

5/7th Bethe Center Workshop “**Challenges in Strong Interaction Physics**”
Physikzentrum Bad Honnef, September 29 – October 2, 2015

Electric Dipole Moments of Light Ions

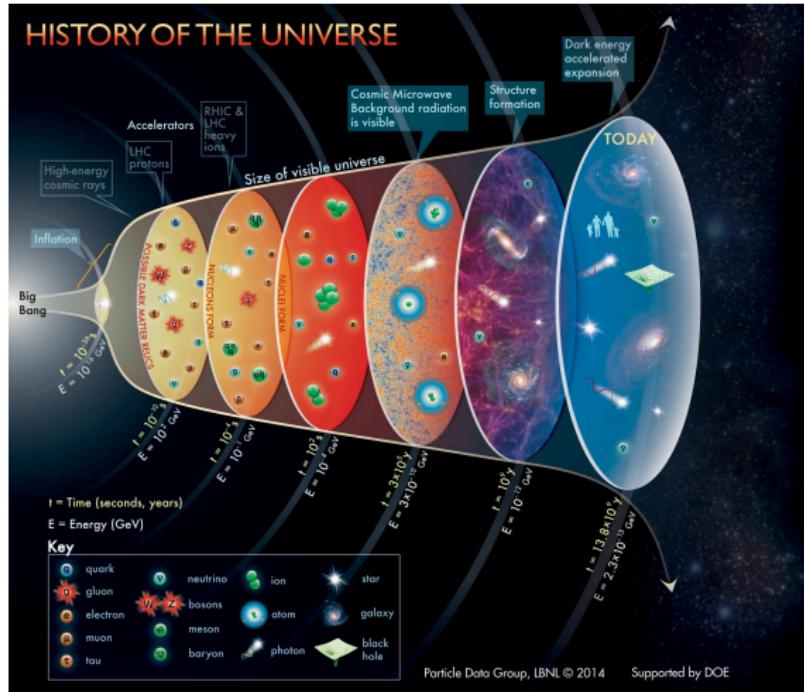
Andreas Wirzba (IAS-4 / IKP-3, Forschungszentrum Jülich)

in collaboration with

Jan Bsaisou, Christoph Hanhart, Ulf-G. Meißner, Andreas Nogga, Jordy de Vries,
Susanna Liebig, David Minossi, Werner Bernreuther and Wouter Dekens

Bad Honnef | October 2, 2015

Matter Excess in the Universe



(*) $2J_{\text{Jarlskog}}^{\text{CKM}} (m_t^2 - m_u^2)(m_t^2 - m_c^2)(m_c^2 - m_u^2)(m_b^2 - m_d^2)(m_b^2 - m_s^2)(m_s^2 - m_d^2)/M_{\text{EW}}^{12} \sim 10^{-18}$

CP violation and the Electric Dipole Moment (EDM)

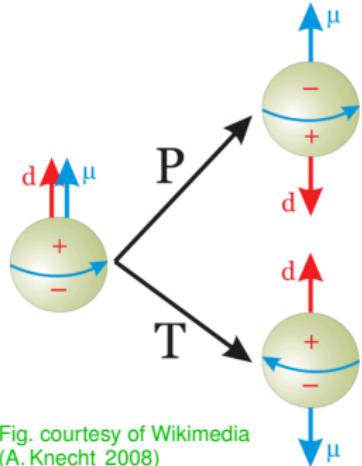


Fig. courtesy of Wikimedia
 (A. Knecht 2008)

$$\text{EDM: } \vec{d} = \sum_i \vec{r}_i e_i \xrightarrow[\text{(polar)}]{\substack{\text{subatomic} \\ \text{particles}}} d \cdot \vec{S}/|\vec{S}| \xrightarrow[\text{(axial)}]{}$$

$$\mathcal{H} = -\mu \frac{\vec{S}}{S} \cdot \vec{B} - d \frac{\vec{S}}{S} \cdot \vec{E}$$

$$P: \quad \mathcal{H} = -\mu \frac{\vec{S}}{S} \cdot \vec{B} + d \frac{\vec{S}}{S} \cdot \vec{E}$$

$$T: \quad \mathcal{H} = -\mu \frac{\vec{S}}{S} \cdot \vec{B} + d \frac{\vec{S}}{S} \cdot \vec{E}$$

Any *non-vanishing EDM* of a non-deg.
 (subatomic) particle violates **P & T**

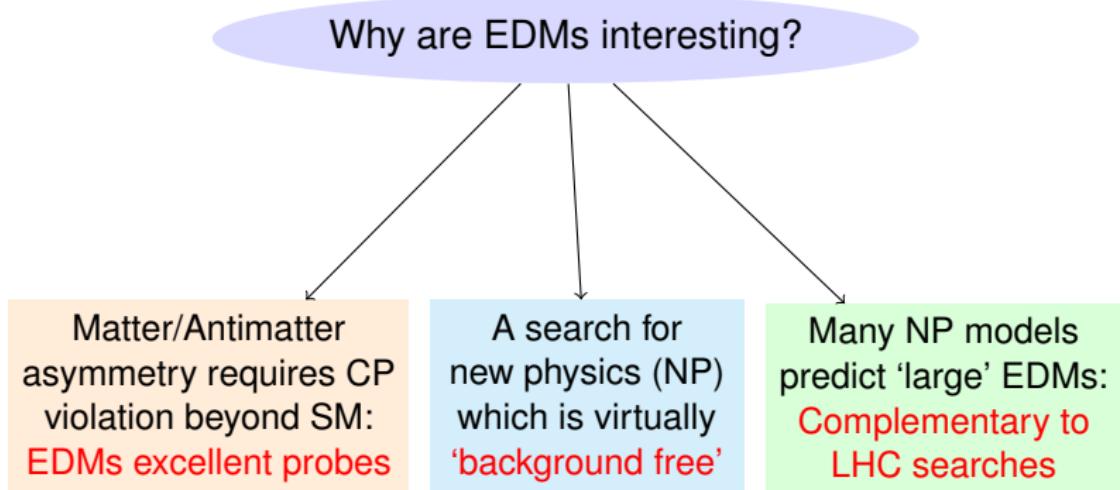
- Assuming **CPT** to hold, **CP** is violated as well (flavor-diagonally)
 ↳ subatomic EDMs: “rear window” to CP violation in early universe
- Strongly suppressed in SM (CKM-matrix): $|d_n| \sim 10^{-31} \text{ ecm}$, $|d_e| \sim 10^{-38} \text{ ecm}$
- Current bounds: $|d_n| < 3 \cdot 10^{-26} \text{ ecm}$, $|d_p| < 8 \cdot 10^{-25} \text{ ecm}$, $|d_e| < 1 \cdot 10^{-28} \text{ ecm}$

n: Baker et al. (2006), *p* prediction: Dimitriev & Sen'kov (2003)*, *e:* Baron et al. (2013)†

* from $|d_{^{199}\text{Hg}}| < 3.1 \cdot 10^{-29} \text{ ecm}$ bound of Griffith et al. (2009)

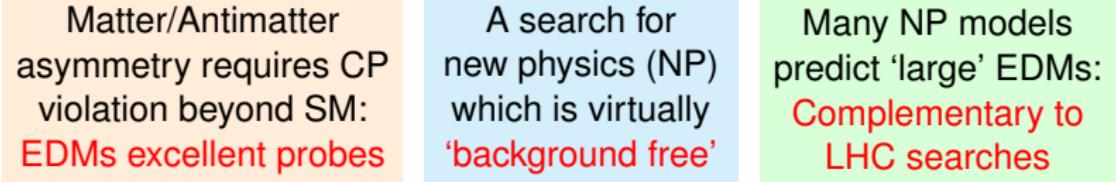
† from polar ThO: $|d_{\text{ThO}}| \lesssim 10^{-21} \text{ ecm}$

Three motivations for EDM searches



Three motivations for EDM searches

Why are EDMs interesting?

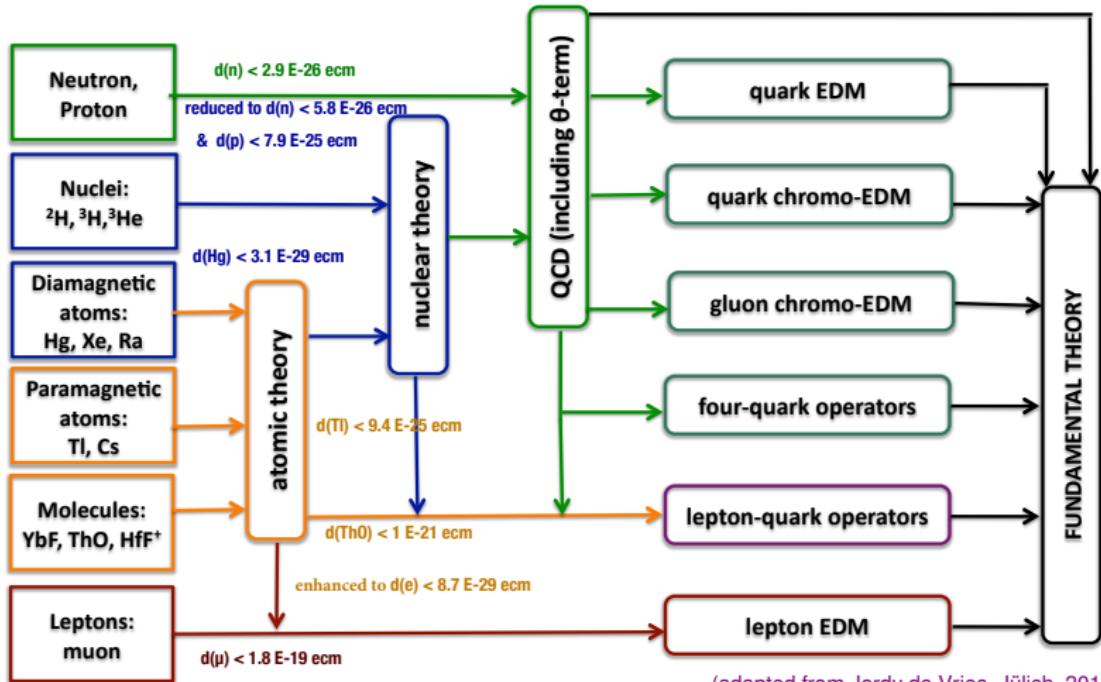


and why are EDMs of *light ions* interesting?

Road map from EDM Measurements to EDM Sources

Experimentalist's point of view →

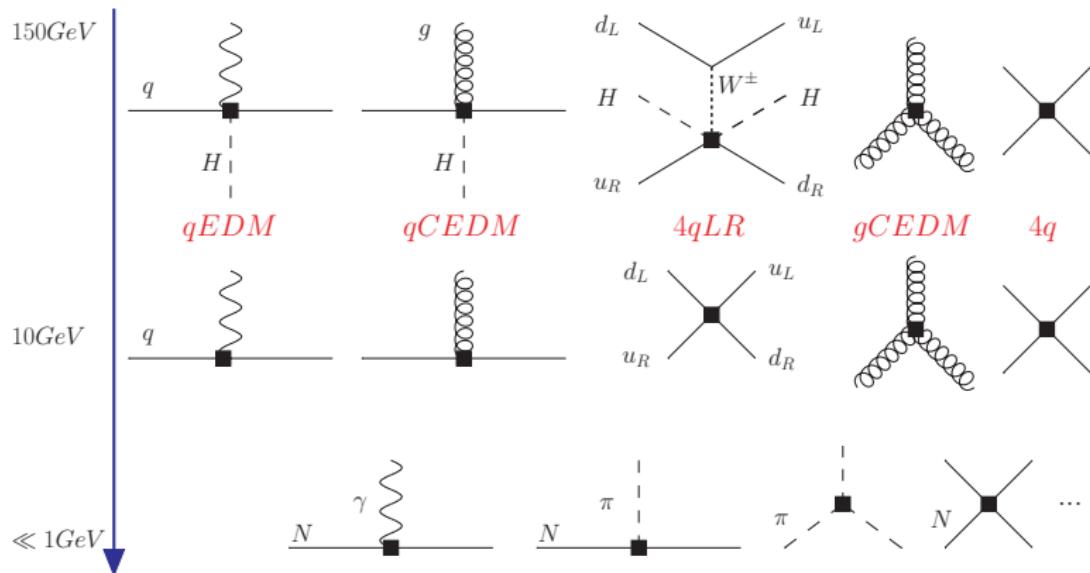
← Theorist's point of view



(adapted from Jordy de Vries, Jülich, 2013)

CP-violating BSM sources of dimension 6 from above EW scale to their hadronic equivalents below 1 GeV

W. Dekens & J. de Vries, JHEP 05 (2013)



$$\begin{aligned}
 \text{Total #} &= 1(\bar{\theta}) + 2(qEDM) + 2(qCEDM) + 1(4qLR) + 1(gCEDM) + 2(4q) \quad [+3(\text{semi}) + 1(\text{lept})] \\
 &= \underbrace{1(\text{dim-four}) + 8(\text{dim-six})}_{\rightarrow 5 \text{ discriminable classes}} \quad [+3+1] \quad [\text{Caveat: } m_s \gg m_u, m_d \text{ (\& } m_\mu \gg m_e \text{) assumed}]
 \end{aligned}$$

EDM Translator

from 'quarkish/machine' to 'hadronic/human' language?



D. Vorderstraße

EDM Translator

from ‘quarkish/machine’ to ‘hadronic/human’ language?



D. Vorderstraße

Symmetries (esp. chiral one) plus Goldstone Theorem
→ Low-Energy Effective Field Theory with External Sources
i.e. Chiral Perturbation Theory (suitably extended)

Scalings of \mathcal{CP} hadronic vertices – from θ to BSM sources

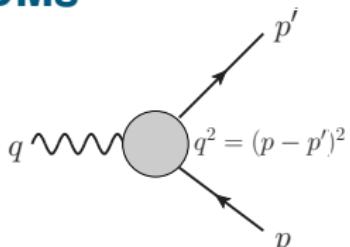
5 discriminable classes:

	g_0 \mathcal{CP}, I	g_1 \mathcal{CP}, I	d_0, d_1 $\mathcal{CP}, \text{I+I'}$	$(m_N \Delta)$ $\mathcal{CP}, \text{I'}$	$C_{1,2}(C_{3,4})$ $\mathcal{CP}, \text{I(I')}$
$\mathcal{L}_{\text{EFT}}^{\mathcal{CP}}$:					
θ -term:	$\mathcal{O}(1)$	$\mathcal{O}(M_\pi/m_N)$	$\mathcal{O}(M_\pi/m_N)$	$\mathcal{O}(M_\pi^2/m_N^2)$	$\mathcal{O}(M_\pi^2/m_N^2)$
qEDM:	$\mathcal{O}(\alpha_{EM}/4\pi)$	$\mathcal{O}(\alpha_{EM}/4\pi)$	$\mathcal{O}(1)$	$\mathcal{O}(\alpha_{EM}/4\pi)$	$\mathcal{O}(\alpha_{EM}/4\pi)$
qCEDM:	$\mathcal{O}(1)$	$\mathcal{O}(1)$	$\mathcal{O}(M_\pi/m_N)$	$\mathcal{O}(M_\pi^2/m_N^2)$	$\mathcal{O}(M_\pi^2/m_N^2)$
4qLR:	$\mathcal{O}(M_\pi^2/m_n^2)$	$\mathcal{O}(1)$	$\mathcal{O}(M_\pi^3/m_N^3)$	$\mathcal{O}(M_\pi/m_n)$	$\mathcal{O}(M_\pi^2/m_N^2)$
gCEDM:	$\mathcal{O}(M_\pi^2/m_N^2)^*$	$\mathcal{O}(M_\pi^2/m_N^2)^*$	$\mathcal{O}(1)$	$\mathcal{O}(M_\pi^2/m_N^2)$	$\mathcal{O}(1)$
4q:	$\mathcal{O}(M_\pi^2/m_N^2)^*$	$\mathcal{O}(M_\pi^2/m_N^2)^*$	$\mathcal{O}(1)$	$\mathcal{O}(M_\pi^2/m_N^2)$	$\mathcal{O}(1)$

*) Goldstone theorem \rightarrow relative $\mathcal{O}(M_\pi^2/m_n^2)$ suppression of $N\pi$ interactions

Calculation: from form factors to EDMs

$$\langle f(p') | J_{\text{em}}^\mu | f(p) \rangle = \bar{u}_f(p') \Gamma^\mu(q^2) u_f(p)$$



$$\Gamma^\mu(q^2) = \gamma^\mu F_1(q^2) - i\sigma^{\mu\nu} q_\nu \frac{F_2(q^2)}{2m_f} + \sigma^{\mu\nu} q_\nu \gamma_5 \frac{F_3(q^2)}{2m_f} + (\not{q} q^\mu - q^2 \gamma^\mu) \gamma_5 \frac{F_a(q^2)}{m_f^2}$$

Dirac FF

Pauli FF

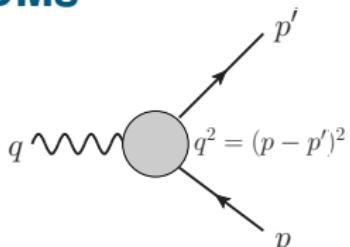
electric dipole FF (\mathcal{GP})

anapole FF (\mathcal{P}')

$$\hookrightarrow d_f := \lim_{q^2 \rightarrow 0} \frac{F_3(q^2)}{2m_f} \quad \text{for } s = 1/2 \text{ fermion}$$

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$$\langle f(p') | J_{\text{em}}^\mu | f(p) \rangle = \bar{u}_f(p') \Gamma^\mu(q^2) u_f(p)$$



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Dirac FF

Pauli FF

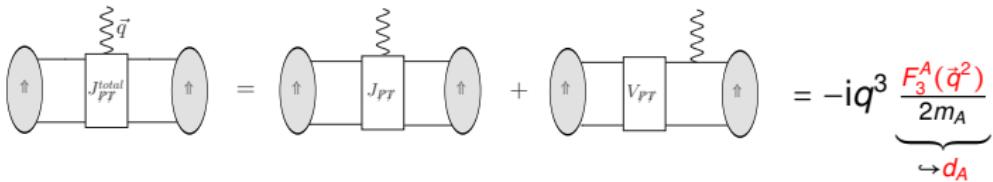
electric dipole FF (\mathcal{OP})

anapole FF (\mathcal{P})

$$\rightarrow d_f := \lim_{q^2 \rightarrow 0} \frac{F_3(q^2)}{2m_f} \quad \text{for } s = 1/2 \text{ fermion}$$

Nucleus A

$\langle \uparrow | J_{PT}^0(q) | \uparrow \rangle$
in Breit frame



$$\langle \uparrow | J_{PT}^0(q) | \uparrow \rangle = \langle \uparrow | J_{PT}^{\text{total}} | \uparrow \rangle + \langle \uparrow | V_{PT} | \uparrow \rangle = -iq^3 \underbrace{\frac{F_3(\vec{q}^2)}{2m_A}}_{\rightarrow d_A}$$

θ -Term Induced Nucleon EDM

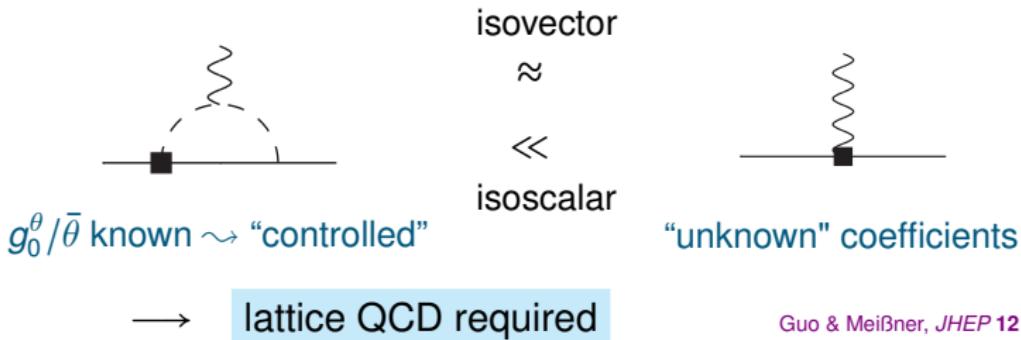
Crewther, di Vecchia, Veneziano & Witten, *PLB*(1979); Pich & de Rafael, *NPB*(1991); Ott nad et al., *PLB*(2010)

Isovector πNN coupling:

$$g_0^\theta = \frac{(m_n - m_p)^{\text{strong}}(1 - \epsilon^2)}{4F_\pi\epsilon} \bar{\theta} \approx (-0.018 \pm 0.007)\bar{\theta} \quad (\text{where } \epsilon \equiv \frac{m_u - m_d}{m_u + m_d})$$

$$\hookrightarrow dN_{\text{loop}}^{\text{isovector}} \sim (2.1 \pm 0.9) \cdot 10^{-16} \bar{\theta} \text{ e cm}$$
Bsaisou et al., *EPJA* **49** (2013)

single nucleon EDM:

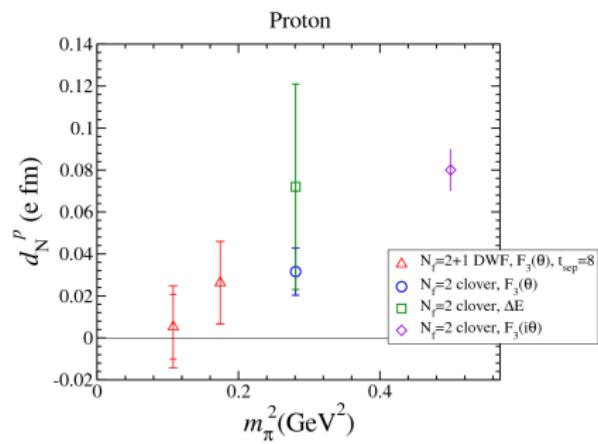
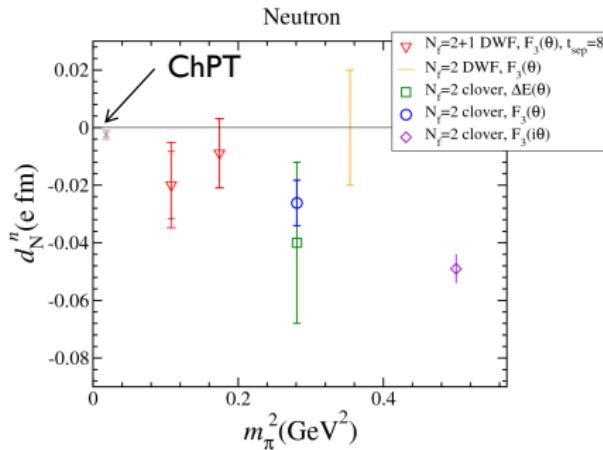


Guo & Meißner, *JHEP* **12** (2012)

Preliminary Lattice (full QCD) results

neutron EDM and

proton EDM



$$\theta \equiv 1 !$$

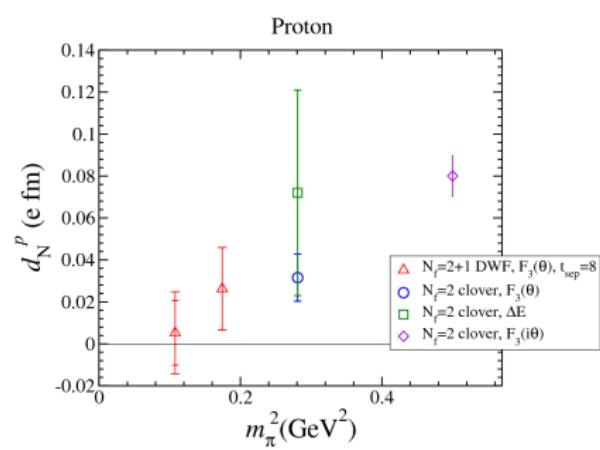
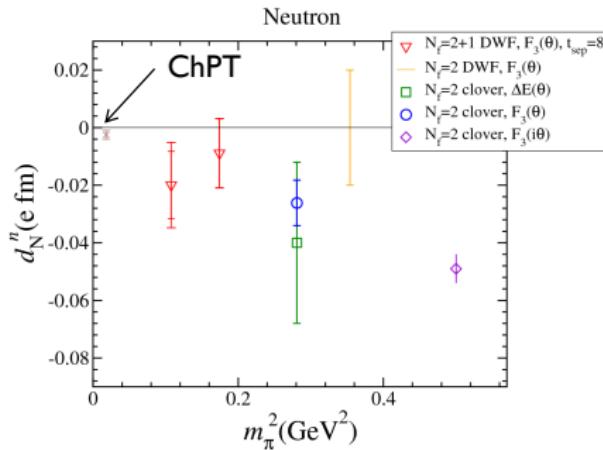
(adapted from Eigo Shintani (Mainz), *Lattice calculation of nucleon EDM*, Hirschegg, Jan. 14, 2014)

no systematical errors!

Preliminary Lattice (full QCD) results

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$$\theta \equiv 1 !$$

(adapted from Eigo Shintani (Mainz), *Lattice calculation of nucleon EDM*, Hirschegg, Jan. 14, 2014)

no systematical errors!

$$\hookrightarrow d_n = \bar{\theta} (-2.7 \pm 1.2) \cdot 10^{-3} \cdot e \cdot fm \quad \text{and} \quad d_p = \bar{\theta} (2.1 \pm 1.2) \cdot 10^{-3} \cdot e \cdot fm$$

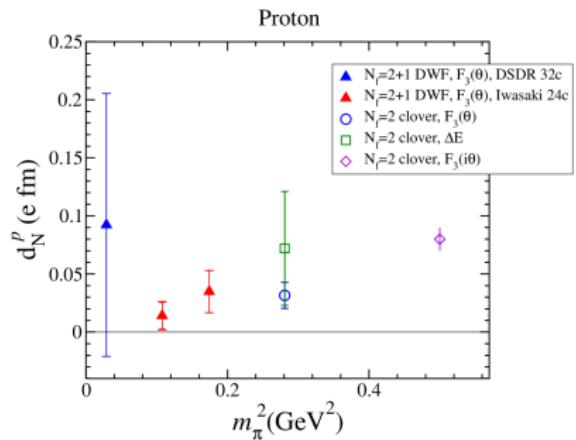
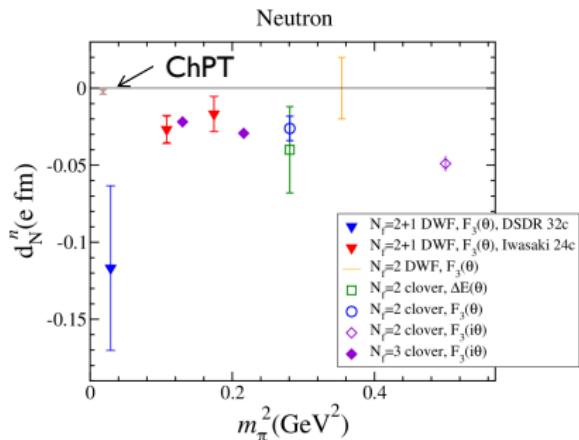
Akan, Guo & Meißner, *PLB 736* (2014); see also $d_n = \bar{\theta} (-3.9 \pm 0.2 \pm 0.9) 10^{-3} e \text{ fm}$ Guo et al., *PRL 115* (2015)

Preliminary Lattice (full QCD) results

neutron EDM

and

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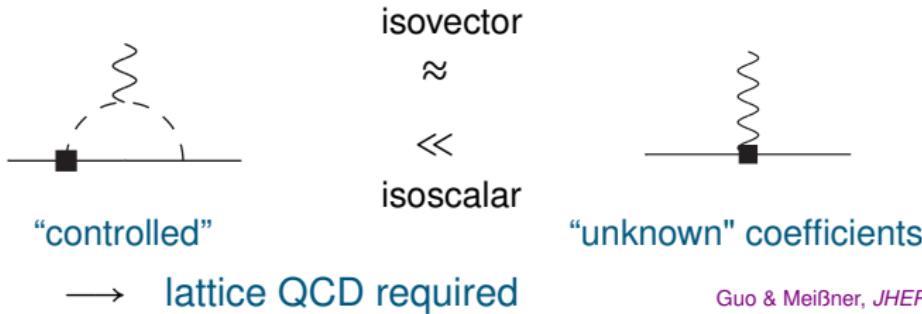


(adapted from Eigo Shintani (RIKEN-AICS), INT Program INT-15-3, Seattle, Sept. 22, 2015)

Don't mention the ... light nuclei

Single Nucleon Versus Nuclear EDM

single nucleon EDM:

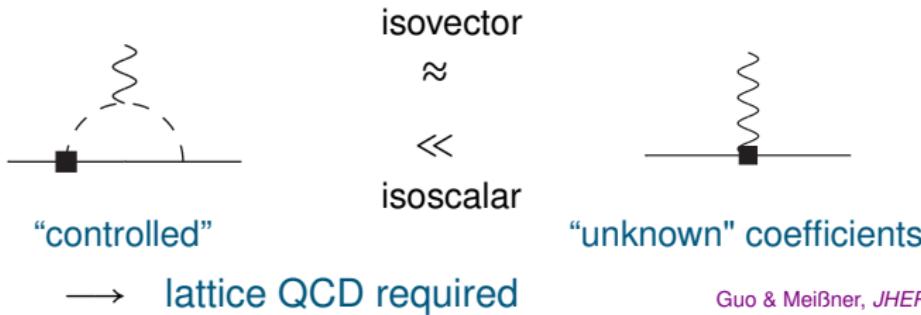


two nucleon EDM:



Single Nucleon Versus Nuclear EDM

single nucleon EDM:

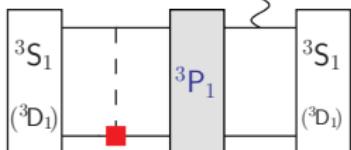


two nucleon EDM:



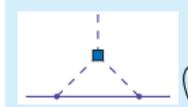
EDM of the Deuteron at LO: CP-violating π exchange

$$\begin{aligned} \mathcal{L}_{CP}^{\pi N} = & -d_n N^\dagger (1 - \tau^3) S^\mu v^\nu N F_{\mu\nu} - d_p N^\dagger (1 + \tau_3) S^\mu v^\nu N F_{\mu\nu} \\ & + (m_N \Delta) \pi^2 \pi_3 + \cancel{g_0 N^\dagger \vec{\pi} \cdot \vec{\tau} N} + \cancel{g_1 N^\dagger \pi_3 N} \\ & + \cancel{C_1 N^\dagger N D_\mu (N^\dagger S^\mu N)} + \cancel{C_2 N^\dagger \vec{\tau} N \cdot D_\mu (N^\dagger \vec{\tau} S^\mu N)} + \dots \end{aligned}$$



LO: $\cancel{g_0 N^\dagger \vec{\pi} \cdot \vec{\tau} N}$ (CP, I) $\rightarrow 0$ (Isospin filter!)

NLO: $g_1 N^\dagger \pi_3 N$ (CP, I) \rightarrow "LO" in D case



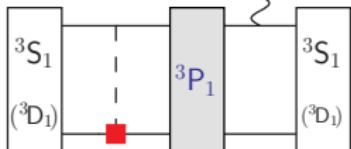
term	$N^2\text{LO ChPT}$	Δv_{18}	CD-Bonn	units
d_n^D	0.939 ± 0.009	0.914	0.927	d_n
d_p^D	0.939 ± 0.009	0.914	0.927	d_p
g_1	0.183 ± 0.017	0.186	0.186	$g_1 e \text{ fm}$
Δf_{g_1}	-0.748 ± 0.138	-0.703	-0.719	$\Delta e \text{ fm}$

Bsaisou, dissertation, Univ. Bonn (2014); Bsaisou et al., JHEP 03 (2015)

BSM CP sources: $g_1 \pi NN$ vertex is of LO in qCEDM and 4qLR case

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Yamanaka & Hiyama, PRC 91 (2015):

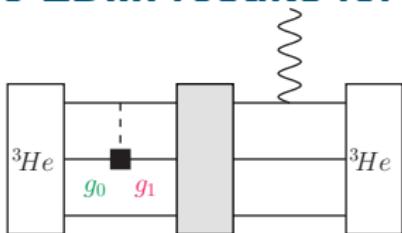
$$d_N^D = \left(1 - \frac{3}{2} P_{^3D_1}\right) d_N$$

term	N^2 LO ChPT	Δv_{18}	CD-Bonn	units
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BSM CP sources: $g_1 \pi NN$ vertex is of LO in qCEDM and 4qLR case

${}^3\text{He}$ EDM: results for CP-violating π exchange



$g_0 N^\dagger \vec{\pi} \cdot \vec{\tau} N$ ($\cancel{\text{CP}}$, I)

LO: θ -term, qCEDM

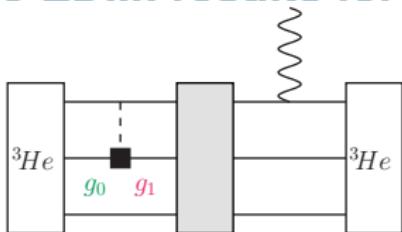
$N^2\text{LO}$: 4qLR

$g_1 N^\dagger \pi_3 N$ ($\cancel{\text{CP}}$, \cancel{I})

LO: qCEDM, 4qLR

NLO: θ term

^3He EDM: results for CP-violating π exchange


 $g_0 N^\dagger \vec{\pi} \cdot \vec{\tau} N$ (\cancel{CP}, I)

 LO: θ -term, qCEDM

 $N^2\text{LO}$: 4qLR

 $g_1 N^\dagger \pi_3 N$ (\cancel{CP}, I)

LO: qCEDM, 4qLR

 $N\text{LO}$: θ term

term	A	$N^2\text{LO ChPT}$	$\text{Av}_{18} + \text{UIX}$	CD-Bonn+TM	units
d_n	^3He ^3H	0.904 ± 0.013 -0.030 ± 0.007	0.875 -0.051	0.902 -0.038	d_n
d_p	^3He ^3H	-0.029 ± 0.006 0.918 ± 0.013	-0.050 0.902	-0.037 0.876	d_p
Δ	^3He ^3H	-0.017 ± 0.006 -0.017 ± 0.006	-0.015 -0.015	-0.019 -0.019	$\Delta e \text{ fm}$
g_0	^3He ^3H	0.111 ± 0.013 -0.108 ± 0.013	0.073 -0.073	0.087 -0.085	$g_0 e \text{ fm}$
g_1	^3He ^3H	0.142 ± 0.019 0.139 ± 0.019	0.142 0.142	0.146 0.144	$g_1 e \text{ fm}$
Δf_{g_1}	^3He ^3H	-0.608 ± 0.142 -0.598 ± 0.141	-0.556 -0.564	-0.586 -0.576	$\Delta e \text{ fm}$
C_1	^3He ^3H	-0.042 ± 0.017 0.041 ± 0.016	-0.0014 0.0014	-0.016 0.016	$C_1 e \text{ fm}^{-2}$
C_2	^3He ^3H	0.089 ± 0.022 -0.087 ± 0.022	0.0042 -0.0044	0.033 -0.032	$C_2 e \text{ fm}^{-2}$

^3He EDM: results for CP-violating π exchange

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term	A	$\text{N}^2\text{LO ChPT}$	$\text{Av}_{18}+\text{UIX}$	CD-Bonn+TM	units
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C_2	^3He ^3H	0.089 ± 0.022 -0.087 ± 0.022	0.0042 -0.0044	0.033 -0.032	$C_2 e \text{ fm}^{-2}$

Discriminating between three \mathcal{CP} scenarios at 1 GeV

Dekens et al., *JHEP* 07 (2014); Bsaisou et al., *JHEP* 03 (2015)

1 The Standard Model + $\bar{\theta}$

$$\mathcal{L}_{\text{SM}}^{\bar{\theta}} = \mathcal{L}_{\text{SM}} + \bar{\theta} m_q^* \bar{q} i \gamma_5 q$$

2 The left-right symmetric model — with two 4-quark operators:

$$\mathcal{L}_{LR} = -i \Xi [1.1 (\bar{u}_R \gamma_\mu u_R) (\bar{d}_L \gamma^\mu d_L) + 1.4 (\bar{u}_R t^a \gamma_\mu u_R) (\bar{d}_L t^a \gamma^\mu d_L)] + \text{h.c.}$$

3 The aligned two-Higgs-doublet model — with the dipole operators:

$$\mathcal{L}_{a2HM} = -e \frac{d_d}{2} \bar{d} i \sigma_{\mu\nu} \gamma_5 d F^{\mu\nu} - \frac{\tilde{d}_d}{4} \bar{d} i \sigma_{\mu\nu} \gamma_5 \lambda^a d G^{a\mu\nu} + \frac{d_W}{3} f_{abc} \tilde{G}^{a\mu\nu} G_{\mu\rho}^b G_{\nu}^{c\rho}$$

— with the hierarchy $\tilde{d}_d \simeq 4d_d \simeq 20d_W$

matched on

$$\begin{aligned} \mathcal{L}_{\mathcal{CP}\text{EFT}}^{\pi N} &= -d_N N^\dagger (1 - \tau^3) S^\mu v^\nu N F_{\mu\nu} - d_p N^\dagger (1 + \tau_3) S^\mu v^\nu N F_{\mu\nu} \\ &\quad + (m_N \Delta) \pi^2 \pi_3 + g_0 N^\dagger \vec{\pi} \cdot \vec{\tau} N + g_1 N^\dagger \pi_3 N \\ &\quad + C_1 N^\dagger N \mathcal{D}_\mu (N^\dagger S^\mu N) + C_2 N^\dagger \vec{\tau} N \cdot \mathcal{D}_\mu (N^\dagger \vec{\tau} S^\mu N) + \dots . \end{aligned}$$

Discriminating between three \mathcal{CP} scenarios at 1 GeV

Dekens et al., JHEP 07 (2014); Bsaisou et al., JHEP 03 (2015)

1 The Standard Model + $\bar{\theta}$

$$\mathcal{L}_{\text{SM}}^{\bar{\theta}} = \mathcal{L}_{\text{SM}} + \bar{\theta} m_q^* \bar{q} i \gamma_5 q$$

2 The left-right symmetric model — with two 4-quark operators:

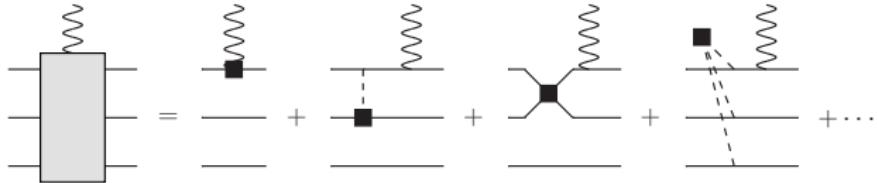
$$\mathcal{L}_{LR} = -i \Xi [1.1 (\bar{u}_R \gamma_\mu u_R) (\bar{d}_L \gamma^\mu d_L) + 1.4 (\bar{u}_R t^a \gamma_\mu u_R) (\bar{d}_L t^a \gamma^\mu d_L)] + \text{h.c.}$$

3 The aligned two-Higgs-doublet model — with the dipole operators:

$$\mathcal{L}_{a2HM} = -e \frac{d_d}{2} \bar{d} i \sigma_{\mu\nu} \gamma_5 d F^{\mu\nu} - \frac{\tilde{d}_d}{4} \bar{d} i \sigma_{\mu\nu} \gamma_5 \lambda^a d G^{a\mu\nu} + \frac{d_W}{3} f_{abc} \tilde{G}^{a\mu\nu} G_{\mu\rho}^b G_{\nu}^{c\rho}$$

— with the hierarchy $\tilde{d}_d \simeq 4d_d \simeq 20d_W$

matched on



Testing strategies: SM + $\bar{\theta}$

Dekens et al., *JHEP* **07** (2014); Bsaisou et al., *JHEP* **03** (2015)

Measurement of the helion
and neutron EDMs

Testing strategies: SM + $\bar{\theta}$

Dekens et al., JHEP 07 (2014); Bsaisou et al., JHEP 03 (2015)

Measurement of the helion
and neutron EDMs

$$d_{^3\text{He}} - 0.9d_n = -\bar{\theta} (1.01 \pm 0.31_{\text{had}} \pm 0.29^*_{\text{nucl}}) \cdot 10^{-16} e\text{cm}$$

Extraction of $\bar{\theta}$

* includes ± 0.20 uncertainty from 2N contact terms

Testing strategies: SM + $\bar{\theta}$

Dekens et al., JHEP 07 (2014); Bsaisou et al., JHEP 03 (2015)

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Extraction of $\bar{\theta}$

$$d_D - 0.94(d_n + d_p) = \bar{\theta} (0.89 \pm 0.29_{\text{had}} \pm 0.08_{\text{nucl}}) \cdot 10^{-16} e\text{ cm}$$

Prediction for $d_D - 0.94(d_n + d_p)$

(& triton EDM): $d_D^{\text{Nucl}} \approx -d_{^3\text{He}}^{\text{Nucl}} \approx \frac{1}{2} d_{^3\text{H}}^{\text{Nucl}}$

* includes ± 0.20 uncertainty from 2N contact terms

Testing strategies: SM + $\bar{\theta}$

Dekens et al., JHEP 07 (2014); Bsaisou et al., JHEP 03 (2015)

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Prediction for $d_D - 0.94(d_n + d_p)$

$$(\& triton EDM): d_D^{\text{Nucl}} \approx -d_{^3\text{He}}^{\text{Nucl}} \approx \frac{1}{2} d_{^3\text{H}}^{\text{Nucl}}$$

$$g_1^\theta / g_0^\theta \approx -0.2$$

* includes ± 0.20 uncertainty from 2N contact terms

$$g_0^\theta = \frac{(m_n - m_p)^{\text{strong}} (1 - \epsilon^2)}{4F_\pi \epsilon} \bar{\theta} = (-16 \pm 2) 10^{-3} \bar{\theta}$$

$$\frac{g_1^\theta}{g_0^\theta} \approx \frac{8c_1(M_{\pi^\pm}^2 - M_{\pi^0}^2)^{\text{strong}}}{(m_n - m_p)^{\text{strong}}} , \quad \epsilon \equiv \frac{m_u - m_d}{m_u + m_d}$$

Testing strategies: minimal LR symmetric Model

Dekens et al. *JHEP* 07 (2014); Bsaisou et al. *JHEP* 03 (2015)

Measurement of the deuteron
and nucleon EDMs

Testing strategies: minimal LR symmetric Model

Dekens et al. *JHEP* 07 (2014); Bsaisou et al. *JHEP* 03 (2015)

Measurement of the deuteron
and nucleon EDMs

$$d_D - 0.94(d_n + d_p) \simeq d_D = -(2.1 \pm 0.5^*) \Delta^{LR} \text{ e fm}$$

Extraction of Δ^{LR}

* includes ± 0.1 uncertainty from 2N contact terms

Testing strategies: minimal LR symmetric Model

Dekens et al. *JHEP* 07 (2014); Bsaisou et al. *JHEP* 03 (2015)

Measurement of the deuteron
and nucleon EDMs

$$d_D - 0.94(d_n + d_p) \simeq d_D = -(2.1 \pm 0.5^*) \Delta^{LR} \text{ e fm}$$

Extraction of Δ^{LR}

$$d_{^3\text{He}} - 0.9d_n \simeq d_{^3\text{He}} = -(1.7 \pm 0.5^*) \Delta^{LR} \text{ e fm}$$

Prediction for the helion EDM
(& triton EDM): $d_D \approx d_{^3\text{He}} \approx d_{^3\text{H}}$

* includes ± 0.1 uncertainty from 2N contact terms

Testing strategies: minimal LR symmetric Model

Dekens et al. *JHEP* 07 (2014); Bsaisou et al. *JHEP* 03 (2015)

Measurement of the deuteron
and nucleon EDMs

$$d_D - 0.94(d_n + d_p) \simeq d_D = -(2.1 \pm 0.5^*) \Delta^{LR} \text{ e fm}$$

Extraction of Δ^{LR}

$$d_{^3\text{He}} - 0.9d_n \simeq d_{^3\text{He}} = -(1.7 \pm 0.5^*) \Delta^{LR} \text{ e fm}$$

Prediction for the helion EDM
(& triton EDM): $d_D \approx d_{^3\text{He}} \approx d_{^3\text{H}}$

$$\begin{aligned} g_1^{LR} &= 8c_1 m_N \Delta^{LR} &= (-7.5 \pm 2.3) \Delta^{LR}, \\ g_0^{LR} &= \frac{(m_n - m_p)^{\text{str}} m_N}{M_\pi^2} \Delta^{LR} &= (0.12 \pm 0.02) \Delta^{LR} \end{aligned}$$

$-g_1^{LR}/g_0^{LR} \gg 1$ (!)

* includes ± 0.1 uncertainty from 2N contact terms

Testing strategies: aligned 2-Higgs Doublet Model

Dekens et al. *JHEP* 07 (2014); Bsaisou et al. *JHEP* 03 (2015)

Measurement of the deuteron
and nucleon EDMs

Testing strategies: aligned 2-Higgs Doublet Model

Dekens et al. *JHEP* 07 (2014); Bsaisou et al. *JHEP* 03 (2015)

Measurement of the deuteron
and nucleon EDMs

$$d_D - 0.94(d_n + d_p) = [(0.18 \pm 0.02)g_1 - (0.75 \pm 0.14)\Delta] \text{ e fm}$$

Extraction of g_1^{eff} (including Δ correction)

Testing strategies: aligned 2-Higgs Doublet Model

Dekens et al. *JHEP* 07 (2014); Bsaisou et al. *JHEP* 03 (2015)

Measurement of the deuteron
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Extraction of g_1^{eff} (including Δ correction)

+ Measurement of $d_{^3\text{He}}$ (or $d_{^3\text{H}}$)

Testing strategies: aligned 2-Higgs Doublet Model

Dekens et al. *JHEP* 07 (2014); Bsaisou et al. *JHEP* 03 (2015)

Measurement of the deuteron
and nucleon EDMs

$$d_D - 0.94(d_n + d_p) = [(0.18 \pm 0.02)g_1 - (0.75 \pm 0.14)\Delta] \text{efm}$$

Extraction of g_1^{eff} (including Δ correction)

+ Measurement of $d_{^3\text{He}}$ (or $d_{^3\text{H}}$)

$$\begin{aligned} d_{^3\text{He}} - 0.9d_n \\ = [(0.11 \pm 0.02^*)g_0 + (0.14 \pm 0.02^*)g_1 - (0.61 \pm 0.14)\Delta] \text{efm} \end{aligned}$$

Extraction of g_0

* includes ± 0.01 uncertainty from 2N contact terms

Testing strategies: aligned 2-Higgs Doublet Model

Dekens et al. *JHEP* 07 (2014); Bsaisou et al. *JHEP* 03 (2015)

Measurement of the deuteron
and nucleon EDMs

$$d_D - 0.94(d_n + d_p) = [(0.18 \pm 0.02)g_1 - (0.75 \pm 0.14)\Delta] \text{ e fm}$$

Extraction of g_1^{eff} (including Δ correction)

+ Measurement of $d_{^3\text{He}}$ (or $d_{^3\text{H}}$)

$$d_{^3\text{He}} - 0.9d_n = [(0.11 \pm 0.02^*)g_0 + (0.14 \pm 0.02^*)g_1 - (0.61 \pm 0.14)\Delta] \text{ e fm}$$

Extraction of g_0

Prediction of $d_{^3\text{H}}$ (or $d_{^3\text{He}}$)

* includes ± 0.01 uncertainty from 2N contact terms

Summary

- D EDM might **distinguish** between $\bar{\theta}$ and other scenarios and allows **extraction** of the g_1 coupling constant via $d_D - 0.94(d_n + d_p)$. (The prefactor of $(d_n + d_p)$ stands for a 4% probability of the 3D_1 state.)
- ${}^3\text{He}$ (or ${}^3\text{H}$) EDM necessary for a **proper test** of $\bar{\theta}$ and LR scenarios
- Deuteron & helion work as complementary **isospin filters** of EDMs
- **a2HDM scenario:** helion *and* triton EDMs would be needed for a test
- pure qCEDM: similar to a2HDM scenario
- pure qEDM: $d_D = 0.94(d_n + d_p)$ and $d_{{}^3\text{He}/{}^3\text{H}} = 0.9d_{n/p}$
- gCEDM, 4quark chiral singlet:
controlled calculation/disentanglement difficult (lattice ?)
- Ultimate progress may eventually come from **Lattice QCD**
 $\hookrightarrow \mathcal{GP} N\pi$ couplings g_0 & g_1 may be accessible even for dim-6 case

Traditional atomic EDMs

- Why can't we get **this info** from EDMs of Hg, Ra, Rn, ... ?

Strong bound on atomic EDM: $|d_{^{199}\text{Hg}}| < 3.1 \cdot 10^{-29} \cdot e \cdot \text{fm}$

Griffiths et al., *PRL* (2009)

- The **atomic** part of the calculation is well under control

$$d_{^{199}\text{Hg}} = (2.8 \pm 0.6) S_{\text{Hg}} \cdot e \cdot \text{fm}^{-2}$$

Dzuba et al., *PRA* (2002), (2009)

S_{Hg} : Nuclear Schiff moment

- But the **nuclear** part isn't ...

$$S_{^{199}\text{Hg}} = [(0.3 \pm 0.4)g_0 + (0.4 \pm 0.8)g_1] e \cdot \text{fm}^3$$

Engel et al., *PPNP* (2013)

- There is **no power counting** for nuclei with so many nucleons
- Short-range 4N contributions **not even considered**
- Hadronic uncertainties of g_0 and g_1 are **underestimated** too

Conclusions

- EDMs **probe** New *CP-odd Physics* (at similar energy scales as LHC)
- The **first** non-vanishing EDM might be detected in a **charge-neutral** case: *neutrons* or *dia-/ paramagnetic atoms* or *molecules* ...
However, measurements of **light ion EDMs** will play a key role in
disentangling the sources of (flavor-diagonal) CP
- EDM measurements are of *low-energy nature*:
 - ↪ non-leptonic predictions have to be in the *language of hadrons*
 - ↪ only systematical methods: *ChPT/EFT* and *Lattice QCD*
- EDMs of light nuclei give **independent information** to nucleon ones and may be even larger and, moreover, even **simpler**

At least the EDMs of p , n , d , and ${}^3\text{He}$ are needed
to have a realistic chance to disentangle the underlying physics

Many thanks to my colleagues

in Jülich: **Jan Bsaisou**, Christoph Hanhart, Susanna Liebig, Ulf-G. Meißner,
David Minossi, Andreas Nogga, **Jordy de Vries**

in Bonn: Feng-Kun Guo, Bastian Kubis, Ulf-G. Meißner

and: Werner Bernreuther, Wouter Dekens, Bira van Kolck, Kolya Nikolaev

References:

- 1 J. Bsaisou, U.-G. Meißner, A. Nogga and A.W.,
P- and T-Violating Lagrangians in Chiral Effective Field Theory and Nuclear Electric Dipole Moments, Annals of Physics **359**, 317-370 (2015), arXiv:1412.5471[hep-ph].
- 2 J. Bsaisou, C. Hanhart, S. Liebig, D. Minossi, U.-G. Meißner, A. Nogga and A.W.,
Electric dipole moments of light nuclei, JHEP **03**, 104 (05, 083) (2015), arXiv:1411.5804.
- 3 A.W., *Electric dipole moments of the nucleon and light nuclei*
Nuclear Physics A **928**, 116-127 (2014), arXiv:1404.6131 [hep-ph].
- 4 W. Dekens, J. de Vries, J. Bsaisou, W. Bernreuther, C. Hanhart, U.-G. Meißner,
A. Nogga and A.W.,
Unraveling models of CP violation through electric dipole moments of light nuclei,
JHEP **07**, 069 (2014), arXiv:1404.6082 [hep-ph].
- 5 J. Bsaisou, C. Hanhart, S. Liebig, U.-G. Meißner, A. Nogga and A.W.,
The electric dipole moment of the deuteron from the QCD θ -term,
Eur. Phys. J. A **49**, 31 (2013), arXiv:1209.6306 [hep-ph].

Backup slides

Hierarchy among the sources at the hadronic EFT level

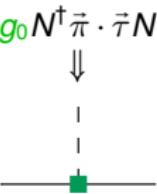
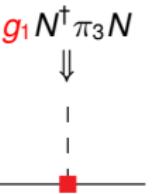
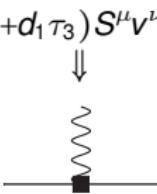
Each source transforms differently under chiral and isospin symmetry

\mathcal{CP}, I	\mathcal{CP}, I	$\mathcal{CP}, I + I'$
$\mathcal{L}_{\text{EFT}}^{\mathcal{CP}} = g_0 N^\dagger \vec{\pi} \cdot \vec{\tau} N + g_1 N^\dagger \pi_3 N + N^\dagger (d_0 + d_1 \tau_3) S^{\mu\nu} F_{\mu\nu} N + \dots$	\downarrow \downarrow \downarrow	\downarrow \downarrow \downarrow
		
dominant for $\bar{\theta}$ term	suppressed for $\bar{\theta}$ term	suppressed by $\mathcal{O}(M_\pi^2)$

- $\mathcal{L}_{QCD}^\theta = \bar{\theta} m_q^* \sum_f \bar{q}_f i \gamma_5 q_f$: \mathcal{CP}, I $m_q^* = \frac{m_u m_d}{m_u + m_d}$
 - ↪ $\bar{\theta}$ source **breaks chiral symmetry** ($\propto m_q^*$) but conserves the isospin one:
 - ↪ $|g_0^\theta| \gg |g_1^\theta|$: NDA estimate: $g_1^\theta / g_0^\theta \sim \mathcal{O}(M_\pi^2 / m_n^2)$ de Vries et al. *PRC* '11
 - ChPT LECs predict: $g_1^\theta / g_0^\theta \sim \mathcal{O}(M_\pi / m_n)$! Bsaisou et al. *EPJA* '13

Hierarchy among the sources at the hadronic EFT level

Each source transforms differently under chiral and isospin symmetry

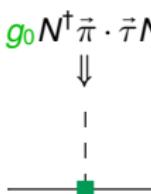
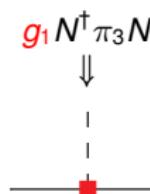
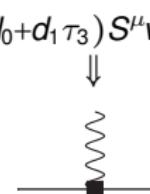
\mathcal{CP}, I	\mathcal{CP}, I	$\mathcal{CP}, I + I$
$\mathcal{L}_{\text{EFT}}^{\mathcal{CP}} = g_0 N^\dagger \vec{\pi} \cdot \vec{\tau} N$  ↓ —————	$+ g_1 N^\dagger \pi_3 N$  ↓ —————	$+ N^\dagger (d_0 + d_1 \tau_3) S^\mu v^\nu F_{\mu\nu} N$  ↓
dominant for chromo qEDM source	dominant for chromo qEDM source	$\mathcal{O}(m_\pi^2)$ suppressed for chromo qEDM source

- **chromo quark EDM:** chiral symmetries are (& isospin ones may be) broken because of quark masses \sim Goldstone theorem respected
- **4quark Left-Right EDM:** **explicit** breaking of **chiral & isospin** symmetries because of underlying W boson exchange \sim Goldstone theorem does not apply

Hierarchy among the sources at the hadronic EFT level

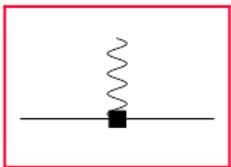
Each source transforms differently under chiral and isospin symmetry

$$\mathcal{L}_{\text{EFT}}^{\mathcal{CP}} = g_0 N^\dagger \vec{\pi} \cdot \vec{\tau} N + g_1 N^\dagger \pi_3 N + N^\dagger (d_0 + d_1 \tau_3) S^{\mu\nu} F_{\mu\nu} N + \dots$$

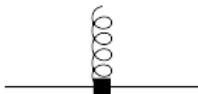

 
 

- **quark EDM:** $N\pi$ (and NN) interactions are **suppressed** by $\alpha_{\text{em}}/(4\pi)$
- **gluon color EDM (and chiral-4quark EDM):** **relative $\mathcal{O}(M_\pi^2)$ suppression** of $N\pi$ interactions because of Goldstone theorem

If $\bar{\theta}$ -term tests fail, then effective BSM dim. 6 sources de Vries et al.(2011)



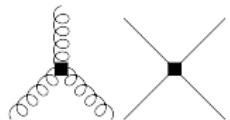
$qEDM$



$qCEDM$



$4qLR$



$gCEDM + 4qEDM$

$$d_D \approx d_p + d_n$$

$$d_{^3He} \approx d_n$$

$$d_D > d_p + d_n$$

$$d_{^3He} > d_n$$

$$d_D > d_p + d_n$$

$$d_{^3He} > d_n$$

$$d_D \sim d_p + d_n$$

$$d_{^3He} \sim d_n$$

→ $g_0, g_1 \propto \alpha/(4\pi)$

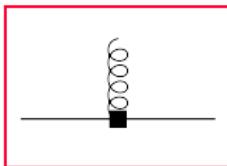
2N contribution suppressed by photon loop!

here: only absolute values considered

If $\bar{\theta}$ -term tests fail, then effective BSM dim. 6 sources de Vries et al.(2011)



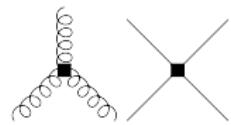
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$$d_D > d_p + d_n$$

$$d_{^3He} > d_n$$

$$d_D \sim d_p + d_n$$

$$d_{^3He} \sim d_n$$

→ g_0 , g_1 dominant and of the same order

$2N$ contribution enhanced!

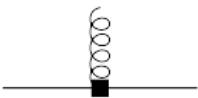
here: only absolute values considered

If $\bar{\theta}$ -term tests fail, then effective BSM dim. 6 sources

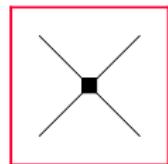
de Vries et al.(2011)



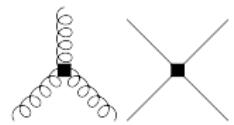
$qEDM$



$qCEDM$



$4qLR$



$gCEDM + 4qEDM$

$$d_D \approx d_p + d_n$$

$$d_{^3He} \approx d_n$$

$$d_D > d_p + d_n$$

$$d_{^3He} > d_n$$

$$d_D > d_p + d_n$$

$$d_{^3He} > d_n$$

$$d_D \sim d_p + d_n$$

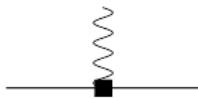
$$d_{^3He} \sim d_n$$

→ $g_1 \gg g_0$; 3π -coupling (unsuppressed in 3He)

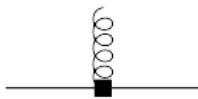
isospin-breaking $2N$ contribution enhanced!

here: only absolute values considered

If $\bar{\theta}$ -term tests fail, then effective BSM dim. 6 sources de Vries et al.(2011)



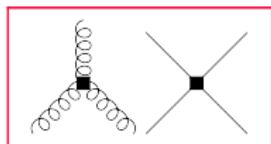
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$$d_D > d_p + d_n$$

$$d_{^3He} > d_n$$

$$d_D \sim d_p + d_n$$

$$d_{^3He} \sim d_n$$

→ g_1 , g_0 , $4N$ – coupling on the same footing

$2N$ contribution difficult to asses!

here: only absolute values considered

θ -term: ~~CP~~ πNN vertices determined from LECs

Leading g_0^θ coupling (from c_5)

Crewther et al. (1979);
 Ott nad et al. (2010); Mereghetti et al. (2011);
 de Vries et al. (2011); Bsaisou et al. (2013)

g_0^θ : $N^\dagger \vec{\pi} \cdot \vec{\tau} N$ -vertex

$$\mathcal{L}_{\pi N} = \dots + c_5 2B N^\dagger \left((m_u - m_d) \tau_3 + \frac{2m^* \bar{\theta}}{F_\pi} \vec{\pi} \cdot \vec{\tau} \right) N + \dots$$

$$\delta M_{np}^{str} = 4B(m_u - m_d)c_5 \rightarrow g_0^\theta = \bar{\theta} \delta M_{np}^{str} (1 - \epsilon^2) \frac{1}{4F_\pi \epsilon}$$

$$\delta M_{np}^{em} \rightarrow \delta M_{np}^{str} = (2.6 \pm 0.5) \text{MeV} \quad \text{Walker-Loud et al. (2012)}$$

$$\rightarrow g_0^\theta = (-0.018 \pm 0.007) \bar{\theta}$$

$$\epsilon = (m_u - m_d)/(m_u + m_d), \quad 4Bm^* = M_\pi^2(1 - \epsilon^2), \quad m^* = \frac{m_u m_d}{m_u + m_d}$$

θ -term: subleading g_1^θ coupling (from c_1 LEC)

g_1^θ : $\pi_3 NN$ -vertex

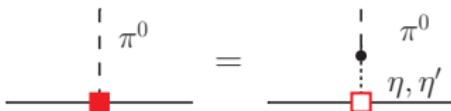
$$\epsilon := (m_u - m_d) / (m_u + m_d)$$

$$\mathcal{L}_{\pi N} = \dots + c_1 4B N^\dagger \left((m_u + m_d) + \frac{(\delta M_\pi^2)_{QCD} (1 - \epsilon^2) \bar{\theta}}{2BF_\pi \epsilon} \pi_3 \right) N + \dots$$

1 $c_1 \longleftrightarrow \sigma_{\pi N}$: $c_1 = (-1.0 \pm 0.3) \text{ GeV}^{-1}$

Compilation: Baru et al. (2011)

2 $(\delta M_\pi^2)_{QCD} \approx \frac{\epsilon^2}{4} \frac{M_\pi^4}{M_K^2 - M_\pi^2}$



$$\rightarrow g_1^\theta = (0.003 \pm 0.002) \bar{\theta}$$

Bsaisou et al. (2013)

$$\frac{g_1^\theta}{g_0^\theta} = -0.20 \pm 0.13 \sim \frac{M_\pi}{m_N}$$

Bsaisou et al. (2013)

$$\gg \epsilon \frac{M_\pi^2}{m_N^2} \sim -0.01 \quad (\text{NDA})$$

de Vries et al. (2011)

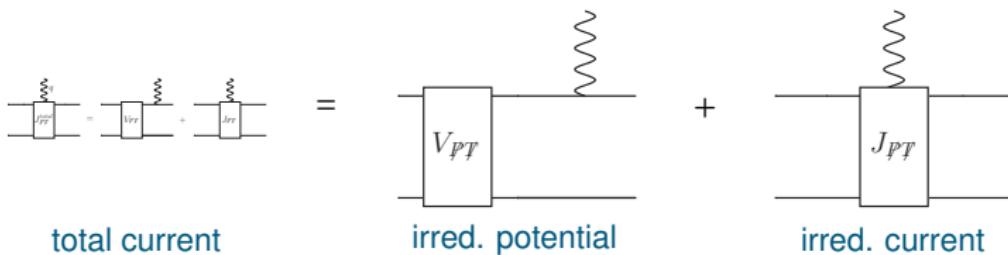
$g_0^\theta (\delta M_{np}^{str})$ is unnaturally small!

EDM of the Deuteron:

Deuteron (D) as Isospin Filter

note:  = $\frac{ie}{2}(1 + \tau_3)$

2N-system: $I + S + L = \text{odd}$



total current

$I = 0$

$I = 0$

irred. potential

$I = 0 \rightarrow I = 1 \rightarrow I = 0$

irred. current

$I = 0 \quad I = 0$

isospin selection rules!

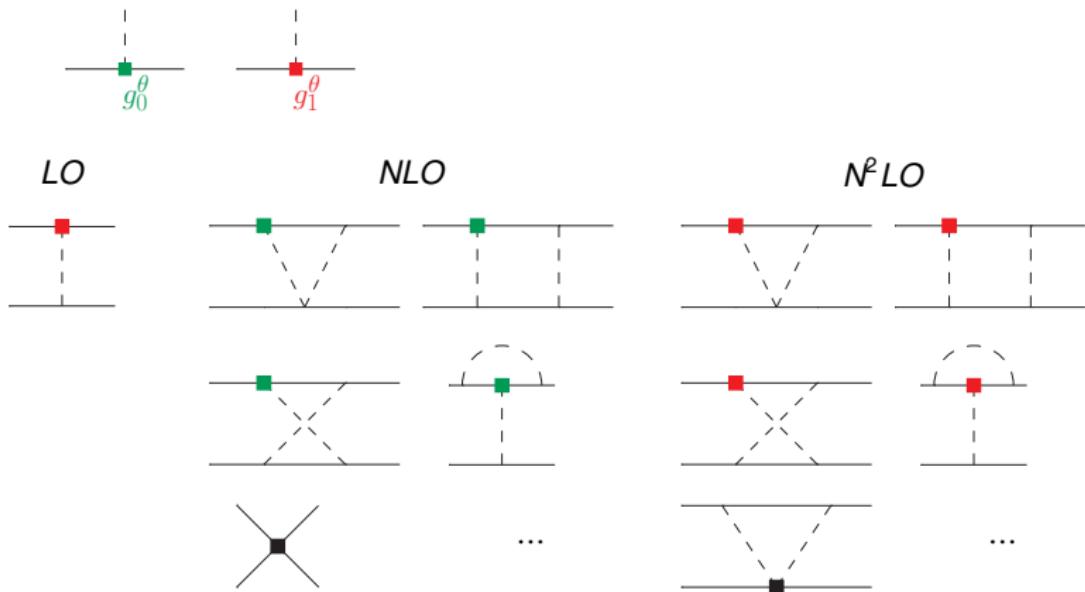


~~$g_0^\theta N^\dagger \vec{\pi} \cdot \vec{\tau} N$~~ at leading order (LO)

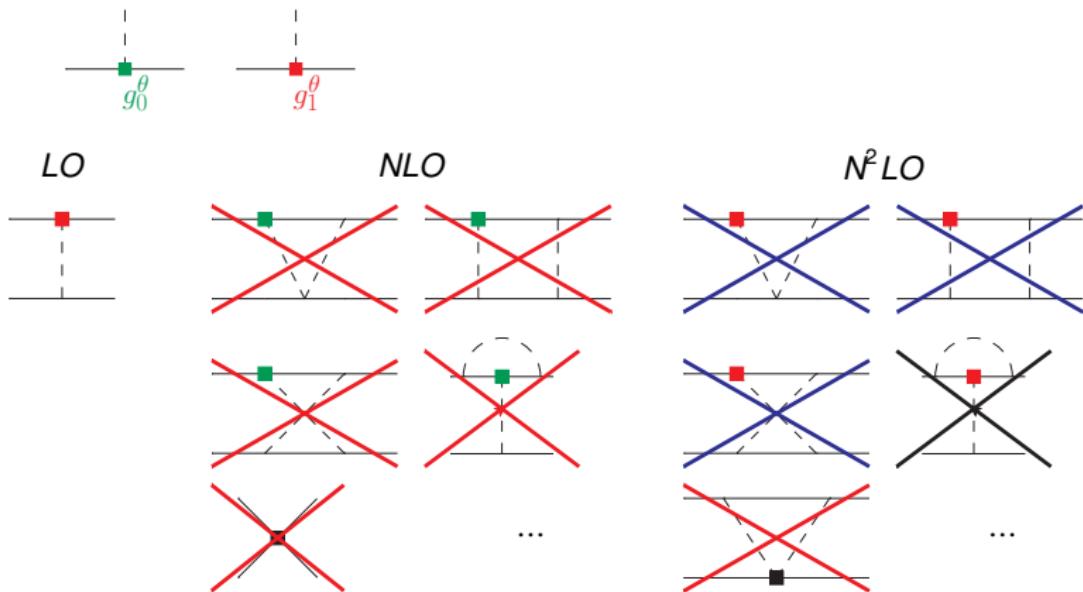


subleading (NLO) $g_1^\theta N^\dagger \pi_3 N$ acts as 'new' leading order (LO) for D

EDM of the Deuteron: NLO -and N^2LO Potentials

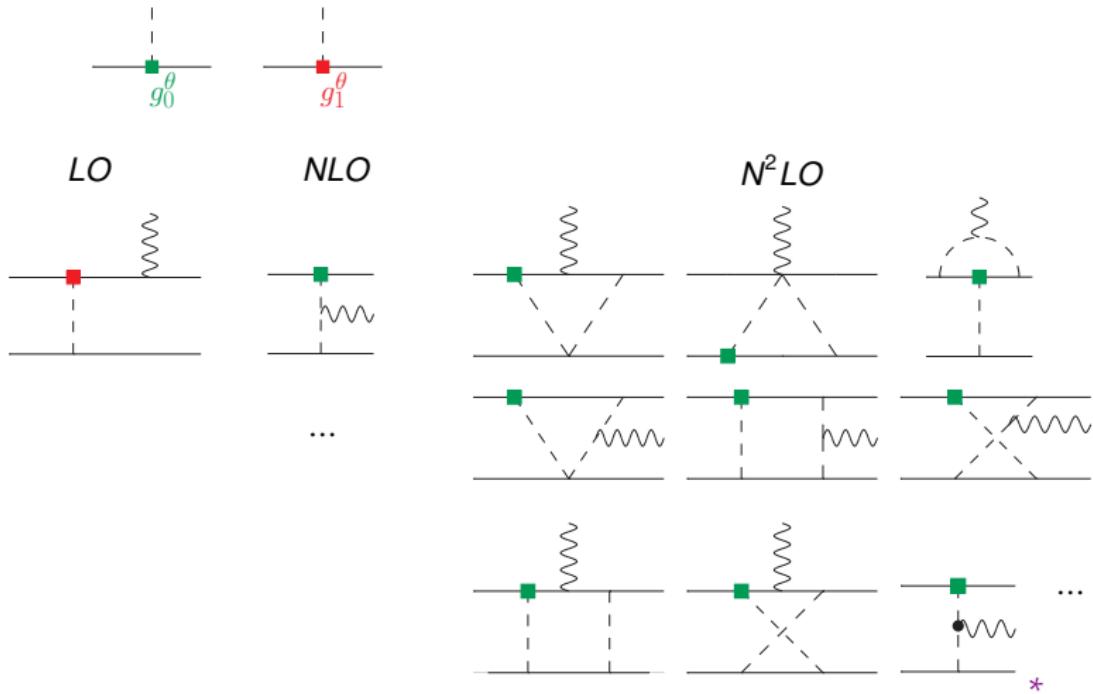


EDM of the Deuteron: NLO-and N^2LO Potentials



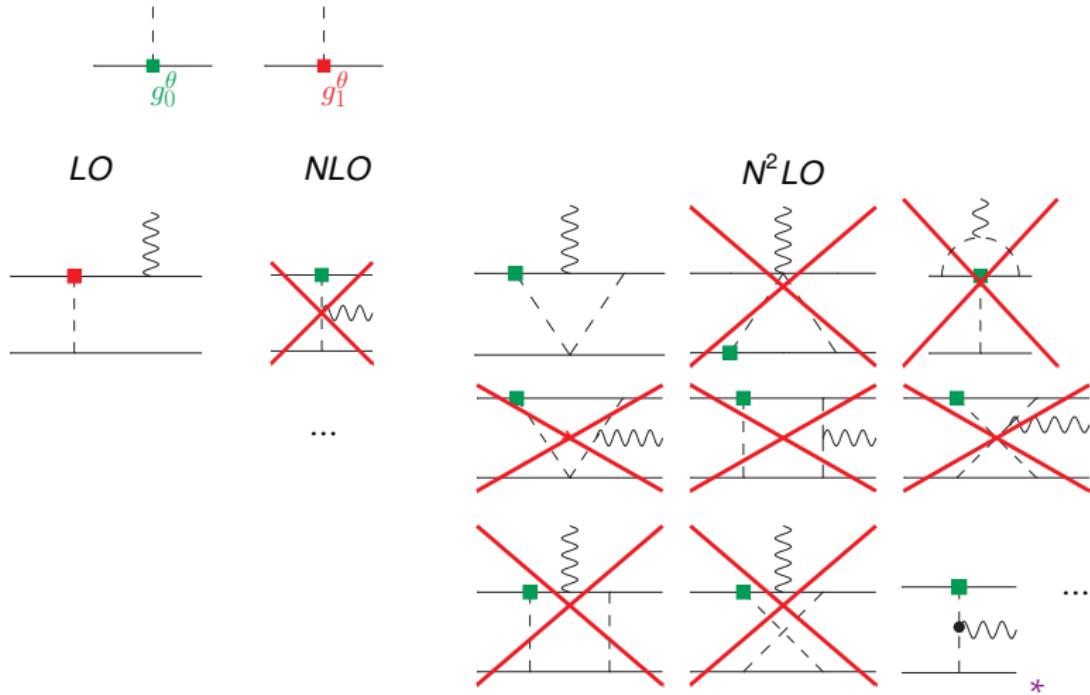
- $\textcolor{red}{X}$: vanishing by selection rules, $\textcolor{blue}{X}$: sum of diagrams vanishes
 \times : vertex correction

EDM of the Deuteron: NLO and N^2LO Currents



*: de Vries et al. (2011), Bsaisou et al. (2013)

EDM of the Deuteron: NLO and N^2LO Currents



- \times : vanishing by selection rules, \times : sum of diagrams vanishes

A *naive* estimate of the scale of the nucleon EDM

Khriplovich & Lamoreaux (1997); Kolya Nikolaev (2012)

- CP & P conserving magnetic moment \sim nuclear magneton μ_N

$$\mu_N = \frac{e}{2m_p} \sim 10^{-14} \text{ ecm}.$$

- A nonzero EDM requires

parity P violation: the price to pay is $\sim 10^{-7}$

$$(G_F \cdot F_\pi^2 \sim 10^{-7} \text{ with } G_F \approx 1.166 \cdot 10^{-5} \text{ GeV}^{-2}),$$

and **CP violation:** the price to pay is $\sim 10^{-3}$

$$(|\eta_{+-}| \equiv |\mathcal{A}(K_L^0 \rightarrow \pi^+ \pi^-)| / |\mathcal{A}(K_S^0 \rightarrow \pi^+ \pi^-)| = (2.232 \pm 0.011) \cdot 10^{-3}).$$

- In summary: $|d_N| \sim 10^{-7} \times 10^{-3} \times \mu_N \sim 10^{-24} \text{ ecm}$
- In SM (without θ term): extra $G_F F_\pi^2$ factor to *undo* flavor change

$$\hookrightarrow |d_N^{\text{SM}}| \sim 10^{-7} \times 10^{-24} \text{ ecm} \sim 10^{-31} \text{ ecm}$$

\hookrightarrow *The empirical window* for search of physics BSM($\theta=0$) is

$$10^{-24} \text{ ecm} > |d_N| > 10^{-30} \text{ ecm}.$$

Chronology of upper bounds on the neutron EDM

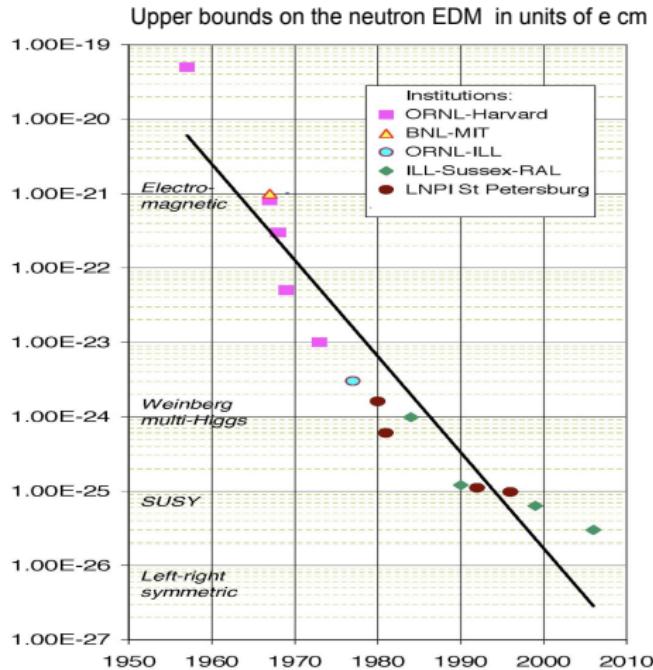


Fig. courtesy of N.N. Nikolaev

Smith, Purcell, Ramsey (1957) Baker et al. (2006)

→ 5 to 6 orders above SM predictions which are out of reach !

Chronology of upper bounds on the neutron EDM

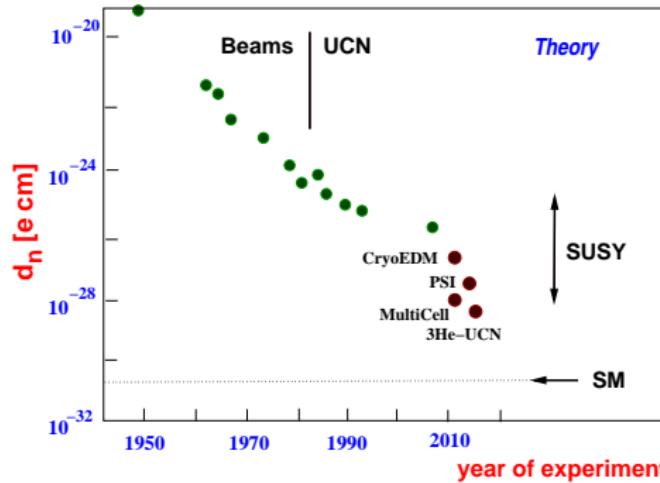


Fig. courtesy of U.-G. Meißner

Smith, Purcell, Ramsey (1957) Baker et al. (2006)

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Chronology of upper bounds on the neutron EDM

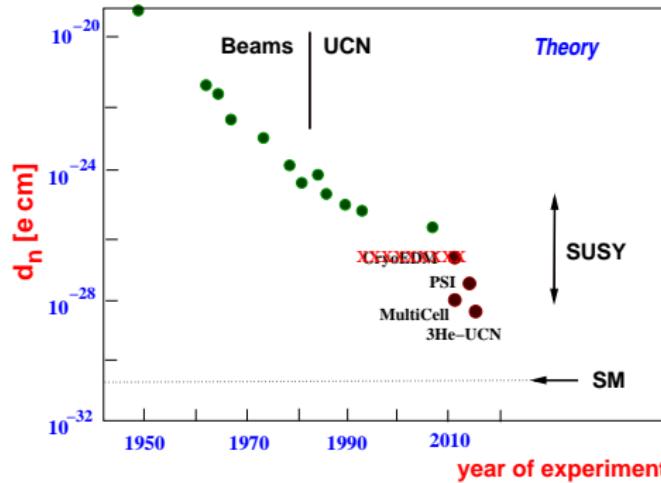


Fig. courtesy of U.-G. Meißner

Smith, Purcell, Ramsey (1957) Baker et al. (2006)

→ 5 to 6 orders above SM predictions which are out of reach !

EDM bounds from neutral particles

- Modern neutron EDM experiments at ILL, SNS, PSI, TRIUMF
 current $d_n = (0.2 \pm 1.5(\text{stat.}) \pm 0.7(\text{sys.})) \cdot 10^{-26} \text{ ecm}$
 proposed $\sim 10^{-28} \text{ ecm}$

Baker et al. *PRL* '06 (ILL)

- Proton (and neutron) EDM inferred from diamagnetic atoms

current $|d(^{199}\text{Hg})| < 3.1 \cdot 10^{-29} \text{ ecm}$ (95% C.L.)

Griffith et al. *PRL* '09 (UW)

$$\hookrightarrow |d_p| < 7.9 \cdot 10^{-25} \text{ ecm}$$

Theory input from: Dimitriev & Sen'kov *PRL* '03

ongoing experiments on Ra, Rn, Xe, ...

- Electron EDM inferred from paramagnetic atoms or non-generate molecules:

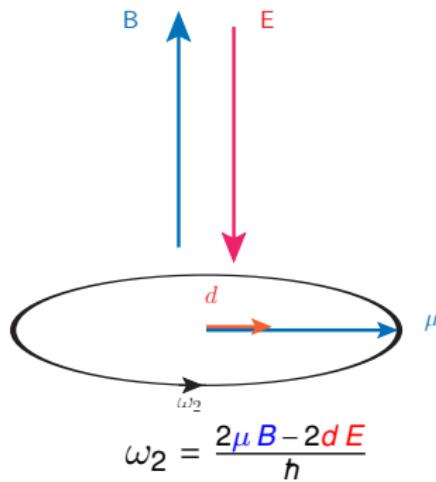
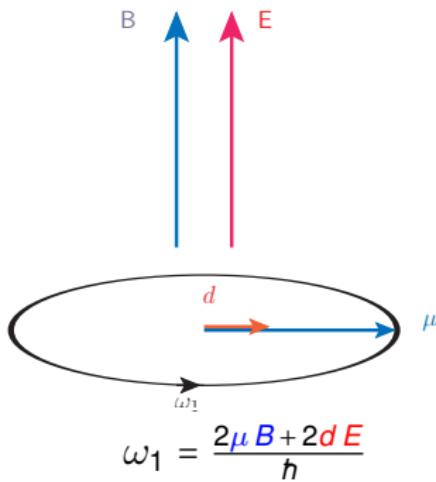
current $|d_e| < 8.7 \cdot 10^{-29} \text{ ecm}$ (90% C.L.)

from polar ThO

Baron et al. *Science* '14 (ACME)

EDM measurement of neutral particles in a nutshell

ground state with $s = 1/2$:

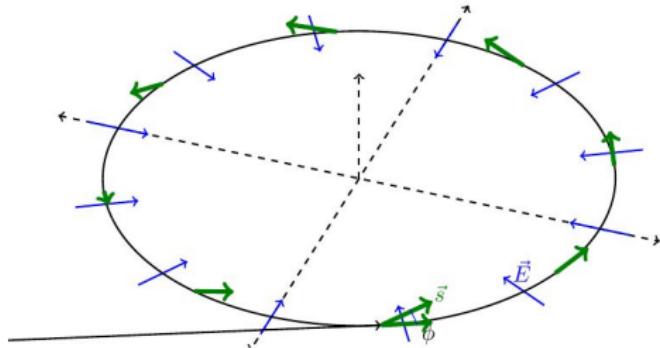


$$\omega_1 - \omega_2 = \frac{4d E}{\hbar}$$

Direct EDM searches with charged particles in storage rings

General idea:

Farley et al. *PRL* '04



Initially **longitudinally** polarized particles interact with **radial \vec{E} field**
 ↳ **build-up of vertical polarization** (measured with a polarimeter)

Limit on muon EDM: $d_\mu < 1.8 \cdot 10^{-19} \text{ e cm}$ (95 % C. L.) Bennett et al. (BNL g-2) *PRL* '09:

Proposed storage ring experiments ($\sim 10^{-29} \text{ e cm}$):

- Counter-circling proton ring at Brookhaven (srEDM) or Fermilab (Project X) ?
- All-purpose ring for proton, deuteron (and helion) in Jülich (JEDI) ?
- ↳ Precursor experiment ($\gtrsim 10^{-24} \text{ e cm}$) for p or D at COSY@Jülich !

CP violation in the Standard Model

The conventional source: Kobayashi-Maskawa mechanism

Empirical facts: 3 generations of u/d quarks (& e/ν leptons)

- quarks & leptons in **mass basis** \neq quarks & leptons in **weak-int. basis**
- $\mathcal{L}_{\text{SM}} = \mathcal{L}_{\text{gauge}} + \mathcal{L}_{\text{gauge-fermion}} + \mathcal{L}_{\text{gauge-Higgs}} + \mathcal{L}_{\text{Higgs-fermion}}$ is CP inv.,
 - with the exception of the θ term of QCD (see later)

and the **charged-weak-current interaction** ($\subset \mathcal{L}_{\text{gauge-fermion}}$)

$$\mathcal{L}_{\text{c-w-c}} = -\frac{g_w}{\sqrt{2}} \sum_{ij=1}^3 \bar{d}_{Li} \gamma^\mu \mathbf{V}_{ij} u_{Lj} W_\mu^- - \frac{g_w}{\sqrt{2}} \sum_{ij=1}^3 \bar{\ell}_{Li} \gamma^\mu \mathbf{U}_{ij} \nu_{Lj} W_\mu^- + \text{h.c.}$$

- \mathbf{V} : 3×3 unitary quark-mixing matrix
 - ▶ (Cabibbo-Kobayashi-Maskawa m.)
- \mathbf{U} : 3×3 unitary lepton-mixing matrix
 - ▶ (Maki-Nakagawa-Sakata matrix)

3 angles + 1 CP phase δ_{KM}

3 angles + 1(3) CP phase(s) for Dirac (Majorana) ν_i 's

\mathcal{CP} and EDMs and in the SM with $J_{\text{KM}} = \text{Im}(V_{tb} V_{td}^* V_{cd} V_{cb}^*) \simeq 3 \cdot 10^{-5}$

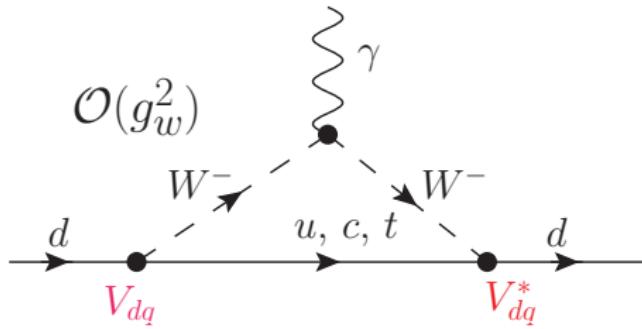
$$\propto \left(\frac{m_t^2 - m_c^2}{M_{EW}^2} \right) \left(\frac{m_c^2 - m_u^2}{M_{EW}^2} \right) \left(\frac{m_t^2 - m_u^2}{M_{EW}^2} \right) \cdot \left(\frac{m_b^2 - m_s^2}{M_{EW}^2} \right) \left(\frac{m_s^2 - m_d^2}{M_{EW}^2} \right) \left(\frac{m_b^2 - m_d^2}{M_{EW}^2} \right) \cdot J_{\text{KM}} \simeq 10^{-15} J_{\text{KM}},$$

Jarlskog *PRL* '85

↪ $(n_B - n_{\bar{B}})/n_\gamma|_{T \sim 20 \text{ MeV}}^{\text{SM}} \sim 10^{-20}$ and $d_n^{\text{SM}} \sim 10^{-20} \cdot 10^{-14} \text{ e cm} \sim 10^{-34} \text{ e cm}$

EDM flavor-neutral ⇒ KM predictions tiny: $\mathcal{O}(G_F^2) \sim \mathcal{O}(g_W^4)$

1 loop:



↪ \mathcal{CP} phase δ_{KM} cancels → prefactor real ⇒ $d_q^{\text{1-loop}} = 0$

\cancel{CP} and EDMs and in the SM with $J_{KM} = \text{Im}(V_{tb} V_{td}^* V_{cd} V_{cb}^*) \simeq 3 \cdot 10^{-5}$

$$\propto \left(\frac{m_t^2 - m_c^2}{M_{EW}^2} \right) \left(\frac{m_c^2 - m_u^2}{M_{EW}^2} \right) \left(\frac{m_t^2 - m_u^2}{M_{EW}^2} \right) \cdot \left(\frac{m_b^2 - m_s^2}{M_{EW}^2} \right) \left(\frac{m_s^2 - m_d^2}{M_{EW}^2} \right) \left(\frac{m_b^2 - m_d^2}{M_{EW}^2} \right) \cdot J_{KM} \simeq 10^{-15} J_{KM},$$

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EDM flavor-neutral ⇒ KM predictions tiny: $\mathcal{O}(G_F^2) \sim \mathcal{O}(g_W^4)$

2 loops:

$$d_{\text{quark}}^{\text{2-loop}} = d_{\text{chromo q}}^{\text{2-loop}} = 0$$

Shabalin *Sov.J.NP* '78

CP and EDMs and in the SM with $J_{\text{KM}} = \text{Im}(V_{tb} V_{td}^* V_{cd} V_{cb}^*) \simeq 3 \cdot 10^{-5}$

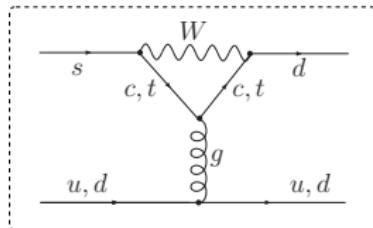
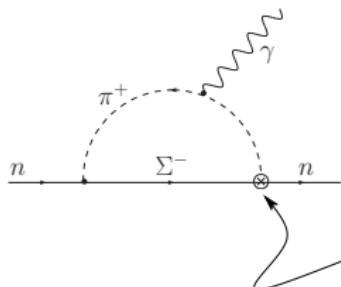
$$\propto \left(\frac{m_t^2 - m_c^2}{M_{EW}^2} \right) \left(\frac{m_c^2 - m_u^2}{M_{EW}^2} \right) \left(\frac{m_t^2 - m_u^2}{M_{EW}^2} \right) \cdot \left(\frac{m_b^2 - m_s^2}{M_{EW}^2} \right) \left(\frac{m_s^2 - m_d^2}{M_{EW}^2} \right) \left(\frac{m_b^2 - m_d^2}{M_{EW}^2} \right) \cdot J_{\text{KM}} \simeq 10^{-15} J_{\text{KM}},$$

Jarlskog *PRL '85*

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EDM flavor-neutral ⇒ KM predictions tiny: $\mathcal{O}(G_F^2) \sim \mathcal{O}(g_W^4)$

however:



$$\mathcal{O}(g_W^4 g_s^2)$$

$d_n^{\text{KM}} \simeq 10^{-32} \text{ e cm}$ because of long-range pion & 'strong penguin'

Gavela; Khriplovich & Zhitnitsky ('82)

CP and EDMs and in the SM with $J_{\text{KM}} = \text{Im}(V_{tb} V_{td}^* V_{cd} V_{cb}^*) \simeq 3 \cdot 10^{-5}$

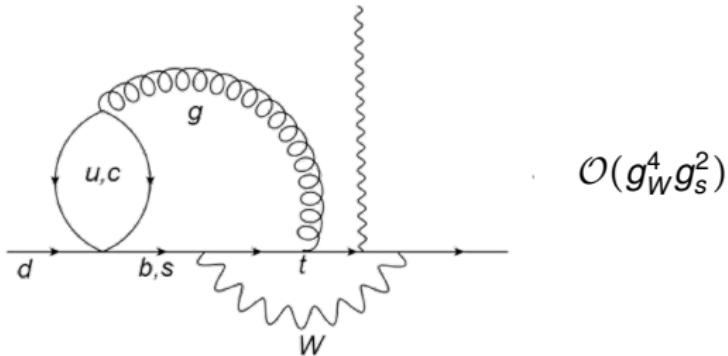
$$\propto \left(\frac{m_t^2 - m_c^2}{M_{EW}^2} \right) \left(\frac{m_c^2 - m_u^2}{M_{EW}^2} \right) \left(\frac{m_t^2 - m_u^2}{M_{EW}^2} \right) \cdot \left(\frac{m_b^2 - m_s^2}{M_{EW}^2} \right) \left(\frac{m_s^2 - m_d^2}{M_{EW}^2} \right) \left(\frac{m_b^2 - m_d^2}{M_{EW}^2} \right) \cdot J_{\text{KM}} \simeq 10^{-15} J_{\text{KM}},$$

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EDM flavor-neutral \Rightarrow KM predictions tiny: $\mathcal{O}(G_F^2) \sim \mathcal{O}(g_W^4)$

at ≥ 3 loops:

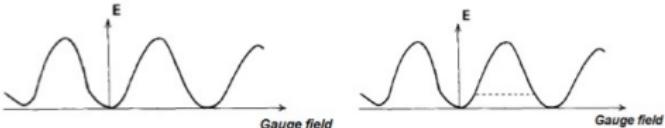


$$d_n^{\text{KM}} \simeq 10^{-34} \dots 10^{-31} \text{ e cm} \quad (d_e^{\text{KM}} \sim 10^{-38} \dots 10^{-40} \text{ e cm since 4 loops & } \mathcal{O}(g_W^6 g_s^2))$$

Khriplovich (1986); Czarnecki & Krause ('97) (Khriplovich & Pospelov (1991))

EDM sources: QCD θ -term of the SM

The topologically non-trivial vacuum structure of QCD



- induces a direct $P \& T \sim CP$ interaction with a new parameter θ :

$$\mathcal{L}_{QCD} = \mathcal{L}_{QCD}^{CP} - \theta \frac{g_s^2}{64\pi^2} \epsilon^{\mu\nu\rho\sigma} G_{\mu\nu}^a G_{\rho\sigma}^a \quad (\text{note: } \epsilon^{0123} = -\epsilon_{0123} \text{ & dim = 4})$$

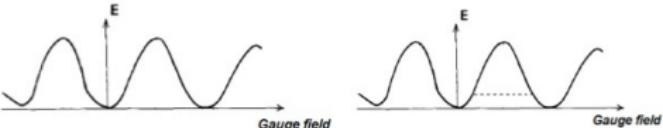
- Anomalous $U_A(1)$ quark-rotations induce mixing with ‘mass’ term

$$-\theta \frac{g_s^2}{64\pi^2} \epsilon^{\mu\nu\rho\sigma} G_{\mu\nu}^a G_{\rho\sigma}^a \xrightarrow{U_A(1)} \bar{\theta} m_q^* \sum_f \bar{q}_f i \gamma_5 q_f \quad (m_q^* = \frac{m_u m_d}{m_u + m_d} \text{ reduced mass})$$

→ additional coupling constant is actually $\bar{\theta} = \theta + \arg \det \mathcal{M}_{\text{quark}}$

EDM sources: QCD θ -term of the SM

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→ additional coupling constant is actually $\bar{\theta} = \theta + \arg \det \mathcal{M}_{\text{quark}}$

- Naive Dimensional Analysis (NDA) estimate of $\bar{\theta}$ -induced n EDM:

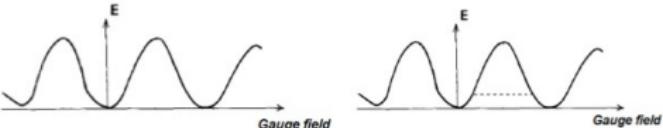
$$|d_n^{\bar{\theta}}| \sim \bar{\theta} \cdot \frac{m_q^*}{m_s} \cdot \frac{e}{2m_n} \sim \bar{\theta} \cdot 10^{-2} \cdot 10^{-14} \text{ e cm} \sim \bar{\theta} \cdot 10^{-16} \text{ e cm} \quad \text{with } \bar{\theta} \sim \mathcal{O}(1).$$

$$|d_n^{\text{emp}}| < 2.9 \cdot 10^{-26} \text{ e cm} \sim |\bar{\theta}| < 10^{-10}$$

► strong CP problem

EDM sources: QCD θ -term of the SM

The topologically non-trivial vacuum structure of QCD



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$$\mathcal{L}_{QCD} = \mathcal{L}_{QCD}^{CP} - \theta \frac{g_s^2}{64\pi^2} \epsilon^{\mu\nu\rho\sigma} G_{\mu\nu}^a G_{\rho\sigma}^a \quad (\text{note: } \epsilon^{0123} = -\epsilon_{0123} \text{ & dim = 4})$$

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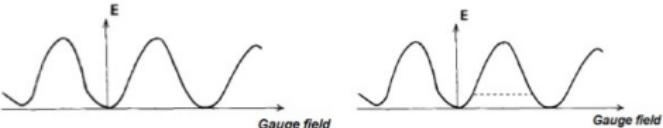
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$10^{-10} > |\bar{\theta}| > 10^{-14}$ eventually measurable via nonzero EDM, but because of $\Lambda_{\chi SB} \ll \Lambda_{EWSB}$ it doesn’t explain the cosmic matter surplus.

EDM sources: QCD θ -term of the SM

The topologically non-trivial vacuum structure of QCD



- induces a direct $P \& T \sim CP$ interaction with a new parameter θ :

$$\mathcal{L}_{QCD} = \mathcal{L}_{QCD}^{CP} - \theta \frac{g_s^2}{64\pi^2} \epsilon^{\mu\nu\rho\sigma} G_{\mu\nu}^a G_{\rho\sigma}^a \quad (\text{note: } \epsilon^{0123} = -\epsilon_{0123} \text{ & dim = 4})$$

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→ additional coupling constant is actually $\bar{\theta} = \theta + \arg \det \mathcal{M}_{\text{quark}}$

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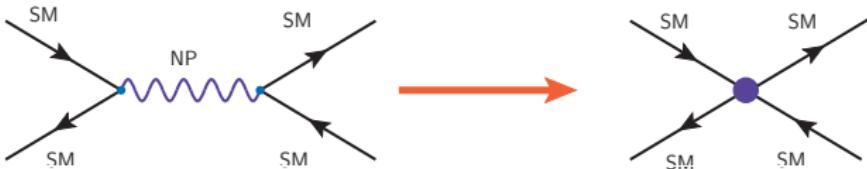
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Thus CP by new physics (NP) (i.e. dimension ≥ 6 sources beyond SM) needed to explain the cosmic matter-antimatter asymmetry.

How to handle CP-violating sources beyond the SM?

New interactions as higher dimensional operators

- Add to the SM **all possible** effective interactions



- The new interactions appear as higher dimensional operators

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{c_5^{(i)}}{M_{\gamma}} \mathcal{O}_5^{(i)} + \sum_i \frac{c_6^{(i)}}{M_{\gamma}^2} \mathcal{O}_6^{(i)} + \dots$$

where M_{γ} is the scale of the *New Physics* particles

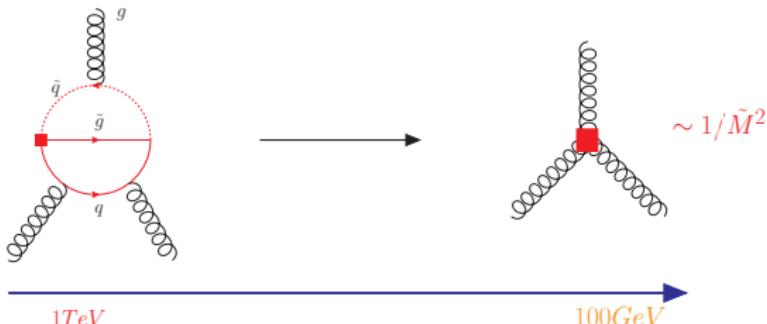
- Only the lowest dimensional operators should be important
- Hadronic EDMs: non-leptonic CP-violating operators of dim. 6
Not of dim. 5 because of Higgs insertion (chiral symm.) at high (low) scales

How to handle CP-violating sources beyond the SM?

Evaluation in Effective Field Theory (EFT) approach

▶ EFT

- All degrees of freedom *beyond NP (EW) scale* are integrated out:
→ Only SM degrees of freedom remain: $q, g, (H, Z, W^\pm, \dots)$
- Write down *all* interactions for these *active* degrees of freedom that *respect the SM+ Lorentz symmetries*: here dim. 6 or higher order
- Need a *power-counting scheme* to order these infinite # interactions
- Relics of eliminated BSM physics ‘remembered’ by the values of the *low-energy constants (LECs)* of the *CP-violating contact terms*, e.g.

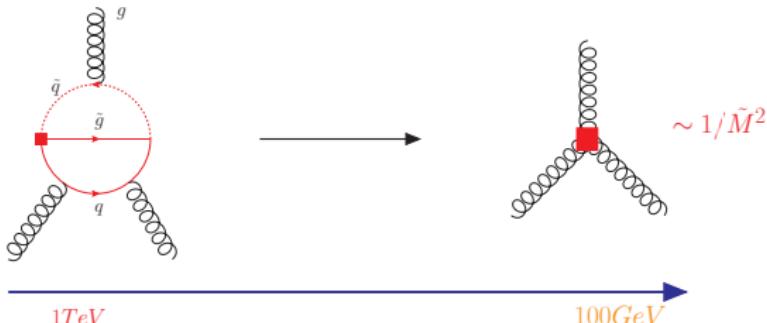


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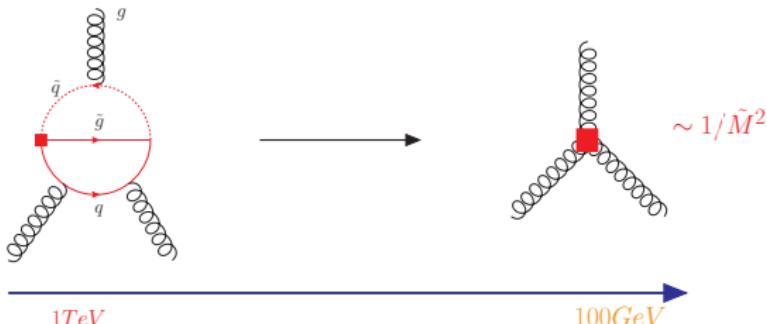


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