

# BEAM BASED ALIGNMENT

## Beam Based Alignment tests at COSY

March 19, 2018 | Tim Wagner, on behalf of the JEDI Collaboration |



# COSY

## Cooler Synchrotron

- Circumference: 184 m
- Provides polarized protons and deuterons
- Maximum momentum: 3.65 GeV/c
- Intensity:  $10^9$  to  $10^{10}$  particles
- Electron cooling
- Spin manipulators



Forschungszentrum Jülich

# COSY

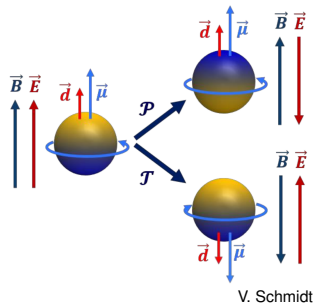
## Cooler Synchrotron



# ELECTRIC DIPOLE MOMENT (EDM)

- Permanent EDMs of light hadrons are  $\mathcal{T}$ - and  $\mathcal{P}$ -violating
- $\mathcal{CPT}$  theorem  $\rightarrow \mathcal{CP}$  violation
- Measure EDMs of charged particles in storage rings
- $d_{\text{Neutron}} < 3 \times 10^{-26} \text{ e} \cdot \text{cm}$
- $d_{\text{Proton}} < 5 \times 10^{-24} \text{ e} \cdot \text{cm}$
- $d_{\text{Deuteron}} = ?$

$$\vec{d} = \eta \cdot \frac{q}{2mc} \vec{S}$$



$$\mathcal{H} = -\vec{\mu} \cdot \vec{B} - \vec{d} \cdot \vec{E}$$

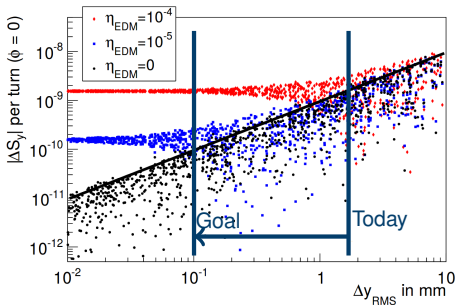
$$\mathcal{P} : \mathcal{H} = -\vec{\mu} \cdot \vec{B} + \vec{d} \cdot \vec{E}$$

$$\mathcal{T} : \mathcal{H} = -\vec{\mu} \cdot \vec{B} + \vec{d} \cdot \vec{E}$$

# BEAM BASED ALIGNMENT

## Why is it needed?

- For an EDM measurement the orbit has to be as good as possible
- Orbit RMS should be lower than  $100\text{ }\mu\text{m}$   
→ Orbit Control
- Orbit Control corrects the beam to the BPM zero position
- Goal is to go central through all magnets (i.e. quadrupoles)
- Thus BPM to quadrupole offset has to be known  
→ Beam Based Alignment

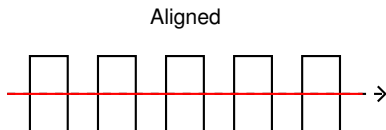


M. Rosenthal, PhD Thesis (modified)

# BEAM BASED ALIGNMENT

## How does it work?

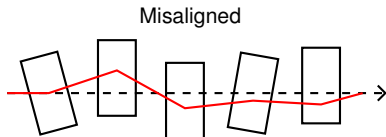
- Use beam to optimize the beam position
- Vary quadrupole strength
- Observe orbit change
- Try to minimize the orbit change



# BEAM BASED ALIGNMENT

## How does it work?

- Use beam to optimize the beam position
- Vary quadrupole strength
- Observe orbit change
- Try to minimize the orbit change



# BEAM BASED ALIGNMENT

## How does it work?

- How does the orbit change when varying the quadrupole strength?

$$\Delta x(s) = \left( \frac{\Delta k x(\bar{s}) l}{B\rho} \right) \left( \frac{1}{1 - k \frac{l\beta(\bar{s})}{2B\rho \tan \pi\nu}} \right) \\ \times \frac{\sqrt{\beta(s)}\sqrt{\beta(\bar{s})}}{2 \sin \pi\nu} \cos(\phi(s) - \phi(\bar{s}) - \pi\nu)$$

- Not possible to calculate  $x(\bar{s})$  due to lack of precise knowledge of all other parameters



# BEAM BASED ALIGNMENT

How does it work?

- Use the following merit function

$$f = \frac{1}{N_{\text{BPM}}} \sum_{i=1}^{N_{\text{BPM}}} (x_i(+\Delta k) - x_i(-\Delta k))^2$$
$$f \propto (\Delta x)^2 \propto (x(\bar{s}))^2$$

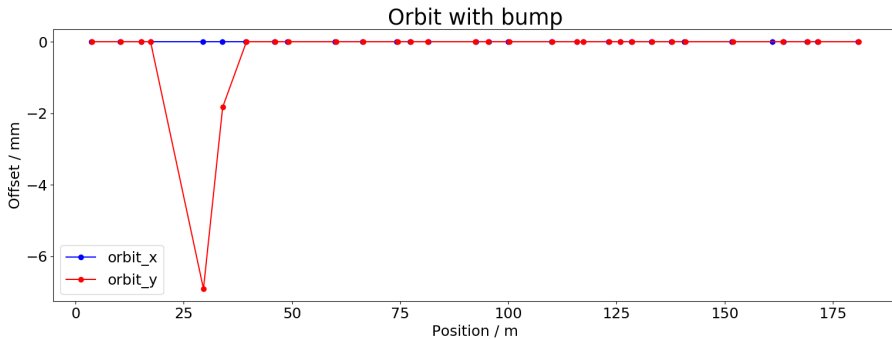
- By finding the minimum the optimal beam position can be found

# SIMULATION

- Simulation of COSY done with MAD-X
- Option 1: Generate a bump inside the quadrupole
- Option 2: Move the quadrupole
- Vary the quadrupole strength
- Observe the effect on the orbit
- Calculate the optimal position

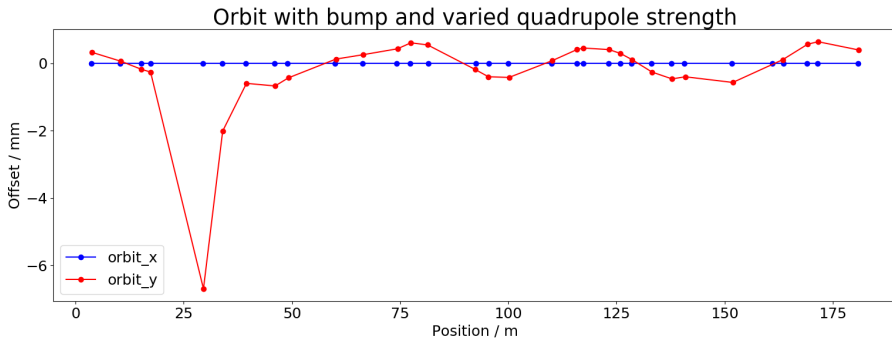
# SIMULATION

## Example Bump



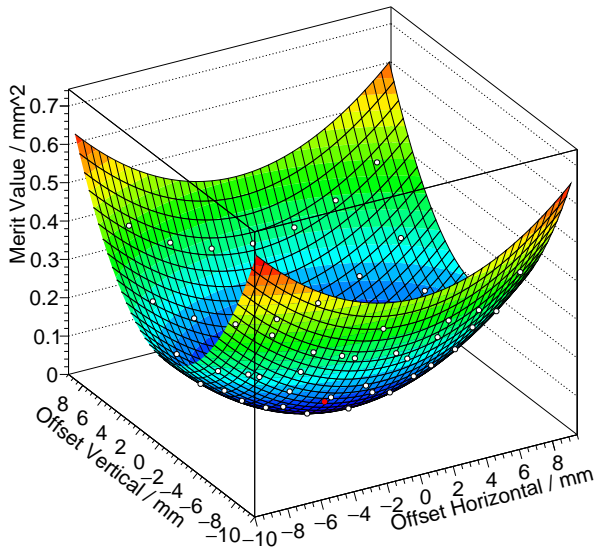
# SIMULATION

## Example Bump



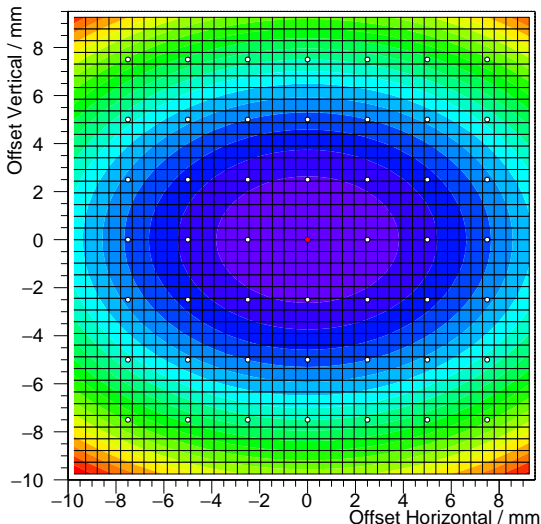
# SIMULATION

## Option 1 - Apply Bump



# SIMULATION

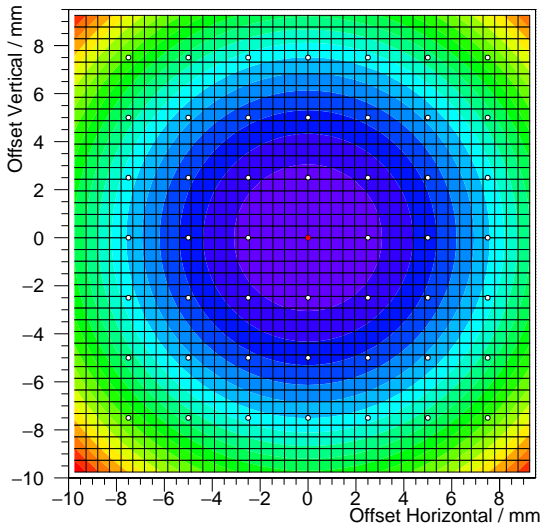
## Option 1 - Apply Bump



- Asymmetric due to imperfect bumps
- Different slopes of the beam for horizontal and vertical direction

# SIMULATION

## Option 2 - Move Quadrupole



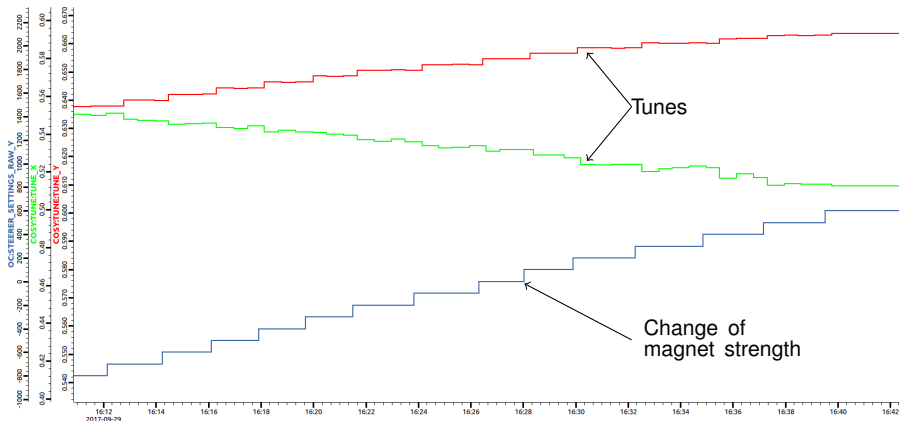
# MEASUREMENT

- Quadrupoles are powered in families of four
- On the poles of quadrupole QT12 the additional coils of the steerer BLW04 were recabled to work as a quadrupole



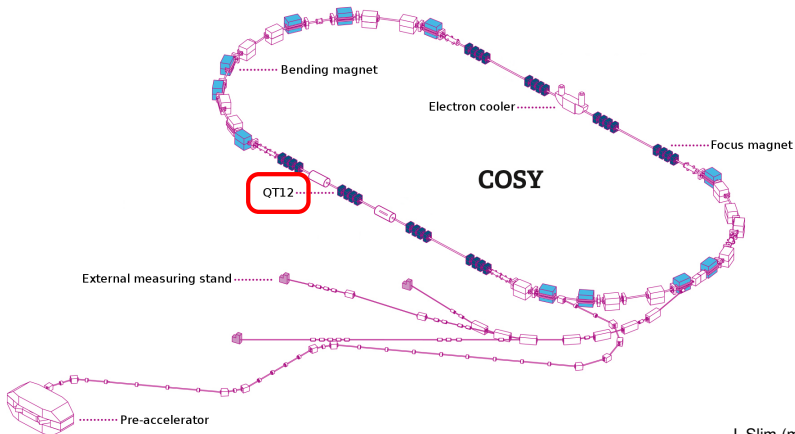
# MEASUREMENT

## Quadrupole behavior



# MEASUREMENT

## Location of QT12



J. Slim (modified)

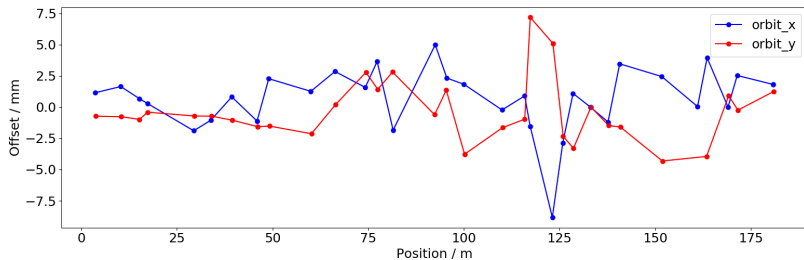
COSY scetch with position of quadrupole QT12 indicated

# MEASUREMENT

- Quadrupoles are powered in families of four
- On the poles of quadrupole QT12 the additional coils of the steerer BLW04 were recabled to work as a quadrupole
- Effectively the strength of quadrupole QT12 can be varied
- Local bumps applied at the position of the quadrupole
- Measured effect on orbit upon varying the quadrupole strength

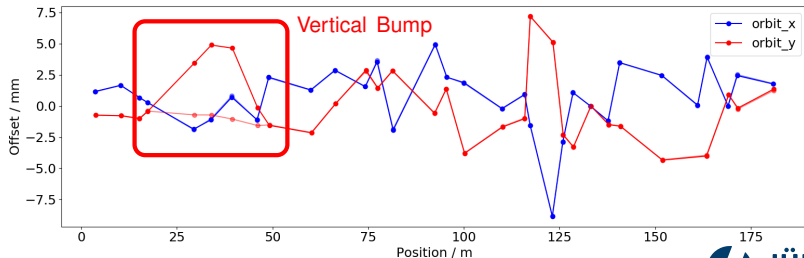
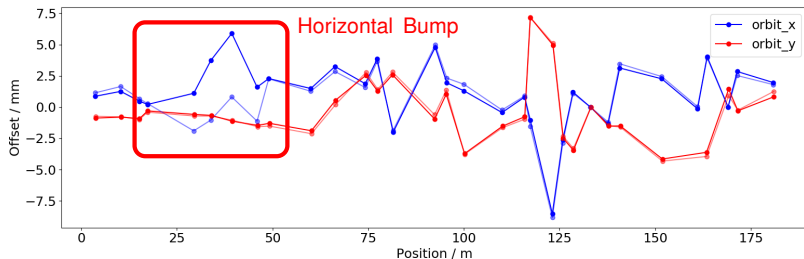
# MEASUREMENT

## Orbit

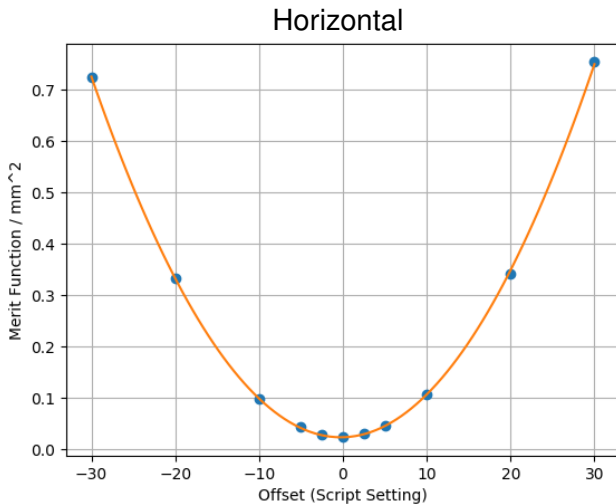


# MEASUREMENT

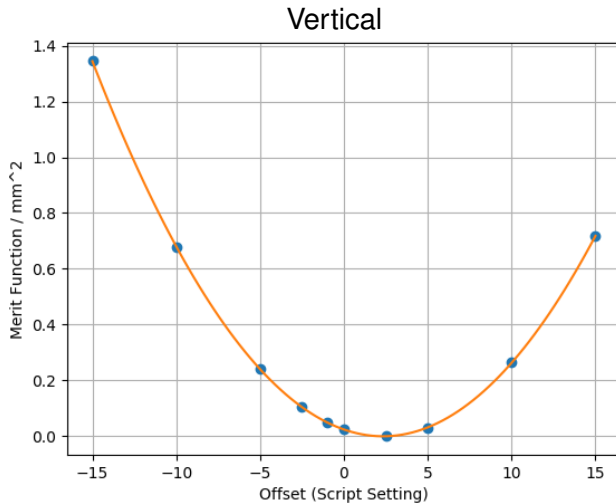
## Orbit



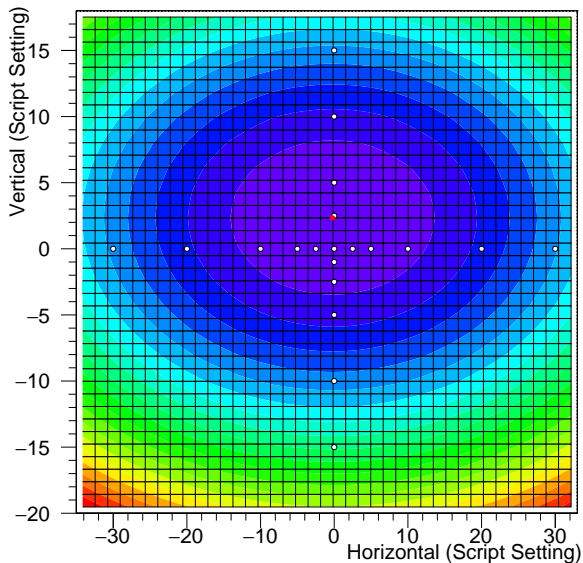
# RESULTS



# RESULTS



# RESULTS





# RESULTS

	Optimal Position	in mm
Horizontal	$-0.255 \pm 0.028$	$-1.98 \pm 0.01$
Vertical	$2.329 \pm 0.011$	$1.15 \pm 0.01$

- Optimal position given in script setting
- The values in mm are the BPM 6 readings nearby

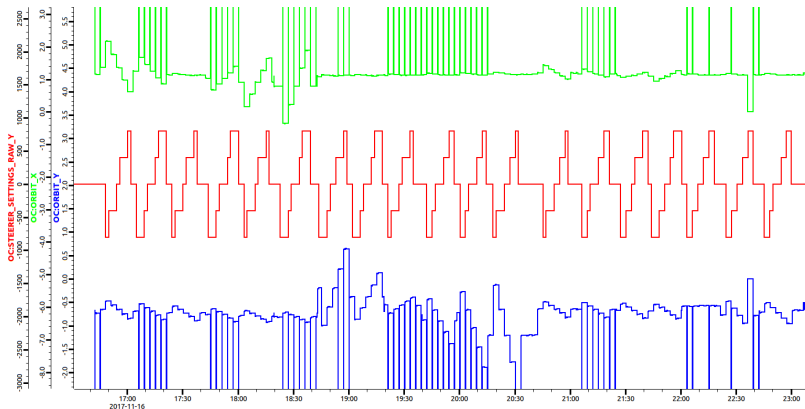
# SUMMARY & OUTLOOK

- Beam based alignment works
- The change of the magnet strength with additional coils works
- Optimal beam position inside the quadrupole could be determined to be  $(-1.98 \pm 0.01)$  mm horizontally and  $(1.15 \pm 0.01)$  mm vertically
- Additional quadrupole magnets need to be changed to be individually controlled
- Measurement all along the ring to obtain quadrupole to BPM offsets

# Backup

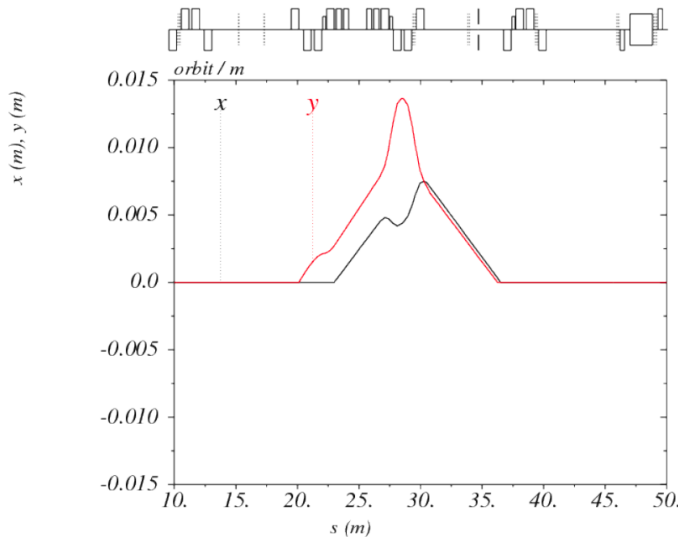


# MEASUREMENT SCREENSHOT

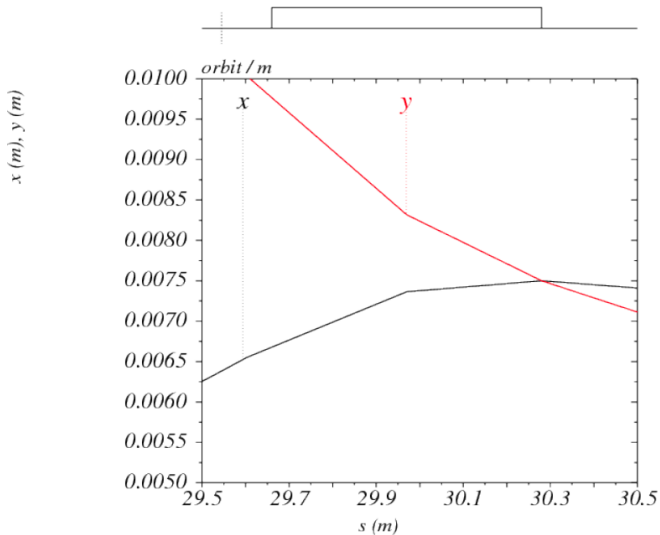


Screenshot of the measurement. In red the change of the magnet strength is shown and in green and blue an example for a bpm reading. For each scan a different beam position was used.

# SIMULATION: BUMP



# SIMULATION: BUMP



# BEAM BASED ALIGNMENT

## Derivation of formula for orbit change

$$\Delta x(s) = \left( \frac{\Delta k \cdot x(\bar{s}) l}{B\rho} \right) \left( \frac{1}{1 - k \frac{l \beta(\bar{s})}{2 B\rho \tan \pi \nu}} \right) \frac{\sqrt{\beta(s)} \sqrt{\beta(\bar{s})}}{2 \sin \pi \nu} \cos(\phi(s) - \phi(\bar{s}) - \pi \nu)$$

- $\Delta x$  = orbit change
- $s$  = measurement position
- $\bar{s}$  = position of quadrupole
- $\Delta k$  = change of quadrupole strength
- $x(\bar{s})$  = position of beam inside the quadrupole
- $\beta$  = beta function
- $\nu$  = tune
- $\phi$  = betatron phase
- $k$  = quadrupole strength
- $l$  = length of quadrupole
- $B\rho$  = magnetic rigidity of the beam

# BEAM BASED ALIGNMENT

## Derivation of formula for orbit change

- Start with effect of a dipole kick  $\theta$  on the orbit.

$$\Delta x(s) = \theta \times \frac{\sqrt{\beta(s)}\sqrt{\beta(\bar{s})}}{2 \sin \pi \nu} \cos(\phi(s) - \phi(\bar{s}) - \pi \nu)$$

$$\theta = \frac{\Delta B l}{B \rho}$$

- To first order a beam offset inside a quadrupole sees a change in quadrupole strength as a dipole kick.
- The change of the tune, beta function and betatron phase are effects of second order and can be neglected.



# BEAM BASED ALIGNMENT

## Derivation of formula for orbit change

- Quadrupole magnetic field is  $B = kx$ , thus

$$\Delta B = (k + \Delta k)(x + \Delta x) - kx = \Delta kx + \Delta xk + \mathcal{O}(\Delta k \Delta x)$$

- Combine the equations with  $\bar{s} = s$  to get

$$\Delta x = \frac{(\Delta kx + \Delta xk)l}{B\rho} \frac{\beta}{2 \sin \pi\nu} \cos \pi\nu$$

- and solve for  $\Delta x$ .

$$\Delta x = \Delta kx \frac{\frac{\beta l}{2B\rho \tan \pi\nu}}{1 - \frac{\beta l}{2B\rho \tan \pi\nu}}$$

# BEAM BASED ALIGNMENT

## Derivation of formula for orbit change

- With that calculate  $\Delta B$

$$\Delta B = \Delta k x \frac{1}{1 - k \frac{\beta l}{2 B \rho \tan \pi \nu}}$$

- and insert that into the equation for  $\theta$  and  $\Delta x(s)$ .

$$\Delta x(s) = \left( \frac{\Delta k \cdot x(\bar{s}) l}{B \rho} \right) \left( \frac{1}{1 - k \frac{l \beta(\bar{s})}{2 B \rho \tan \pi \nu}} \right) \frac{\sqrt{\beta(s)} \sqrt{\beta(\bar{s})}}{2 \sin \pi \nu} \cos(\phi(s) - \phi(\bar{s}) - \pi \nu)$$