

Theory of Electric Dipole Moments: A (theorists) motivation for JEDI

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Outline of this talk

Part I: What are EDMs and why are they interesting in the first place ?

Part II: EDMs of nucleons and (light) nuclei

Part III: Unraveling models of CP violation









- Electroweak CP-violation
- Nobel prize for predicting third generation



Highly Suppressed



Electroweak CP-violation



5 to 6 orders **below** upper bound \longrightarrow **Out of reach!**

I.B. Khriplovich, S.K. Lamoreaux, CP Violation Without Strangeness, Springer, 1997



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- Second source: QCD theta-term
- Due to complicated vacuum structure of QCD



E Gauge field



- Second source: QCD theta-term
- Due to complicated vacuum structure of QCD





• Causes a 'new' CP-violating interaction with coupling constant θ

$$\theta \,\varepsilon^{\mu\nu\alpha\beta}G_{\mu\nu}G_{\alpha\beta}$$
 (in QED ~ $\vec{E}\cdot\vec{B}$)

• Size of θ is **unknown**



Theta Term Predictions



Sets θ upper bound: $\theta < 10^{-10}$

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"the poor man's high-energy physics" (S. Lamoreaux)



Problem of the Universe Matter/Anti-Matter



Asymmetry

13.7 billion years



Observed: Expected:

$$\frac{n(b)}{n(\gamma)} \approx 10^{-9}, \quad n(\overline{b}) \approx 0$$
$$\frac{n(b)}{n(\gamma)} \approx \frac{n(\overline{b})}{n(\gamma)} \approx 10^{-18}$$

Sakharov Conditions

- Baryon number violation
 - $X \twoheadrightarrow Y + B$
- C- and CP-violation

$$\Gamma(X \twoheadrightarrow Y + B) \neq \Gamma(\overline{X} \twoheadrightarrow \overline{Y} + \overline{B})$$

• Out of thermal equilibrium

$$\Gamma(X \to Y + B) \neq \Gamma(Y + B \to X)$$

Requires more CP-violation







Why are EDMs interesting to measure?

A search for new physics which is *'background free'* Many beyond-the-SM models predict large EDMs: Complementary to LHC search Matter/Antimatter asymmetry requires more CPV: EDMs are excellent probes



• New neutron EDM experiments at ILL, SNS, PSI, TRIUMF

current

Baker *et al PRL* '06 (ILL)
$$d_n = (0.2 \pm 1.5(stat) \pm 0.7(sys)) \cdot 10^{-26} e cm$$

proposed

 $\sim 10^{-28} \ e \ cm$



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• Proton EDM inferred from diamagnetic atoms

Griffith et al PRL '09 (UW)

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$$d(^{199}Hg) \le 3.1 \cdot 10^{-29} \ e \ cm \quad (95\% \ C.L.)$$

Dmitriev + Sen'kov PRL '03
$$d_p \le 7.9 \cdot 10^{-25} \ e \ cm$$

Ongoing experiments on Ra, Rn, Xe....



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Ongoing experiments on Ra, Rn, Xe....

• Electron EDM from ThO molecule:

 $d_e \le 9 \cdot 10^{-29} \ e \ cm$



• New kid on the block: Charged particle in storage ring

Anomalous magnetic

$$\frac{d\vec{S}}{dt} = \vec{S} \times \vec{\Omega} \qquad \vec{\Omega} = \frac{q}{m} \left[a\vec{B} + \left(\frac{1}{v^2} - a\right)\vec{v} \times \vec{E} \right] + 2d\left(\vec{E} + \vec{v} \times \vec{B}\right)$$

Bennett et al (BNL g-2) PRL '09

Farley et al PRL '04

• Limit on muon EDM $d_{\mu} \le 1.8 \cdot 10^{-19} \ e \ cm \ (95\% \ C.L.)$



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Limit on muon EDM
$$d_{\mu} \le 1.8 \cdot 10^{-19} \ e \ cm \ (95\% \ C.L.)$$

 Proposals to measure EDMs of proton and deuteron at level

Other light nuclei? 3He?

$$\sim 10^{-29} \ e \ cm$$

COSY @ Jülich Brookhaven/Fermilab

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lacksquare



Not really background free.....

Measurement of a Hadronic/nuclear EDM

New sources of **Standard Model: CP-violation θ**-term High-energy model?



Finding the **Source**



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Questions :

Do **different** models of CP-violation leave behind a **different** 'EDM-footprint'



Can we **pinpoint** the microscopic source of CP-violation from **EDM measurements**?







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Lower and lower energies



• After integrating out new physics (whatever it is) at low energies:

~ **1 GeV**
$$L = L_{QCD} + \frac{\theta}{32\pi^2} G_{\mu\nu} \tilde{G}^{\mu\nu} + \frac{1}{M_{CP}^2} \sum O^{(6)}$$

Effective CP-odd operators: They encode Beyond-the-SM physics.

• **Different** BSM-models produce **different** effective operators

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Effective CP-odd operators:

They encode Beyond-the-SM physics.

- **Different** BSM-models produce **different** effective operators
- At lower energies: QCD becomes nonperturbative



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Chiral effective field theory



• Use the symmetries of QCD to get chiral Lagrangians

$$L_{QCD} \rightarrow L_{chiPT} = L_{\pi\pi} + L_{\pi N} + L_{NN} + \cdots$$

• Massless QCD Lagrangian has a global *SU(2)xSU(2)* symmetry spontaneously broken to *SU(2)*

$$q \rightarrow \left(e^{i\vec{\theta}_V \cdot \vec{\tau} + i\vec{\theta}_A \cdot \vec{\tau} \gamma^5} \right) q \qquad q = (u \ d)^T$$

• Pions are the corresponding **Goldstone** bosons (small pion mass due to small quark mass)



Chiral effective field theory

$$L_{QCD} \rightarrow L_{chiPT} = L_{\pi\pi} + L_{\pi N} + L_{NN} + \cdots$$

- The chiral Lagrangian can be constructed order by order
- Form of interactions **fixed by symmetry** considerations
- Each interaction associated with unknown LEC (needs to be fitted or from lattice)
- Provides a **perturbative** expansion in $\frac{Q}{\Lambda}$

$$Q/_{\Lambda_{\chi}} \quad \Lambda_{\chi} \cong 1 \, GeV$$

Weinberg, Gasser, Leutwyler, Meißner, Kaiser, Bernard, van Kolck, Epelbaum....

CP-violation in chiPT



• Repeat the exercise with the **CP-odd operators included**:

$$L = L_{QCD} + \frac{\theta}{32\pi^2} G_{\mu\nu} \tilde{G}^{\mu\nu} + \frac{1}{M_{CP}^2} \sum O^{(6)}$$

Different models of CP-violation (theta, SUSY, Left-Right, multi-Higgs,....)



For now: keep it general



• The CP-odd terms induce **CP-odd hadronic interactions**:



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Different models of CP-violation (theta, SUSY, Left-right, multi-higgs,....)

Predict a different hierarchy between these 7 terms !

Goal: probe these hierarchies experimentally

The Nucleon EDM



• Calculate from the chiral Lagrangians



$$d_{n} = \overline{d}_{0} - \overline{d}_{1} + (0.13 + 0.01) \ \overline{g}_{0} \ e \ fm$$
$$d_{p} = \overline{d}_{0} + \overline{d}_{1} - (0.13 + 0.03) \ \overline{g}_{0} \ e \ fm$$

Crewther et al., PLB '79 Pich, Rafael, NPB '91

Hockings, van Kolck, PLB '05 Ottnad et al, PLB '10

JdV, Mereghetti et al, PLB '11 '14

The Nucleon EDM







Hard to probe the hierarchy with only neutron and proton EDMs

Crewther et al., PLB '79 Pich, Rafael, NPB '91 Hockings, van Kolck, PLB '05 Ottnad et al, PLB '10 JdV, Mereghetti et al, PLB '11 '14 Mei

Proton EDM still important!



- 1) Potential high accuracy ! $\sim 10^{-29} e cm$
- 2) Test for the QCD theta term. With lattice input for LECs

$$d_{n} = (2.7 \pm 1.2) \cdot 10^{-16} \,\overline{\theta} \, e \, cm$$
$$d_{p} = -(2.1 \pm 1.2) \cdot 10^{-16} \,\overline{\theta} \, e \, cm$$

Shintani '12 '13 Guo, Meißner '13 '14

Could provide **strong hint** for theta term. But..... No lattice data for other CPV scenarios

3) **Crucial** input for EDMs of nuclei !

Nuclear EDMs



• Nuclear EDMs: tree-level dependence !



- No loop suppression and no counter terms!
- Possible to calculate light-nuclear EDMs with high accuracy!

EDM of a general light nucleus

EDM of a nucleus with A nucleons can be separated in 2 contributions



JdV et al '11 Bsaisou et al '12 Song et al '13

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One-body:

$$d_D = d_n + d_p$$

T-violating pion-exchange

$$L = \overline{g}_0 \overline{N} (\vec{\pi} \cdot \vec{\tau}) N + \overline{g}_1 \overline{N} \pi_3 N$$

Khriplovich+Korkin NPA '00 Liu+Timmermans PRC '04 JdV et al PRL '11 Bsaisou et al '12





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Deuteron is a special case due to N=Z

$${}^{3}S_{1} \xrightarrow{\overline{g}_{0}} {}^{1}P_{1} \xrightarrow{\gamma} {}^{3} \underbrace{\overline{g}_{1}} {}^{3}S_{1} \xrightarrow{\overline{g}_{1}} {}^{3}P_{1} \xrightarrow{\gamma} {}^{3}S_{1}$$

Khriplovich+Korkin NPA '00 Liu+Timmermans PRC '04 JdV et al PRL '11 Bsaisou et al '12



Bsaisou et al, in prep

Obtain deuteron wave function from chiral EFT potential

$$(E - H_{PT}) | \Psi_A > = 0$$

$$(E - H_{PT}) | \tilde{\Psi}_A > = V_{CP} | \Psi_A >$$
Both consistently derived in chiral EFT

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Obtain deuteron wave function from chiral EFT potential



Do the same for 3He and 3H



No isospin filter in these nuclei, both g0 and g1 dependence

$$d_{3He} = 0.9 d_n - 0.05 d_p + \left[(0.14 \pm 0.03) \overline{g}_1 + (0.10 \pm 0.03) \overline{g}_0 \right] e fm$$

$$d_{3H} = -0.05 d_n + 0.9 d_p + \left[(0.14 \pm 0.03) \overline{g}_1 - (0.10 \pm 0.03) \overline{g}_0 \right] e fm$$

Still good accuracy, can most likely be improved by using N3LO

Stetcu et al, PLB '08 JdV et al, PRC '11 Song et al, PRC '13 Bsaisou et al, in prep

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³H probably not a candidate for JEDI



Stetcu et al, PLB '08 JdV et al, PRC '11 Song et al, PRC '13 Bsaisou et al, in prep

What would this tell us ?



- From measurements of dn, dp, dD, and/or d3He we can:
 - 1) Extract the (relative size of) the couplings $\overline{g}_1 \quad \overline{g}_0 \quad (\overline{\Delta}_{\pi})$
 - 2) The size of the two- and three-body contributions, e.g.

$$\left|\frac{d_D}{d_p}\right| \qquad \left|\frac{d_D - d_n - d_p}{d_n + d_p}\right| \qquad \left|\frac{d_{3He}}{d_p}\right| \qquad \left|\frac{d_{3He}}{d_n}\right|$$

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$$\left|\frac{d_D}{d_p}\right| \qquad \left|\frac{d_D - d_n - d_p}{d_n + d_p}\right| \qquad \left|\frac{d_{3He}}{d_p}\right| \qquad \left|\frac{d_{3He}}{d_n}\right|$$

- These quantities are very **indicative** of the CP-odd source
- What about heavy nuclei ?

Traditional EDMs



• Why can't we get this info from EDMs of Hg, Ra, Rn....??

Strong bound on atomic EDM: d_1

$$d_{199}_{Hg} < 3.1 \cdot 10^{-29} \ e \ cm$$

Griffiths et al, PRL '09

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• The atomic part of the calculation is well under control

$$d_{199}_{Hg} = (2.8 \pm 0.6) \cdot 10^{-4} S_{Hg} e fm^2$$
 Dzuba et al, PRA '02, '09

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The atomic part of the calculation is well under control

$$d_{199}_{Hg} = (2.8 \pm 0.6) \cdot 10^{-4} S_{Hg} e fm^2$$
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But the nuclear part isn't.....

$$S_{199}_{Hg} = \left[(0.3 \pm 0.4) \overline{g}_0 + (0.4 \pm 0.8) \overline{g}_1 \right] e fm^3$$

Engel et al, PPNP '13

• There is no **power counting** for nuclei with so many nucleons



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Big questions :

Do **different** models of CP-violation leave behind a **different** 'EDM-footprint'



Can we **pinpoint** the microscopic source of CP-violation from **EDM measurements**?

Unraveling models of CPV



- In recent work we studied 4 popular scenarios of CP-violation
 - 1) Standard Model including QCD theta term
 - 2) The minimal left-right symmetric model

Mohapatra et al '08

3) The aligned two-Higgs-Doublet model

Pich & Jung '13

- 4) The MSSM (well, specific versions of it)
- Can we **unravel** these models using **JEDI** experiments?

Dekens, JdV, Nogga, et al, JHEP '14



1) We first look at the QCD theta term

$$L = L_{QCD} + \frac{\theta}{32\pi^2} G_{\mu\nu} \tilde{G}^{\mu\nu}$$
Axial U(1) transformation
$$\overline{m} = (m_u + m_d)/2$$

$$L = L_{QCD} + i \frac{\overline{m}}{2} \theta \ \overline{q} i \gamma^5 q$$
a CP-odd quark mass Isospin-symmetric!!

Leads to a very **specific** hadronic CP-odd Lagrangian









$$\frac{g_1}{\overline{g}_0} = -(0.2 \pm 0.1) \qquad \qquad \overline{\Delta}_{\pi} \qquad \text{Too small to matter !}$$



- 2) Now the minimal left-right symmetric model Mohapatra et al '08
 - Based on unbroken Parity symmetry at high energies
 - Gauge group: $SU_R(2) \times SU_L(2) \times SU_c(3) \times U(1)$
 - Additional Higgs fields to break SU_R(2)
 - Additional heavy right-handed gauge bosons W_R⁺⁻ and Z_R



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CP-odd **isospin-breaking** four-quark operator



2) Now the minimal left-right symmetric model



Completely opposite behavior with respect tot theta term

$$\frac{g_0}{\overline{g}_1} = -(0.02 \pm 0.01) \qquad \qquad \overline{\Delta}_{\pi} \qquad \text{Leading order interaction!}$$

Dekens, JdV, Nogga, et al, JHEP '14









Deuteron EDM, sensitive mainly to \overline{g}_1

 $d_D = d_n + d_p + [(0.18 \pm 0.02) \overline{g}_1 + (0.0028 \pm 0.0003) \overline{g}_0] e fm$

$$\left|\frac{d_D - d_n - d_p}{d_n + d_p}\right| < 1$$

$$\left|\frac{d_D - d_n - d_p}{d_n + d_p}\right| > 1$$
Rather big uncertainty
$$d_D - d_n - d_p \cong \frac{d_n}{6}$$

$$d_D - d_n - d_p \cong (3 - 10) d_n$$
(5)





3He EDM, sensitive to \overline{g}_1 and \overline{g}_0 $d_{_{3He}} = 0.9 d_n - 0.05 d_p + [(0.14 \pm 0.03) \overline{g}_1 + (0.10 \pm 0.03) \overline{g}_0] e fm$

$$d_{3He} - 0.9d_n \cong \frac{d_n}{2} \cong 3 d_D$$

$$d_{^{3}H\!e}-0.9d_{_{n}}\cong0.7~d_{_{D}}$$





3He EDM, sensitive to \overline{g}_1 and \overline{g}_0 $d_{_{3He}} = 0.9 d_n - 0.05 d_p + [(0.14 \pm 0.03) \overline{g}_1 + (0.10 \pm 0.03) \overline{g}_0] e fm$

$$d_{3He} - 0.9d_n \cong \frac{d_n}{2} \cong 3 d_D$$



Unraveling models of CPV



- EDMs of nucleons and light nuclei can **identify** the theta term
- It can also provide strong hints for other models:
 e.g. left-right symmetric models

Dekens, JdV, Nogga, et al, JHEP '14

Unraveling models of CPV



- EDMs of nucleons and light nuclei can **identify** the theta term
- It can also provide strong hints for other models: e.g. left-right symmetric models
- Multi-Higgs and the MSSM leave different hierarchies behind

$$\left|\frac{\overline{g}_1}{\overline{g}_0}\right| \cong 1$$

- And give rise do different **electron/nucleon EDM ratio**
- JEDI could tell us a lot about high-energy physics !

Conclusion/Summary



- 1) EDMs are very good probes of new CP-odd physics
- 2) Probe **similar energy scales** as LHC, strong bounds on new physics
- 3) However, if one EDM is measured: **not clear** what is responsible

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The motivation for JEDI (for me at least!)

- 1) Potential for very high accuracy
- 2) The **light nuclear EDMs** are:

Simple enough to be well under control...... But, complex enough to get non-trivial info on CP-odd source



 $\sim 10^{-29} e cm$

