Atomic Parity Violation in Ytterbium

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Atomic PV: important landmarks

- ✓ 1959 Ya. B. Zel'dovich: APV (Neutr. Current)
 ⇒ Opt. Rotation in atoms
- ✓ 1974 M.-A. & C. Bouchiat Z^3 enhancement ⇒ APV observable in heavy atoms
- ✓ 1978-9 Novosibirsk, Berkeley discovery of APV in OR(Bi) and Stark-interf.(□)
- ✓ 1995 Boulder, Oxford, Seattle, Paris APV measured to 1-2% in Cs, Tl, Bi, Pb
- ✓ 1997 Boulder 0.35% measurement, discovery of anapole moment



Prof. Ya. B. Zel'dovich

Parity transformation



Classification of classical variables:

Parity transformation

"Scalars (P=1): Mass, Energy, Time ...

- Scalars \rightarrow Pseudoscalars (P=-1): Helicity ...

Variables

Vectors \longrightarrow Vectors (P=-1): Linear momentum, E-field, Force ...

Pseudovectors (P=1): Angular momentum, B-field ...

Two frontiers in the search

Collider experiments (pp, e⁺e⁻, etc) at higher energies (E >> M_Z)



High energy physics

Indirect searches at lower energies ($E < M_Z$) but high precision



Particle, nuclear & atomic physics

Sources of parity violation in atoms

 Z^0 -exchange between e and nucleus

 \Rightarrow P-violating, T-conserving product of axial and vector currents

$$\hat{h} = -\frac{G}{\sqrt{2}} \sum_{N} \left[C_{1N} \overline{e} \gamma_{\mu} \gamma_{5} e \overline{N} \gamma_{\mu} N + C_{2N} \overline{e} \gamma_{\mu} e \overline{N} \gamma_{\mu} \gamma_{5} N \right]$$



 C_{1n} is by a factor of 10 larger than C_{1p}, C_{2N} leading to a dominance of the time-like nuclear spin-independent interaction (A_e, V_N)

A contribution to APV due to Z^0 exchange between electrons is suppressed by a factor ~1000 for heavy atoms.

Nuclear Spin-Independent (NSI) electron-nucleon interaction

NSI Hamiltonian in non-relativistic limit assuming equal proton and neutron densities $\rho(r)$ in the nucleus: $\hat{h}_W = -\frac{G}{2\sqrt{2}}Q_W\gamma_5\rho(r)$

The nuclear weak charge
$$Q_W$$
 to the lowest order in the electroweak interaction is

$$Q_W = -N + Z(1 - 4\sin^2\theta_W) \approx -N$$

$$\sin^2 \theta_W = 1 - \left(\frac{M_W}{M_Z}\right)^2$$

The nuclear weak charge is protected from strong-interaction effects by conservation of the nuclear vector current. **Thus, APV measurements allows for extracting weak couplings of the quarks and for searching for a new physics beyond SM**

- NSI interaction gives the largest PV effect compared to other mechanisms
- PV interaction is a pseudo-scalar ⇒ mixes only electron states of same angular momentum

NSI interaction and particle physics implications



APV utilizes low-energy system and gives an access to the weak mixing angle, $Sin^2(\theta_W)$, at low-momentum transfer.

- S. G. Porsev, K. Beloy, and A. Derevianko, PRL 2009
- J.L. Rosner, PRD 1999
- V.A. Dzuba, V.V. Flambaum, and O.P. Sushkov, PRA 1997
- J. Erler and P. Langacker, Ph.Lett. B 1999

Isotope ratios and neutron distribution

The atomic theory errors can be excluded by taking ratios of APV measurements along an isotopic chain. While the atomic structure cancels in the isotope ratios, there is an enhanced sensitivity to the neutron distribution $\rho_n(r)$.

$$A_{PV} = \xi_{atomic} (Q_W + Q_W^{nuc})$$

$$Q_W^{nuc} = -N(q_n - 1) + Z(1 - 4\sin^2 \theta_W)(q_p - 1)$$

$$q_n = \int \rho_n(r) f(r) d^3r, \ q_p = \int \rho_p(r) f(r) d^3r$$

f(r) is the variation of the electron wave functions inside the nucleus normalized to f(0)=1.

$$\begin{split} R &= \frac{A_{PV}(N')}{A_{PV}(N)} \approx \frac{Q_W(N')}{Q_W(N)} \Big[1 + \Delta q_n \Big] \\ \Delta q_n &= q_n - q'_n \end{split}$$

R is sensitive to the difference in the neutron distributions.

Amplitude interference: the trick for observing weak interaction in atoms

 $\begin{array}{l} \mathbf{h}_{\mathrm{NSI}} \mbox{ mixes } \mathbf{s}_{1/2} \mbox{ and } \mathbf{p}_{1/2} \mbox{ states of valence electron } \Rightarrow \\ \mathbf{A}_{\mathrm{PV}} \mbox{ of dipole-forbidden transition.} \\ \mbox{ If } \mathbf{A}_{\mathrm{PC}} \mbox{ is also induced, the amplitudes interfere.} \end{array}$

$$R \propto |A_{PC} + A_{PV}|^2 \cong A_{PC}^2 + 2A_{PC}A_{PV} + o(A_{PV}^2)$$

Interference

E-field



E1 PC-amplitude ∝ E

E1-PV interference term is odd in E

Reversing E-field changes transition rate Transition rate $\propto A_{PV}A_{Stark}$

Observing APV in Yb



The population of $6s6p {}^{3}P_{0}$ metastable level is probed by pumping the $6s6p {}^{3}P_{0}$ - $6s7s {}^{3}S_{1} 649$ nm transition. Proposed by D. DeMille, PRL 1995

Pumping rates of the 408-nm transition are detected by measuring the population of the ${}^{3}P_{0}$ state, where 65% of the atoms excited to the ${}^{3}D_{1}$ state decay spontaneously.



PV effect: line-shape signature







Experimental setup



Light collection efficiency: Interaction region: ~0.2% (556 nm)

Detection region: ~25%

Yb density in the beam $\sim 10^{10}$ cm⁻³ E-field up to 15 kV/cm, spatial homogeneity 99% Reversible B-field up to 100 G, homogeneity 99%

Schematic of the optical system



PBC: Asymmetric design Finesse 17000 Power 20 W Locking: Pound-Drever-Hall technique

Light powers: Ar⁺: 12W; Ti:Sapp (816 nm): 1W; Doubler (408 nm): 50 mW



Fast E-modulation scheme: Profiles



Effective integration time: 10 s p-p

Shot noise limited SNR with respect to PV signal ~ $2/\sqrt{\tau(s)}$

 $\Rightarrow 0.1\%$ accuracy in 70 hours

- Lineshape scan: 20 s
- E-field reversal: 14 ms (70 Hz)
- B-field reversal: 20 minutes
- Polarization angle: 10 minutes
- E-field magnitude
- B-field magnitude
- Angle magnitude

PV Amplitude: Current results



 $\zeta/\beta = 39(4)_{\text{stat.}}(3)_{\text{syst.}} \text{ mV/cm} \Rightarrow |\zeta| = 8.7 \pm 1.4 \times 10^{-10} \text{ ea}_0$

Accuracy is affected by HV amplifier noise, fluctuations of stray fields, and laser drifts \rightarrow to be improved

Summary

Completed Work

- ✓ Lifetime Measurements
- ✓ General Spectroscopy (hyperfine shifts, isotope shifts)
- ✓ dc Stark Shift Measurements
- ✓ Stark-Induced Amplitude (β): 2 independent

measurements

- ✓ M1 Measurement (Stark-M1 interference)
- ✓ ac Stark shifts measured
- ✓ Verification of PV enhancement



And then...

- > PV in a string of even isotopes; **neutron distributions**
- > PV in odd isotopes: NSD PV, Anapole Moments

Statistical noise



Fast E-modulation scheme: Systematics

E- and B-field imperfection:

 $E = \tilde{E} + E'$ $\tilde{E} = (\tilde{E}_0 \hat{x} + \tilde{e}_y \hat{y} + \tilde{e}_z \hat{z}) \cos(\omega t)$ $E' = (E_{dc} \hat{x} + e_y \hat{y} + e_z \hat{z})$ $B = \tilde{B} + B'$ $\tilde{B} = (\tilde{b}_x \hat{x} + \tilde{b}_y \hat{y} + B \hat{z})$ $B' = (b'_x \hat{x} + b'_y \hat{y} + b'_z \hat{z})$

Light polarization now includes a small ellipticity:

 $\vec{\varepsilon} = \varepsilon \, \left(\hat{y} \sin \theta + \hat{z} \, e^{i\phi} \cos \theta \right)$

Residual M1 transition: $A_{M}^{(M1)} = M1 (-1)^{M} (\delta \vec{k} \times \vec{\varepsilon})_{-M}$

Normalized-rate modulation amplitudes include additional terms:

$$\frac{R_{\rm M}^{[1]}}{R_{\rm M}^{[2]}} = r_{\rm M}^{\rm (Stark)} + r_{\rm M}^{\rm (PV)} + r_{\rm M}^{\rm (M1)} + r_{\rm M}^{(\phi)}$$

M1- and ϕ -contribution

TABLE I: Lowest-order terms contributing to the normalized transition-rate modulation amplitudes r_M .

	$r_M^{(APV)}$	$r_M^{(\mathrm{M1})}$	$r_M^{(\phi)}$
M = 0	$+ \frac{4 \zeta \cot \theta}{\beta \tilde{E}_0}$	0	0
M = -1	$-rac{4\zeta an heta}{eta ilde{E}_0}$	$+\frac{4\delta k\mathcal{M}(\tilde{e}_y-\tilde{e}_z\tan\theta)}{\beta\tilde{E}_0^2}$	$+rac{4 e_z \phi \tan \theta}{ ilde{E}_0}$
M = +1	$-rac{4\zeta an heta}{eta ilde{E}_0}$	$-\frac{4\delta k\mathcal{M}(\tilde{e}_y-\tilde{e}_z\tan\theta)}{\beta\tilde{E}_0^2}$	$-rac{4 e_z \phi \tan \theta}{ ilde{E}_0}$

$$K = \frac{R_{-1}^{[1]}}{R_{-1}^{[2]}} + \frac{R_{+1}^{[1]}}{R_{+1}^{[2]}} - 2\frac{R_{0}^{[1]}}{R_{0}^{[2]}} = \frac{16 \ \varsigma}{\beta E_{0}}$$

Stark contribution

$$\begin{bmatrix} \mathcal{K}_1 \\ \mathcal{K}_2 \\ \mathcal{K}_3 \\ \mathcal{K}_4 \end{bmatrix} = \frac{1}{4} \begin{bmatrix} -1 & -1 & +1 & +1 \\ -1 & +1 & +1 & -1 \\ +1 & -1 & +1 & -1 \\ +1 & +1 & +1 & +1 \end{bmatrix} \cdot \begin{bmatrix} \mathcal{K}(+B, +\theta) \\ \mathcal{K}(-B, +\theta) \\ \mathcal{K}(+B, -\theta) \\ \mathcal{K}(-B, -\theta) \end{bmatrix}$$

TABLE II: List of the lowest-order terms contributing to the asymmetry \mathcal{K} for $|\theta| = \pi/4$ sorted with respect to their response to the reversals. \mathcal{K}_4 corresponding to a rather long list of terms that are invariant with respect to all reversals, is not shown in the table.

\mathcal{K}_1	\mathcal{K}_2	\mathcal{K}_3
$\frac{8(\tilde{e}_y e_z + \tilde{e}_z e_y)}{\tilde{E}_0^2} + \frac{16\tilde{b}_x e_y}{B\tilde{E}_0} + \frac{16\zeta}{\beta\tilde{E}_0}$	$\frac{16b'_x e_y}{B\tilde{E}_0}$	$\frac{16b'_x e_z}{B\tilde{E}_0}$

Stark contribution measurements



$$e_{y}\left(\frac{\tilde{e}_{z}}{2\tilde{E}_{0}}+\frac{b_{x}}{B}\right)+e_{z}\frac{\tilde{e}_{y}}{2\tilde{E}_{0}}=-2.6 \ (1.6)_{\text{stat}}(1.5)_{\text{syst}} \ \text{mV/cm}$$

Error budget

$$\frac{5}{\beta} = 39 \ (4)_{\text{stat}} (3)_{\text{syst}} \ \text{mV/cm}$$

TABLE IV: List of factors contributing to the systematic uncertainty of the PV parameter, ζ/β .

Factor	Uncertainty (%)
\tilde{E} value:	
geometry	5
numerical modeling	3
E-field imperfections	5
Phase mixing	0.5
Other	1
${\bf Total} \ ({\rm in} \ {\rm quadrature})$	8

Problems

• Photo-induced PBC mirror degradation in vacuum

• Fields imperfection

• Laser stability

Power-buildup cavity design and characterization: schematic



Power-buildup cavity design and characterization



$$F = \frac{2\pi}{T_1 + T_2 + L_1 + L_2}$$
$$\frac{P_{trans}}{\varepsilon P_{in}} = T_1 T_2 \left(\frac{F}{2\pi}\right)^2$$

C. J. Hood, H. J. Kimble, J. Ye. PRA 64, 2001



Power-buildup cavity design and characterization: mirrors

	REO set1	REO set2	ATF	Boulder expt.
	λ =408 nm	λ =408 nm	λ =408 nm	λ =540 nm
Transmission	320 ppm	45; 23 ppm	150 ppm	40; 13
S+A losses	120 ppm	213; 83 ppm	30 ppm	<1 ppm

Mirror set used during the latest APV measurements:

Finesse of 17000 with ATF mirrors

Photodegradation: a factor of 3 increase of S+A losses in 2 runs (~8 hours of exposure with ~10 W of circulating power)

Yb isotopes and abundances

Seven stable isotopes, two have non-zero spin



C.J. Bowers et al, PRA 1999

Sources of NSD interaction

$$\hat{h}_{NSD} = \frac{G}{\sqrt{2}} \frac{\kappa}{I} \gamma_0 \gamma \mathbf{I} \ \rho(\vec{r})$$

Anapole moment



Weak neutral current



Hyperfine correction to the weak neutral current



$$\kappa = \frac{K}{I+1} \kappa_A + \kappa_2 + \kappa_{Q_w};$$

K = (-1)^{I+1/2-l} (I+1/2)

$$\kappa_A \approx 1.15 \cdot 10^{-3} A^{2/3} \mu_\alpha g_\alpha; A = N + Z$$

 $\kappa_2 = \frac{1/2 - K}{I + 1} C_{2\alpha}$

 κ_A -Anapole moment κ_2 -Neutral currents κ_{QW} -Radiative corrections

Anapole moment

In the nonrelativistic approximation PNC interaction of the valence nucleon with the nuclear core has the form:

n(r) is core density and g_{α} is dimensionless effective weak coupling constant for valence nucleon.



$$\hat{h}_A \propto \frac{G g_{\alpha}}{2\sqrt{2}} \frac{(\mathbf{\sigma}\mathbf{p})}{m_p} n(\vec{r})$$

- As a result, the spin σ acquires projection on the momentum p and forms spin helix
- Spin helix leads to the toroidal current. This current is proportional to the magnetic moment of the nucleon and to the cross section of the

core.

Khriplovich & Flambaum

$$\kappa_A \approx 1.15 \cdot 10^{-3} A^{2/3} \mu_\alpha g_\alpha$$

<u>**neutron**</u>: μ_n =-1.2; g_n =-1 <u>**proton**</u>: μ_p =3.8; g_p =5

Anapole moment is bigger for nuclei with unpaired <u>proton</u>

Nuclear physics implication: weak meson coupling constants

There are 7 independent weak couplings for π -, ρ -, and ω -mesons known as DDH constants. Proton and neutron couplings, g_{α} , can be expressed in terms of 2 combinations of these constants:

$$g_{p} = 8.0 \times 10^{4} \left[70f_{\pi} - 19.5h^{0} \right]$$
$$g_{n} = 8.0 \times 10^{4} \left[-47f_{\pi} - 18.9h^{0} \right]$$

$$f_{\pi} \equiv f_{\pi}^{1} - 0.12h_{\rho}^{1} - 0.18h_{\omega}^{1}$$
$$h^{0} \equiv h_{\rho}^{0} + 0.7h_{\omega}^{0}$$

At present the values of the coupling constants are far from being reliably established. The projected measurement of the anapole moment in ¹⁷³Yb should provide an important constraint.



PV effect on line shapes: odd isotopes



$$\vec{E} = (E,0,0)$$

$$\vec{\varepsilon} = (0,\sin\theta,\cos\theta)$$

$$R^{center} = \frac{\beta_{FF'}^2 E^2}{6} (4\sin^2\theta + \cos^2\theta) + E \beta_{FF'} \varsigma' \sin\theta \cos\theta$$

$$R^{side} = \frac{\beta_{FF'}^2 E^2}{2} \cos^2\theta - E \beta_{FF'} \varsigma' \sin\theta \cos\theta$$

¹⁷¹Yb



 $\zeta^{NSD} \approx 10^{-12} \text{ ea}_0 \text{ for}$ odd Yb isotopes $\zeta = 10^{-9} \text{ ea}_0$ $\zeta^{\text{must be}}$ measured with 0.1% accuracy

 $\varsigma' = \varsigma + \left\langle \vec{I} \cdot \vec{J} \right\rangle$

NSD