

HYPERTRITON LIFETIME IN EFT

16.09.2022 | Fabian Hildenbrand | IAS-4



Theoretical Framework \Rightarrow Pionless EFT

Shallow S-Wave State

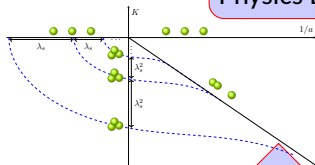
$$J^P = \frac{1}{2}^+$$

Distinguishable

${}^3_{\Lambda}\text{H}$

Theoretical Framework \Rightarrow Pionless EFT

Physics Determined by a and Λ_*



Shallow S-Wave State

$$J^P = \frac{1}{2}^+$$

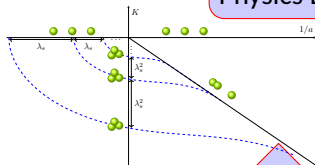
Distinguishable

Large Scattering Length

${}^3\Lambda\text{H}$

Theoretical Framework \Rightarrow Pionless EFT

Physics Determined by a and Λ_*



Universal Relations
Between Observables

Shallow S-Wave State

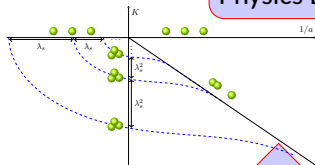
$$J^P = \frac{1}{2}^+$$

Distinguishable

Large Scattering Length

Theoretical Framework \Rightarrow Pionless EFT

Physics Determined by a and Λ_*



Universal Relations
Between Observables

$$B_{\Lambda} \text{ and } \langle r^2 \rangle$$

$$B_{\Lambda} \text{ and } \tau$$

$$B_{\Lambda} \text{ and } a_{\Lambda d}$$

Shallow S-Wave State

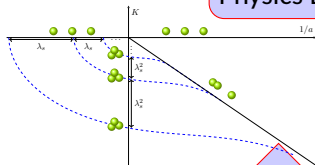
$$J^P = \frac{1}{2}^+$$

Distinguishable

Large Scattering Length

Theoretical Framework \Rightarrow Pionless EFT

Physics Determined by a and Λ_*



Universal Relations
Between Observables

$$B_{\Lambda} \text{ and } \langle r^2 \rangle$$

$$B_{\Lambda} \text{ and } \tau$$

$$B_{\Lambda} \text{ and } a_{\Lambda d}$$

Shallow S-Wave State

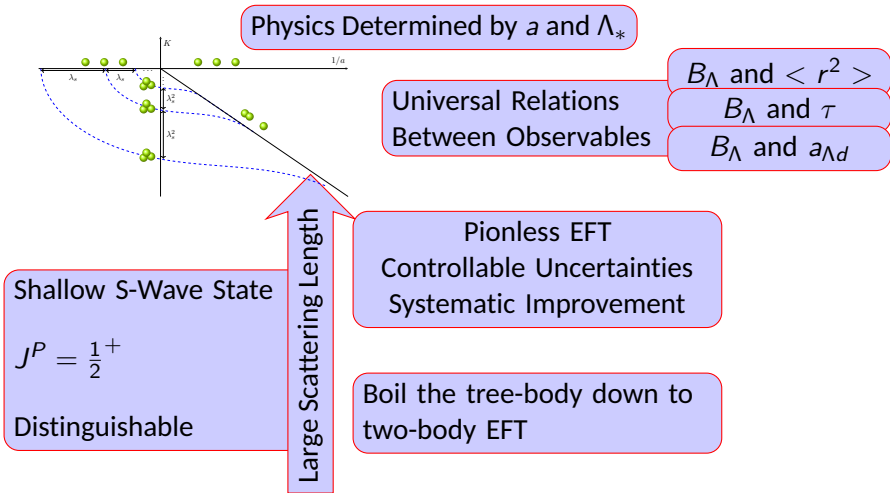
$$J^P = \frac{1}{2}^+$$

Distinguishable

Large Scattering Length

Pionless EFT
Controllable Uncertainties
Systematic Improvement

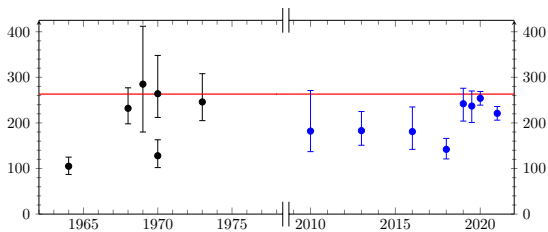
Theoretical Framework \Rightarrow Pionless EFT





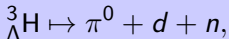
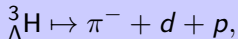
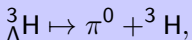
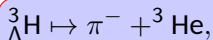
Channels and Isospin Rule

- Two-Body Picture Works
- Calculate Lifetime in a Theory with Fundamental Deuteron
- Focus on B_{Λ} Dependence



${}^3_{\Lambda}\text{H}$

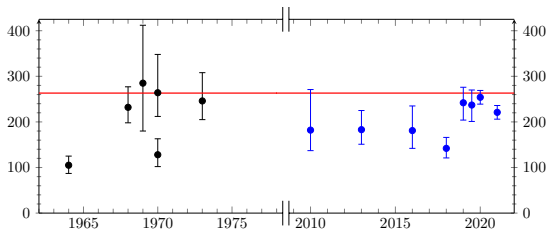
Channels and Isospin Rule



Charged and Uncharged Channel Are Related by the $\Delta I = \frac{1}{2}$ Rule
 \Rightarrow Calculate only one

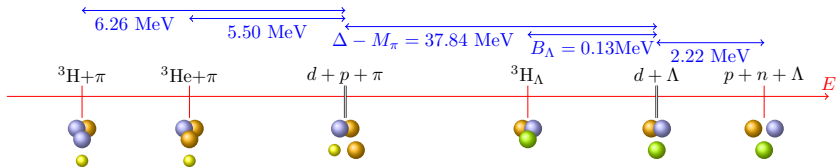
- Two-Body Picture Works
- Calculate Lifetime in a Theory with Fundamental Deuteron
- Focus on B_{Λ} Dependence

Leptonic and Non-Mesonic Decays are Negligible

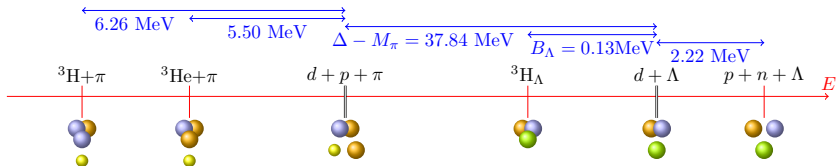


${}^3_{\Lambda}\text{H}$

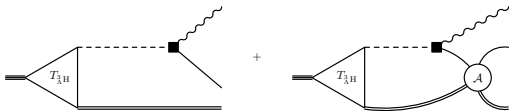
Thresholds and Feynman Diagrams



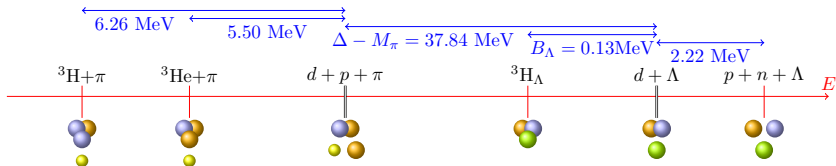
Thresholds and Feynman Diagrams



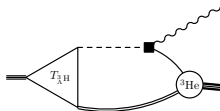
Deuteron Final State



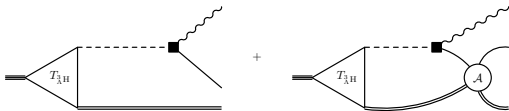
Thresholds and Feynman Diagrams



Trinucleon Final State

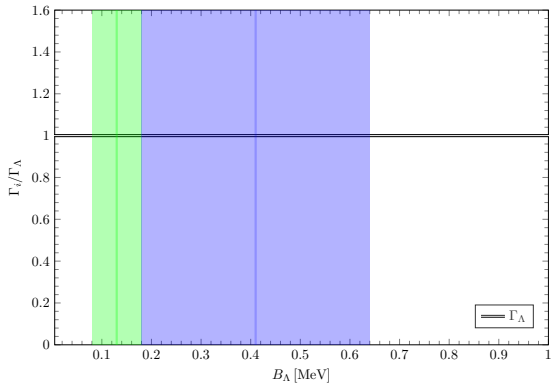


Deuteron Final State



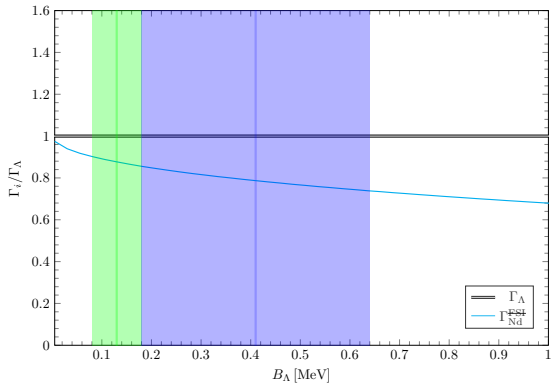
${}^3_{\Lambda}\text{H}$

Hypertriton Width and Branching Ratios



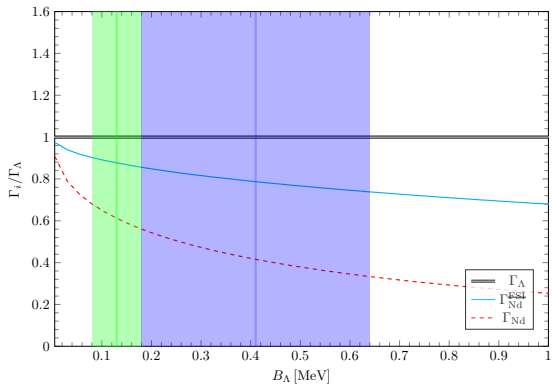


Hypertriton Width and Branching Ratios



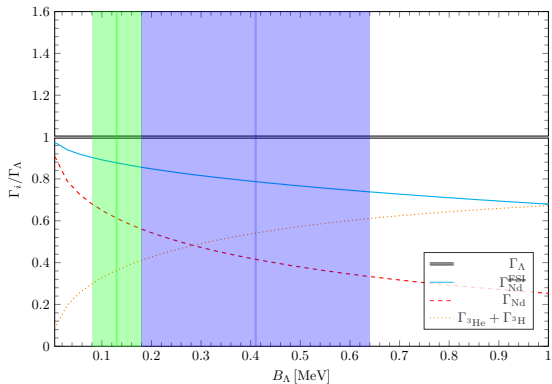


Hypertriton Width and Branching Ratios



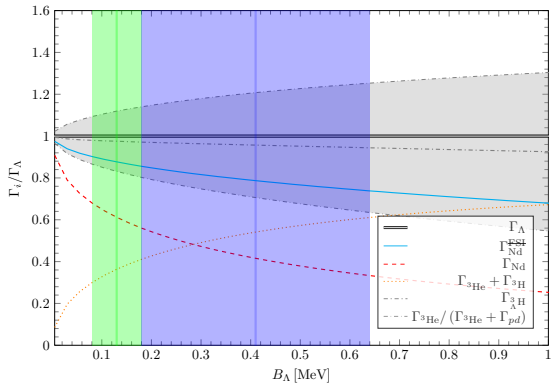


Hypertriton Width and Branching Ratios



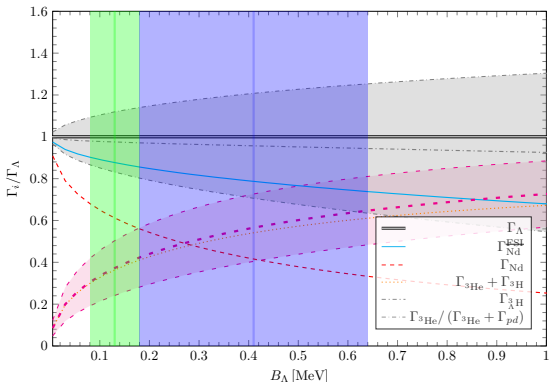


Hypertriton Width and Branching Ratios





Hypertriton Width and Branching Ratios



- $\Gamma_{{}^3_{\Lambda}\text{H}}$ Barely Depends on B_{Λ}
- Final State Interactions are Important
- $\Gamma_{3\text{He}}/(\Gamma_{3\text{He}} + \Gamma_{pd})$ Depends Strongly on B_{Λ}
- STAR Branching ratio 0.32(5)(8)

Emulsion Data: $R = \Gamma_{3\text{He}}/(\Gamma_{3\text{He}} + \Gamma_{pd}) = 0.3 - 0.4$



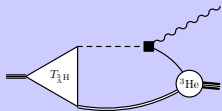
Pionic Final State Interaction

Work by Perez-Obiol and Gal suggest significant contribution from Pionic final states

Perez-Obiol (2020), Gal(2019)

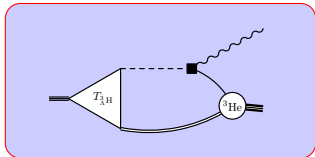
Different Type of calculation only has 2 body decay channel uses Branching ratio as input Contribution $0.10 - 0.15\Gamma_{\Lambda}$

Choose this channel!



- only two particles in FSI
- FSI is momentum locked
- not much data available
- direct comparison possible

Pionic Final State Interaction



Watson-Migdal approach for FSI adds interaction between ${}^3\text{He}$ and π^-

$$\Gamma_{3\text{H}} = \frac{G_F^2 M_\pi^4}{\pi} \frac{\bar{k} M_{3\text{H}}}{M_{3\text{H}} + \omega_{\bar{k}}} \bar{Z}_{3\text{H}}(B_\Lambda) \bar{Z}_{3\text{H}}(B_{3\text{H}}) \left(A_\pi^2 + \frac{1}{9} \left(\frac{B_\pi}{M_\Lambda + m} \right)^2 \bar{k}^2 \right) |l_q(\bar{k}, B_\Lambda)|^2 \int_{\text{Loop}} |g^2 G_{\pi t}(\Delta - m_\pi, 0)|^2$$

with $iG_{\pi t}(\mathbf{p}_0, \mathbf{p}) = \frac{\pi}{\mu_{\pi t} g^2} \frac{-i}{-\gamma_{\pi t} + \sqrt{-2\mu_{\pi t} \left(p_0 - \frac{\mathbf{p}^2}{2(M_\pi + M_{\text{He}})} \right) + i\epsilon}} \Rightarrow \Gamma_{3\text{H}}^{\pi\text{FSI}} = (1 + \text{cor})\Gamma_{3\text{H}}$ cor = 0.06 Maximal

contribution



Hypertriton Width and Branching Ratios

Our Results:

- $\Gamma_{{}^3_{\Lambda}H}(0.13) = (1.03 \pm 0.15)\Gamma_{\Lambda}$
- $\Gamma_{{}^3_{\Lambda}H}(0.41) = (1.03 \pm 0.25)\Gamma_{\Lambda}$
- $R(0.13) = 0.38 \pm 0.05$
- $R(0.41) = 0.57 \pm 0.11$



Hypertriton Width and Branching Ratios

Our Results:

- $\Gamma_{\Lambda}({}^3_{\Lambda}H(0.13)) = (1.03 \pm 0.15)\Gamma_{\Lambda}$
- $\Gamma_{\Lambda}({}^3_{\Lambda}H(0.41)) = (1.03 \pm 0.25)\Gamma_{\Lambda}$
- $R(0.13) = 0.38 \pm 0.05$
- $R(0.41) = 0.57 \pm 0.11$

Consistent:

- Calculation by Congleton for Γ and R
- Calculation by Kamada for Γ and R
- Emulsion Data
 $0.05\text{MeV} \lesssim B_{\Lambda} \lesssim 0.2\text{MeV}$



Hypertriton Width and Branching Ratios

Our Results:

- $\Gamma_{{}^3_{\Lambda}H}(0.13) = (1.03 \pm 0.15)\Gamma_{\Lambda}$
- $\Gamma_{{}^3_{\Lambda}H}(0.41) = (1.03 \pm 0.25)\Gamma_{\Lambda}$
- $R(0.13) = 0.38 \pm 0.05$
- $R(0.41) = 0.57 \pm 0.11$

Slight Tension:

- STAR results Branching ratio
 $R = 0.32 \pm 0.05 \pm 0.08$

Consistent:

- Calculation by Congleton for Γ and R
- Calculation by Kamada for Γ and R
- Emulsion Data
 $0.05\text{MeV} \lesssim B_{\Lambda} \lesssim 0.2\text{MeV}$

Hypertriton Width and Branching Ratios

Our Results:

- $\Gamma_{{}^3_{\Lambda}H}(0.13) = (1.03 \pm 0.15)\Gamma_{\Lambda}$
- $\Gamma_{{}^3_{\Lambda}H}(0.41) = (1.03 \pm 0.25)\Gamma_{\Lambda}$
- $R(0.13) = 0.38 \pm 0.05$
- $R(0.41) = 0.57 \pm 0.11$

Slight Tension:

- STAR results Branching ratio
 $R = 0.32 \pm 0.05 \pm 0.08$

Consistent:

- Calculation by Congleton for Γ and R
- Calculation by Kamada for Γ and R
- Emulsion Data
 $0.05\text{MeV} \lesssim B_{\Lambda} \lesssim 0.2\text{MeV}$

Good part:

- EFT systematic improvement possible
- Go to NLO or three-body

Summary

- Elegant theory with few input parameters
- Branching ratio as results and not as input
- Consistent results with a fundamental deuteron including the full three-body phase space
- Branching ratio favors small binding energies
- Systematic improvement possible in the future