

# Investigation of the Spin Coherence Time for measuring the Electric Dipole Moment of protons in the COSY COoler SYnchrotron

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# MOTIVATION

## Matter-antimatter asymmetry

- Predominance of matter over antimatter in the Universe
- Sakharov conditions (1967):
  1. Baryon number violation
  2. Non thermal equilibrium
  3. Violation of  $\mathcal{C}$  and  $\mathcal{CP}$  symmetry

- Baryon-to-photon ratio:  $\frac{n_B - n_{\bar{B}}}{n_\gamma}$

Baryon-to-photon ratio	
Observation	$\approx 6 \times 10^{-10}$
Theory (SMC)	$\leq 10^{-18}$

# MOTIVATION

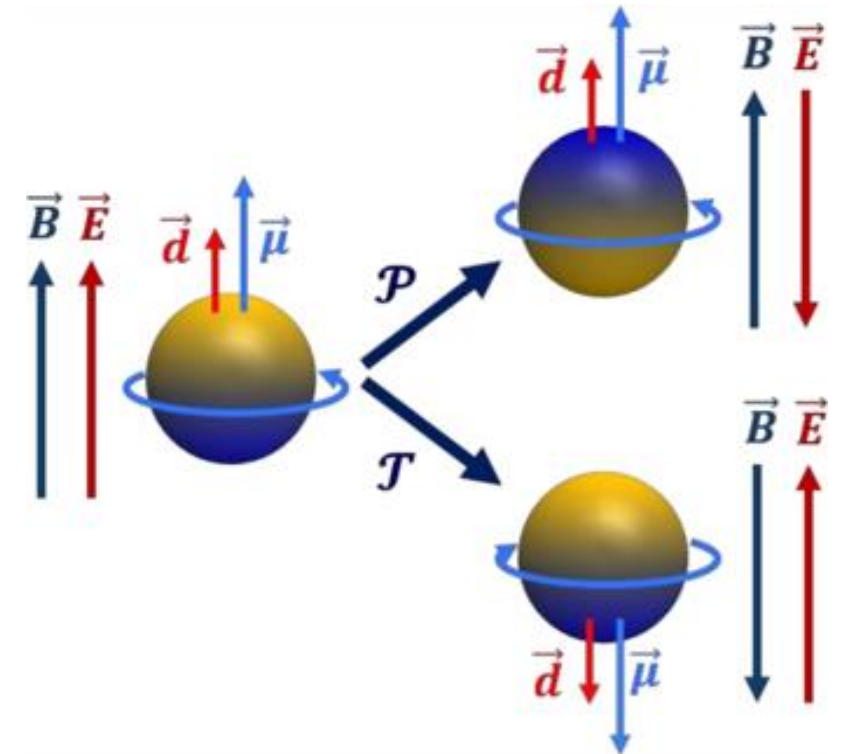
## ELECTRIC DIPOLE MOMENT (EDM)

- EDM: Permanent separation of positive and negative charge
- non-zero EDM violates both parity  $\mathcal{P}$  and time reversal  $\mathcal{T}$  symmetry ( $CP$  violation)

$$\mathcal{H} = -\vec{\mu} \cdot \vec{B} - \vec{d} \cdot \vec{E}$$

$$\mathcal{P} : \mathcal{H} = -\vec{\mu} \cdot \vec{B} + \vec{d} \cdot \vec{E}$$

$$\mathcal{T} : \mathcal{H} = -\vec{\mu} \cdot \vec{B} + \vec{d} \cdot \vec{E}$$



- Storage ring EDM experiments
- Longitudinally polarized beam:  $\vec{S} \parallel \vec{p}$
- Interaction of a particles' spin with electromagnetic fields
- non-zero EDM results in a vertical polarization build up

- Thomas-BMT Equation:  
(pure magnetic field)

$$\frac{d\vec{S}}{dt} = \vec{\Omega} \times \vec{S}$$

$$\Omega = \frac{q}{m} \left[ G\vec{B} + \underbrace{\frac{\eta}{2}\vec{\beta} \times \vec{B}}_{\text{EDM}} \right]$$

$\Omega$ : angular precession frequency

G: anomalous magnetic moment

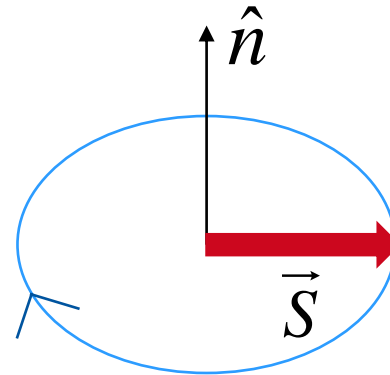
# SPIN COHERENCE TIME (SCT)

- Spin tune  $\nu_s = G\gamma$  :  
number of spin precessions per turn

Critical parameter:

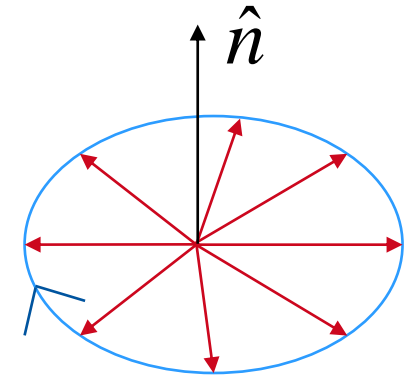
- Spin Coherence Time (SCT):  
time after which polarization drops to 1/e of  
initial value.
- SCT > 1000 s  
(Achieved at COSY for deuterons, 2016)

Horizontally polarized



At injection

unpolarized



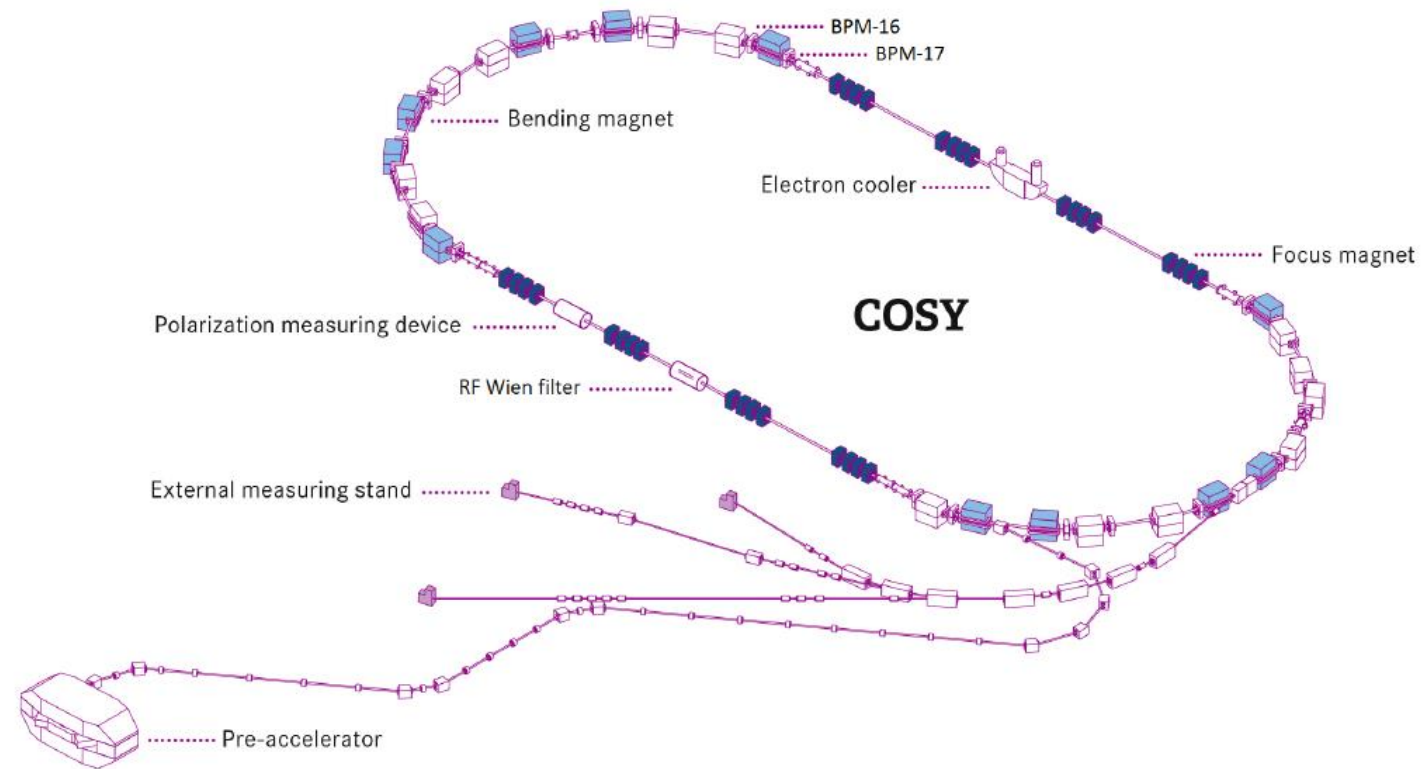
After some time

- Spin tune spread  $\Delta\nu_s = G\Delta\gamma$
- First order effect: momentum spread  $\frac{\Delta p}{p_0}$ .
- Second order effects: path length change & intrinsic resonances.
- The path length change due to:
  1. betatron motion:  $\left(\frac{\Delta L}{L}\right)_\beta = \frac{2\pi}{L} (\varepsilon_x \xi_x + \varepsilon_y \xi_y)$
  2. momentum deviation:  $\left(\frac{\Delta L}{L}\right)_\alpha = \alpha_0 \left(\frac{\Delta p}{p_0}\right) + \alpha_1 \left(\frac{\Delta p}{p_0}\right)^2 + \dots$
- Path length changes  $\Delta L \rightarrow 0$ .
- Two optimization approaches.

# COSY COoler SYnchrotron

- Circumference: 184 m
- Polarized protons and deuterons
- Current experiment uses protons :  
 $p = 531 \text{ MeV}/c$
- Electron cooling system:
  1. Reducing momentum spread
  2. Reducing emittance

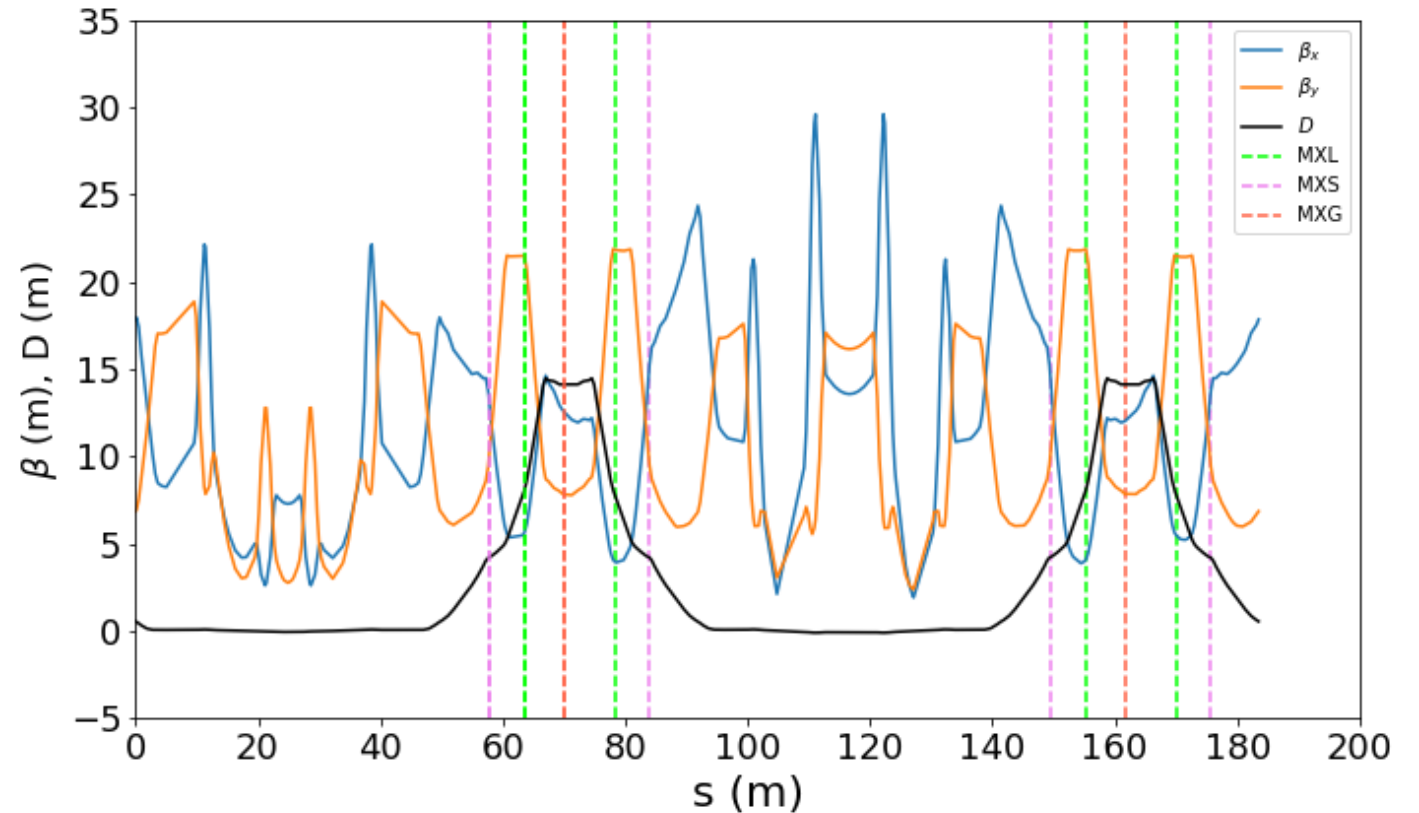
Improve SCT !





# COSY LATTICE

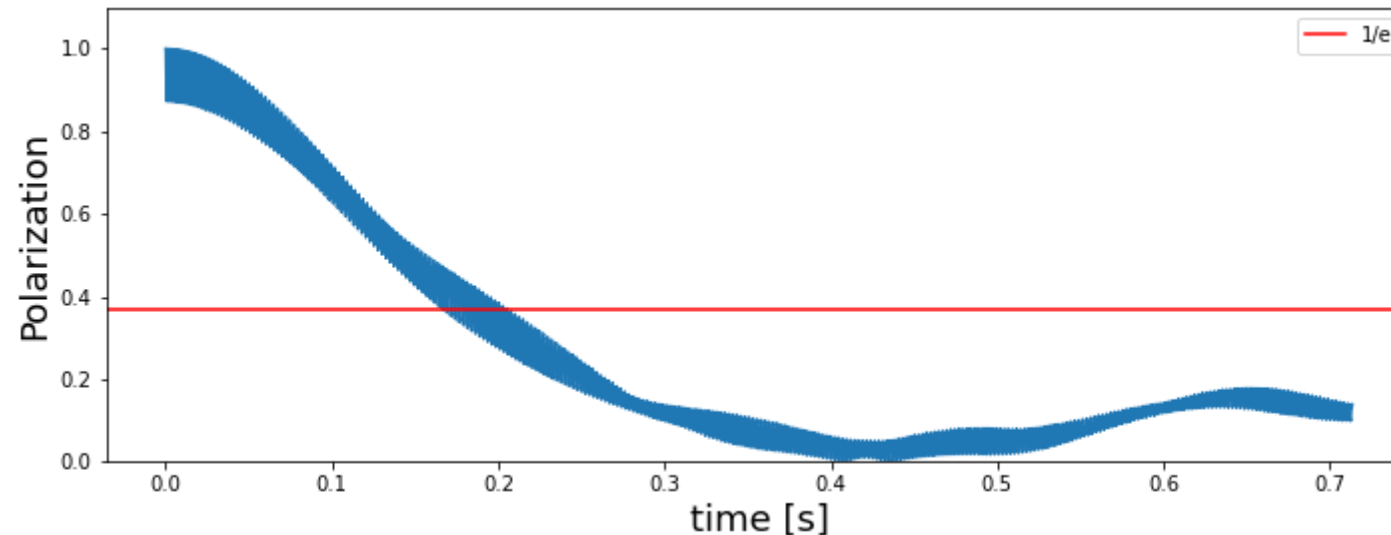
- Software library BMAD
- Idealized COSY lattice
- $Q_x = 3.63, Q_y = 3.72$
- Three groups of sextupole:
  1. MXS: large  $\beta_x$
  2. MXL: large  $\beta_y$
  3. MXG: large dispersion D



# ZERO CHROMATICITIES

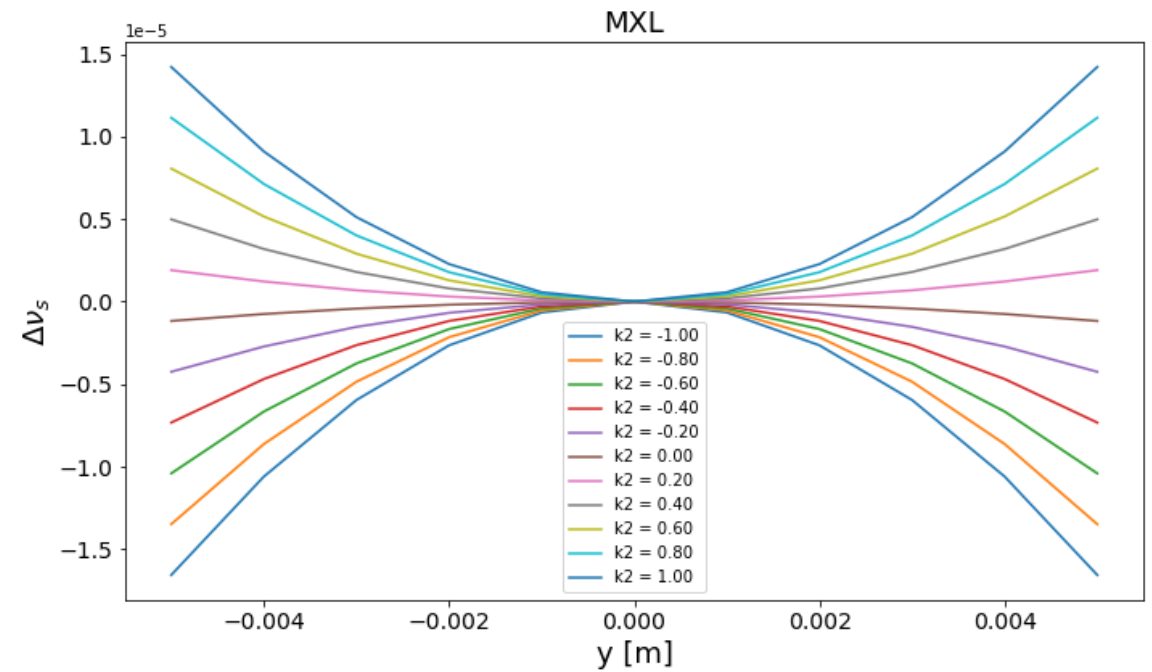
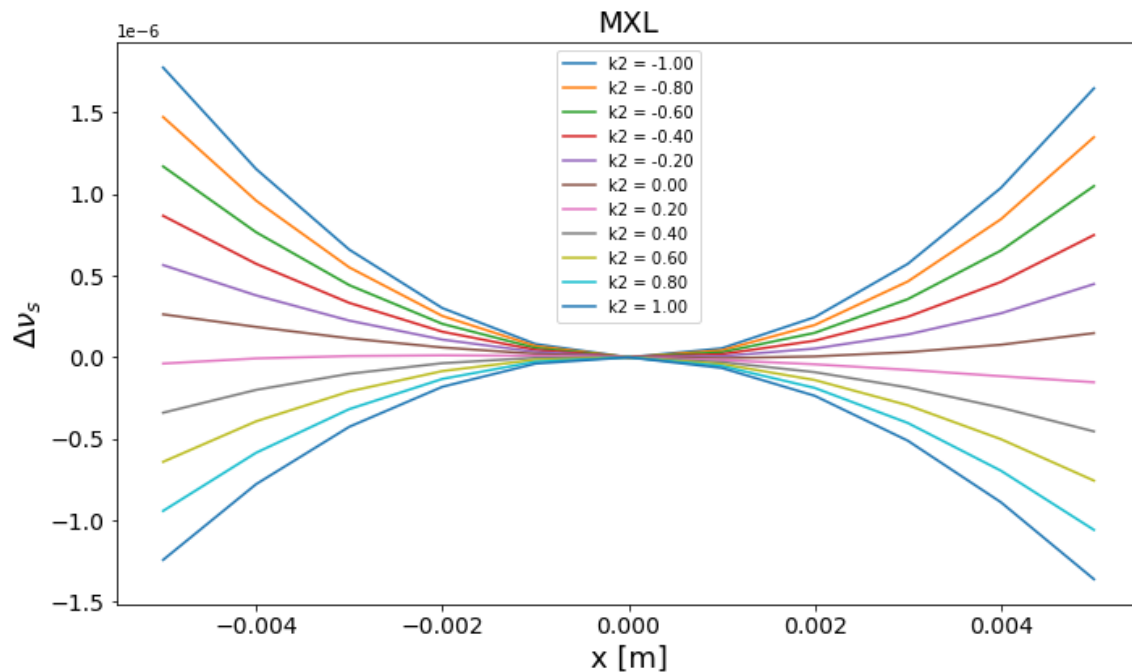
$$(\xi_x, \xi_y) = (0, 0)$$

- 3 dimensional BMAD scanning routine : MXL x MXG x MXS
- Rough scan with 121 x 101 x 101 grid:  
(0,0) points are at nearly fixed MXL:  $k_2 \approx -0.5 \text{ m}^{-3}$
- Finer scan with 121 x 101 x 401 grid.
- SCT = 0.185 s



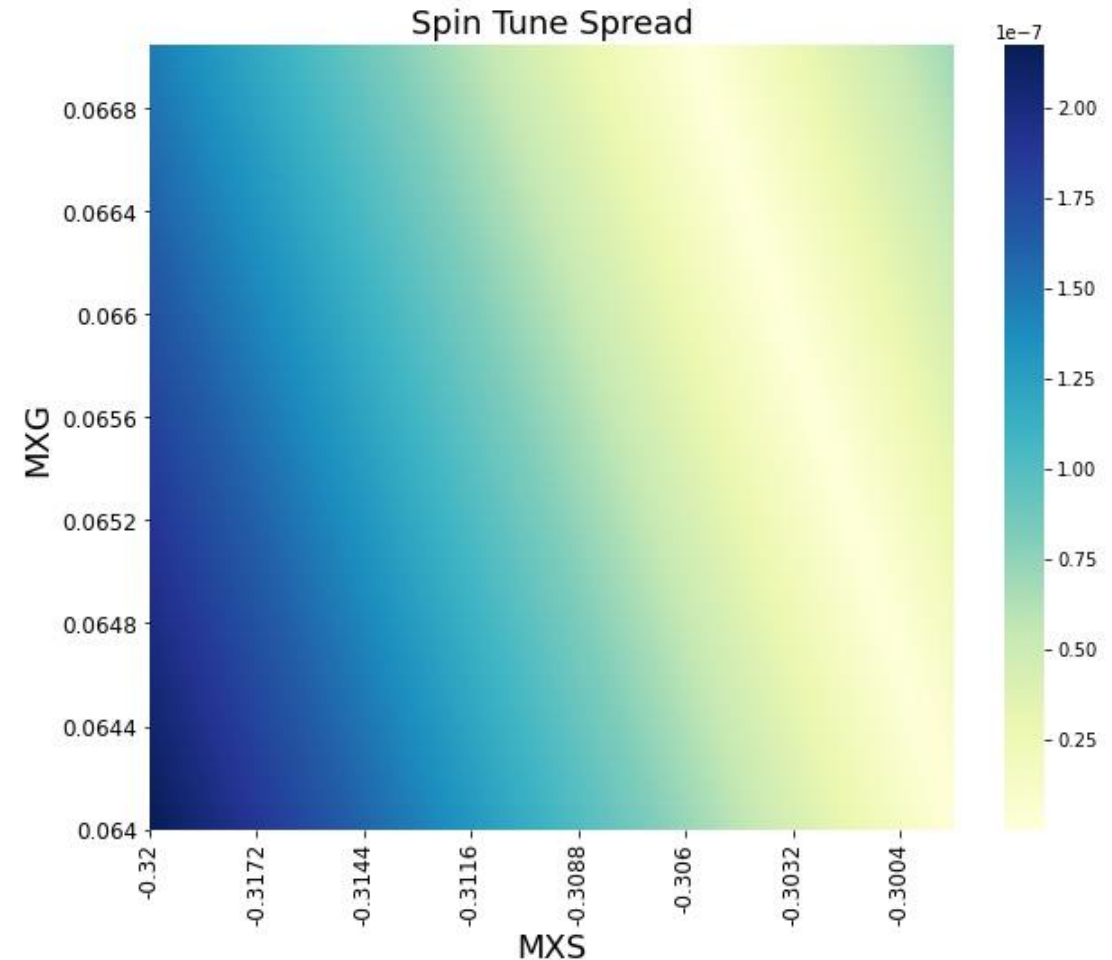
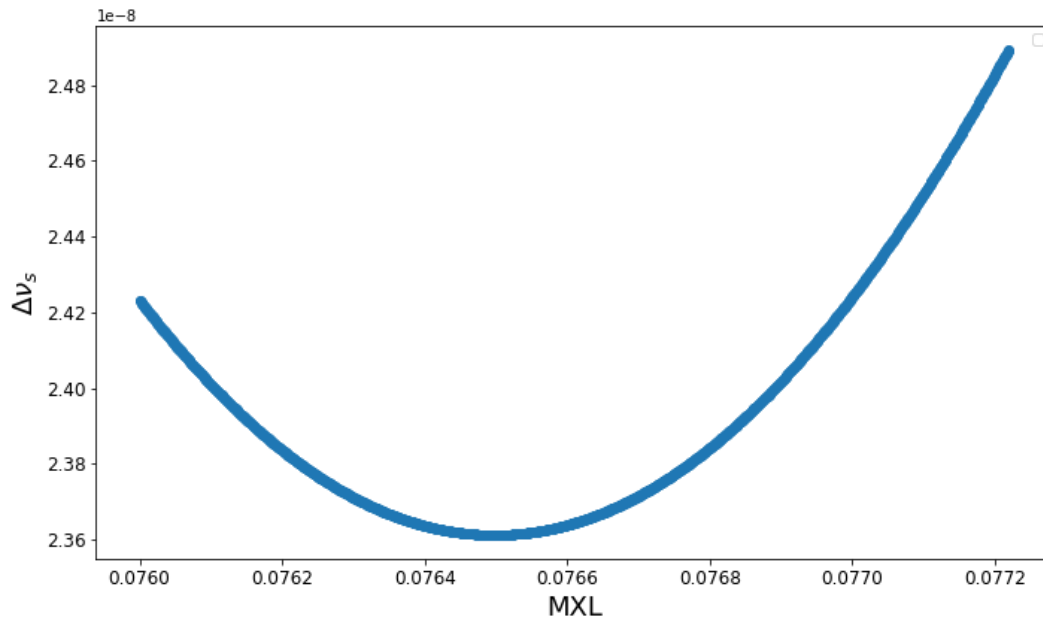
# OPTIMIZATION METHOD

- Spin-tune shift for horizontal or vertical offset particles at different sextupole settings.
- The minimum  $\Delta\nu_s$  can be obtained by flattening these parabolas.
- Spin tune spread  $\Delta\nu_s$  in MXL-y plane is 1 order of magnitude larger than others.



# OPTIMIZATION PROCEDURE

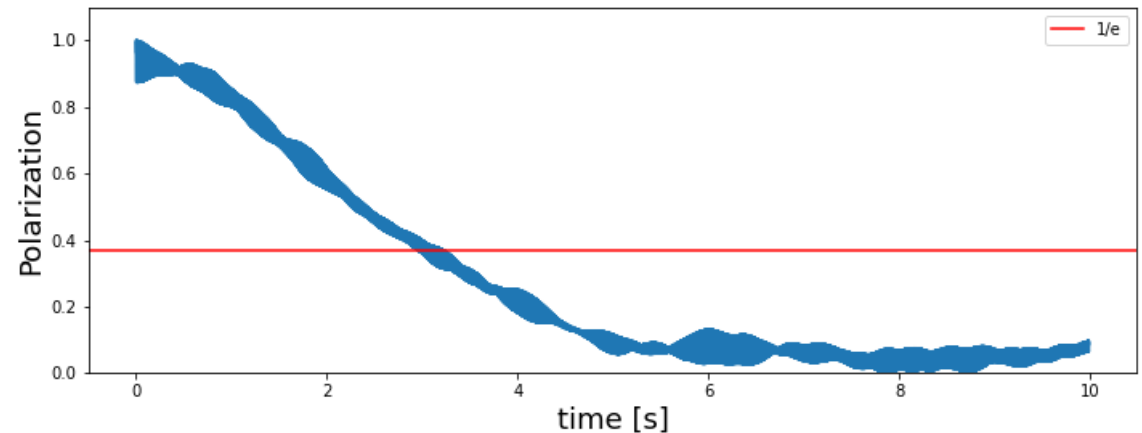
- BMAD scanning routine + spin tracking
- 1D:        MXL + MXS + MXG
- 1D + 2D: MXL + MXS x MXG
- Find the minimum  $\Delta\nu_s$  point



# OPTIMIZATION RESULTS

- $\Delta\nu_s$  are reduced by 3 orders of magnitude: ( $10^{-5} \sim 10^{-6}$  to  $10^{-8} \sim 10^{-9}$ )
- After optimization with horizontal and vertical planes, the SCT reaches 3 s.
- Optimal chromaticities are all negative and far from zero.
- The smaller the  $\alpha_1$  the longer the SCT.

	$\alpha_1$	$\xi_x$	$\xi_y$	SCT(s)
$(\xi_x, \xi_y) = (0, 0)$	-6.284	+0.0002	-0.0002	0.185
BMAD-1D (x, y)	0.051	-3.9770	-4.9849	3.388
BMAD-2D (x, y)	0.294	-3.9596	-4.9446	3.094
COSY infinity (x, y, E)	0.035	-3.6920	-5.3711	7.899

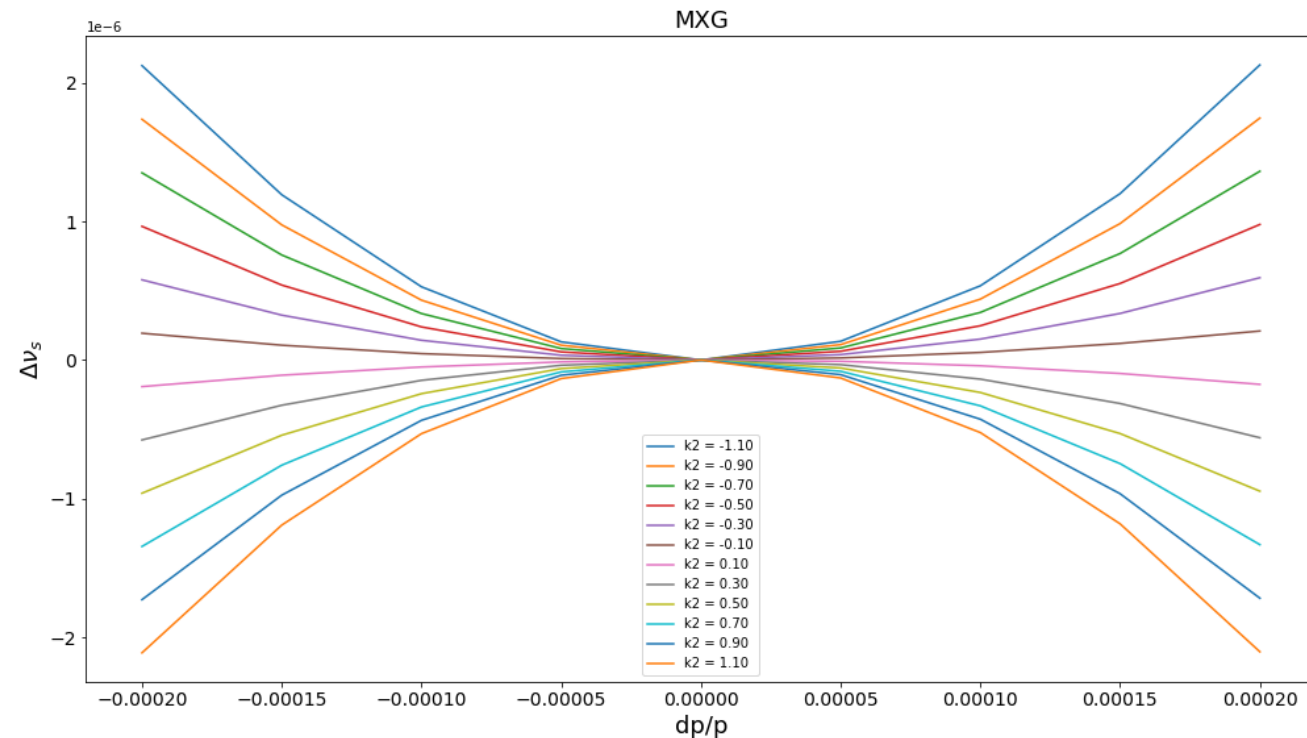


# SUMMARY

- Storage ring EDM experiment requires the SCT  $> 1000$  s.
- Path length change leads to spin tune decoherence.
- The new optimization method significantly improves SCT of protons.

# OUTLOOK

- Implement the momentum deviation to BMAD optimization.
- Investigate the impact of intrinsic resonances for protons.



**Thank You!**