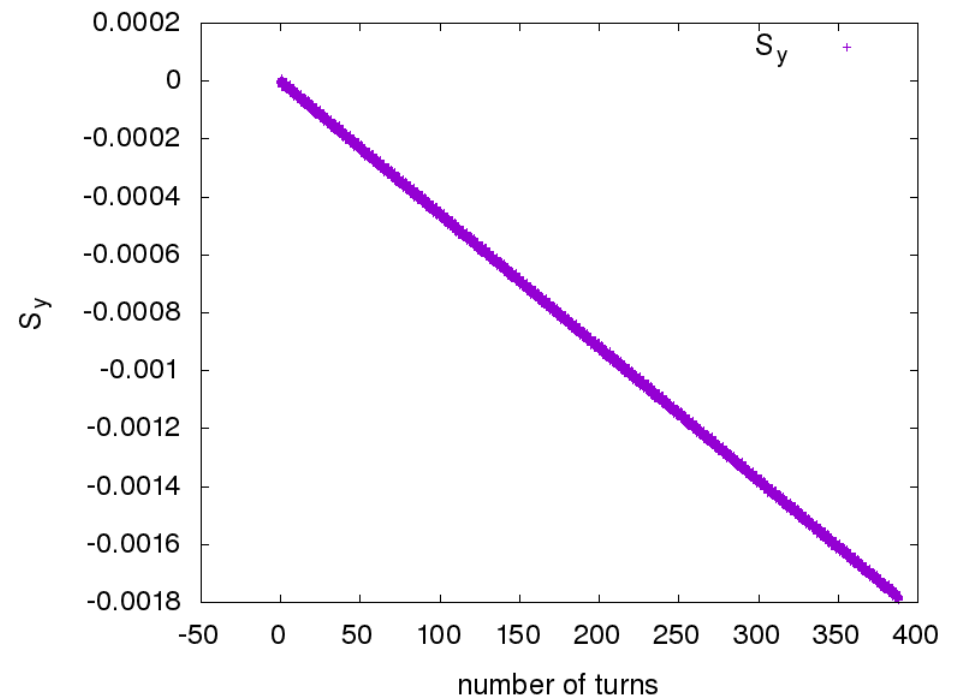
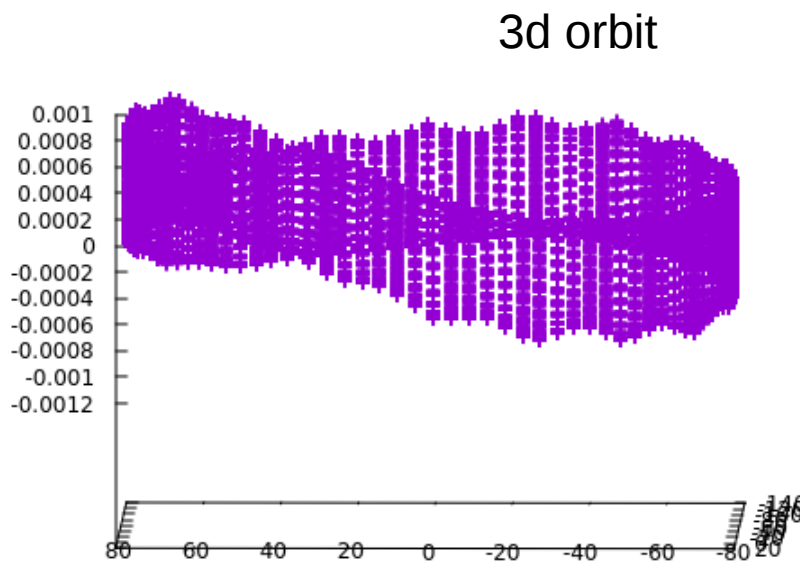
# Systematic Error: Radial B-field

- Main systematic error: radial magnetic field (few aT)
- Strategy: Shield as good as possible, use CW/CCW beams
- Radial B-field separates beams vertically
- Separation can be measured with squids
- Requires: **equal beams, low vertical tune, symmetric lattice**
- Radial B-field from off-center passage through rf-cavity can be distinguished from EDM effect with CW/CCW beams



# Systematic Error: Quadrupole Offsets

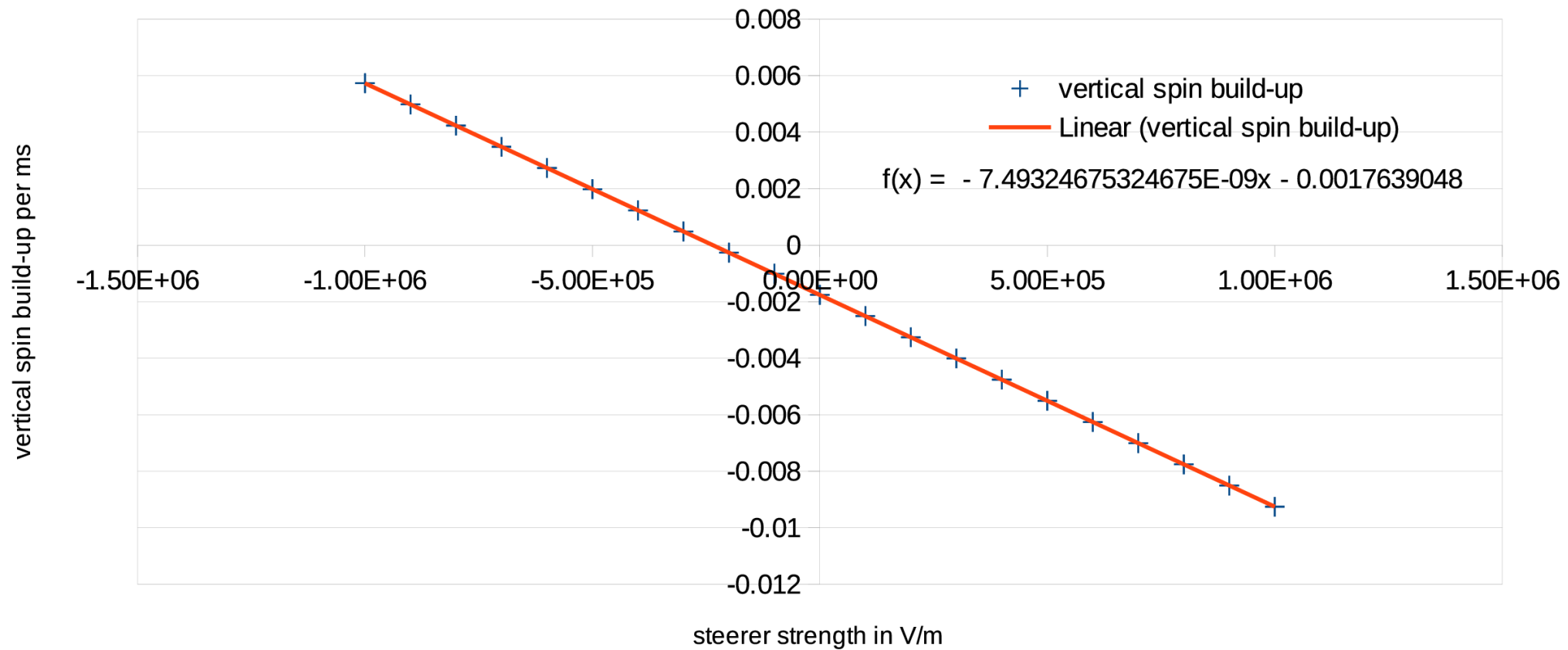
- Other source of vertical spin build-up: Vertical quadrupole offset
- Distorts orbit in 3d → average vertical velocity nonzero in deflectors
- Only seen with radial spin component → use also transversely polarized bunches, effect cancels with CW/CCW operation



All quads randomly offset by 0.1 mm, simulated for 1 ms, start on design orbit

# Correct for Quadrupole Offsets: Use Steerer

## Solution: Add vertical steerer to lattice (length 0.5m)

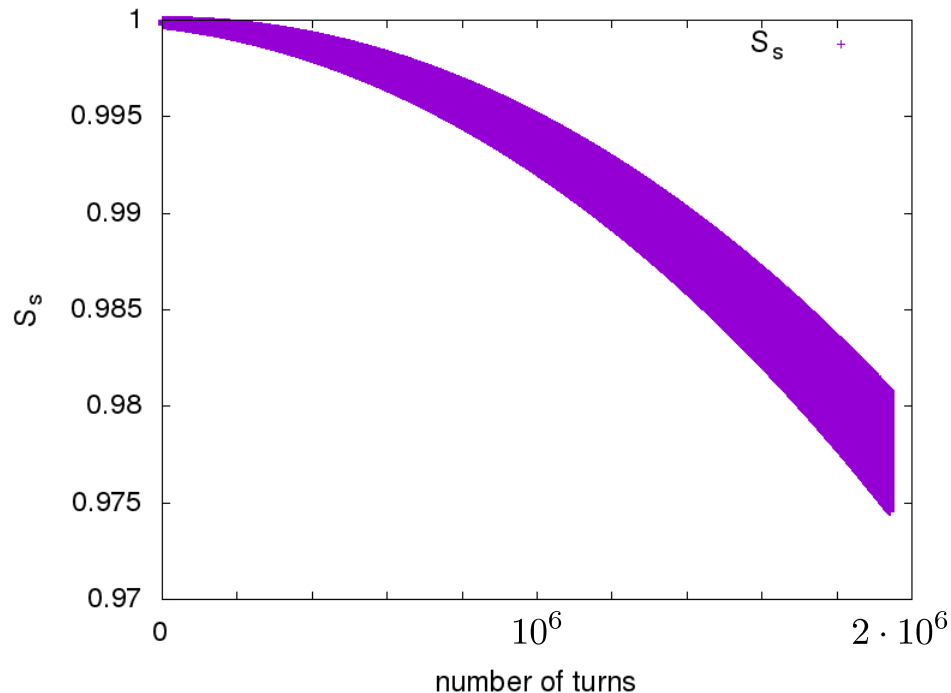


## Perfect ring:

- Design particle has frozen spin
- Particle at magic momentum started from position off axis will oscillate
- If it oscillates around design orbit the orbit becomes longer → need higher energy to keep revolution frequency → off magic momentum → spin rotates
- Other option: oscillate about a different equilibrium orbit (negative average x-position) → off magic momentum inside field regions → spin rotates
- **Betatron oscillations limit spin coherence time (SCT)**



Simulate particle at magic momentum with initial x- and y-offset in straight section of 10mm for  $T = 5\text{s}$ :



Estimate precession rate:

$$\cos(\omega_y T) \approx 0.978$$

$$\Rightarrow \omega_y = \frac{\arccos(0.978)}{5 \text{ s}} = 0.042 \text{ 1/s}$$

How long does it take for a  $90^\circ$  rotation?

$$\cos(\omega_y t) = 0$$

$$\Rightarrow t = \frac{\arccos(0)}{\omega_y} = 37.4 \text{ s}$$

- Very rough estimate for SCT: 10s-100s (depends on phase space distributions)
- **need to make it longer by factor 10**

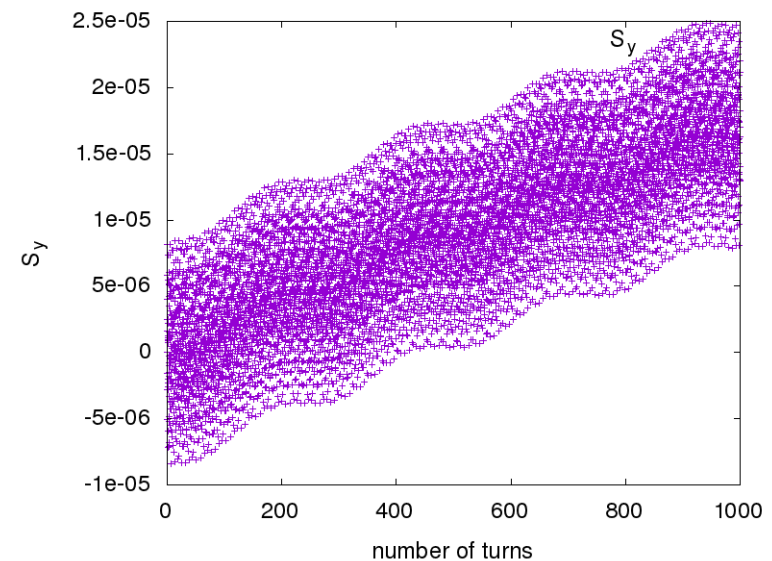
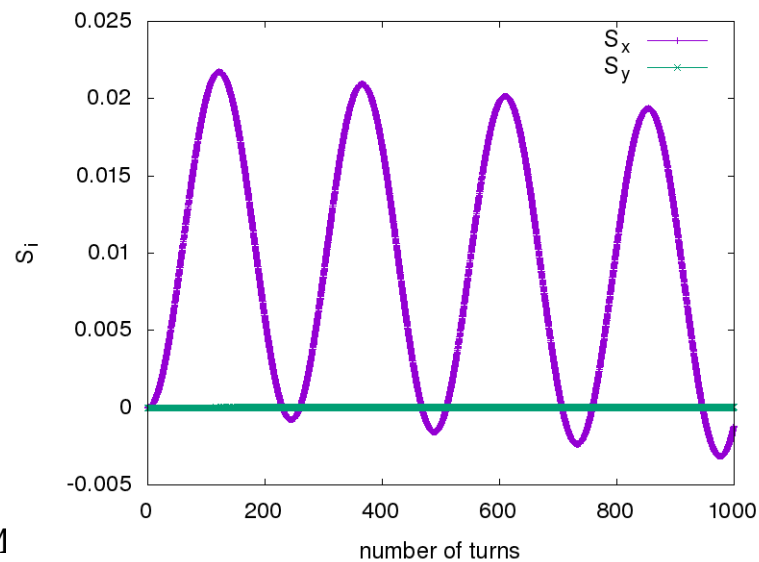
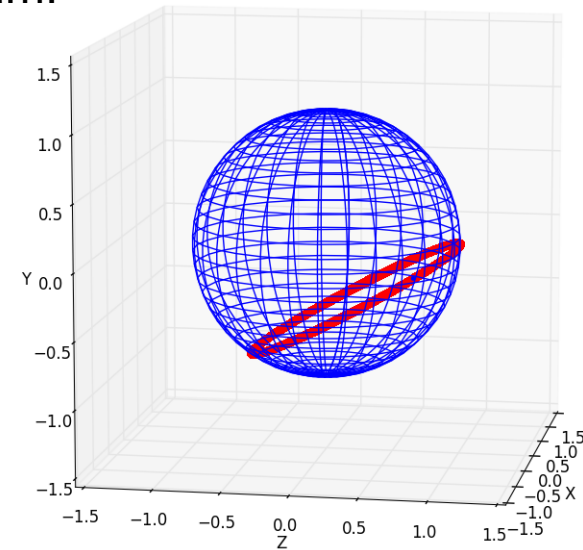
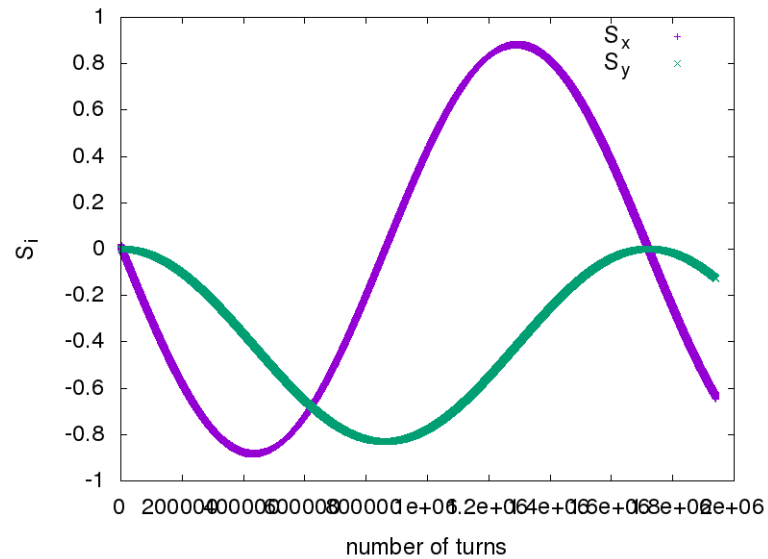
- Very interesting but challenging experiment for CERN/Physics Beyond Colliders Program
- Dominated by systematics
- Need high accuracy and proper beam instrumentation
- Need high quality simulations
- Have lots of experience in Jülich with deuteron EDM experiment (compare with talks of V. Schmidt, T. Wagner, K. Grigoriev)
- Looks prudent to build prototype (check lifetime, test components, etc.)

**Simulate exactly the same situation as before but with some changes to the ring:**

- Randomly misplace all quadrupoles, horizontally and vertically with one sigma offset =  $10\mu\text{m}$
- Randomly rotate all quads and bends with one sigma rotation of  $10\mu\text{rad}$
- Randomly change field strength of all elements with one sigma relative field change of  $1e-5$

# Influence of Imperfections

Particle started on the design orbit with magic momentum:



Particle started on the design orbit with magic momentum:

- Get extremely large vertical precession rate (compared to expected nrad/s EDM signal)!  
→ **need feedback system**
- May not look that bad in shorter (1ms) simulations!  
→ **requires (numerically) stable long term tracking**
- Cavity needs to be adjusted to freeze horizontal spin → happens only after 1-2 seconds of data taking  
→ **need very high temporal stability of accelerator!**
- **CW/CCW beams will cancel error to large degree**

