



### 6<sup>th</sup> Georgian – German School and Workshop in Basic Science

# Spin-tracking studies for EDM search in storage rings

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Tbilisi State University, July 7<sup>th</sup> 2014

### Matter-antimatter asymmetry

Big Bang Theory: initial symmetric configuration of the universe

BARYOGENESIS



#### Sakharov's conditions (1967):

- $B = n_b n_{\overline{b}}$  violation
- Departure from thermal equilibrium
- C and CP violation

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Matter-dominated universe: Baryon-to-photon ratio  $n_b/n_v$ 

Observed (PLANCK) 6.08(14)x10<sup>-10</sup> SM expected value

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#### Standard Model (SM):

- Contains the 3 elements
- Does not account for baryon asymmetry
- CP-violation source is too small

#### STANDARD MODEL

Electro-Weak interaction

Source: CKM matrix (quark-flavor mixing): Complex phase  $\delta$ 3 quark flavor mixing angles

Observed in K<sup>0</sup> (1964) and B<sup>0</sup> (2001) systems

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- Several proposed models
- New CP-violating sources

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#### **Theoretical predictions**

SM  $\left| d_{e}^{SM} \right| < 10^{-38} e \cdot cm$   $\left| d_{N}^{SM} \right| < 10^{-32} e \cdot cm$ 

#### Models beyond SM

predict EDM values that are close to the sensitivity of current and future experiments

(UNOBSERVABLE)



### Searching EDM: Neutral systems

Basic idea: apply E-field and look for the energy shift  $-\vec{d}\cdot\vec{E}$ 

• Precession frequency in B and E field (spin ½):

$$\hbar\omega_{\pm} = -2\vec{\mu}\cdot\vec{B} \mp 2\vec{d}\cdot\vec{E}$$

- 2 cases: E parallel and antiparallel to B
- Subtracting the 2 frequencies cancels out the magnetic term:

$$d = \frac{\hbar \Delta \omega}{4E}$$

#### First experiment: Purcell and Ramsey (1951) searched for neutron EDM

Particle/Atom	Current EDM limit (e∙cm)	Future Goal (e∙cm)
Neutron	<2.9x10 <sup>-26</sup>	~10 <sup>-28</sup>
<sup>199</sup> Hg	<3.1x10 <sup>-29</sup>	~10 <sup>-29</sup>
<sup>205</sup> Tl	<9x10 <sup>-25</sup>	~10 <sup>-28</sup> - 10 <sup>-31</sup>
Proton	<7.9x10 <sup>-25</sup>	~10 <sup>-29</sup>
Deuteron		~10 <sup>-29</sup>

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• External E-field produces a torque on the EDM:

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• Freeze the horizontal spin precession and watch for the development of a vertical component

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Spin precession in the vertical plane





### The frozen spin method

 $\vec{\omega}_{s}$ 

 $\vec{\omega}_{c}$ 

#### **BMT Equation**

$$\vec{\omega}_G = \vec{\omega}_s - \vec{\omega}_c = -\frac{q}{m} \left\{ G\vec{B} + \left[ G - \left(\frac{m}{p}\right)^2 \right] \frac{\vec{\beta} \times \vec{E}}{c} \right\}$$

- spin precession frequency in the horizontal plane
- particle revolution frequency

 $G = \left(\frac{g-2}{2}\right)$  anomalous magnetic moment

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Spin along the momentum vector

• **Protons**  $G = 1.79 > 0 \rightarrow$  magic momentum:

$$G - \left(\frac{m}{p}\right)^2 = 0 \implies p = \frac{m}{\sqrt{G}} = 0.7 \frac{GeV}{c}$$

 $\vec{B} = 0 \rightarrow$  pure electric ring!

• **Deuterons**  $G = -0.14 < 0 \rightarrow$  no magic momentum: magnetic field with a radial outward electric field



### Storage ring projects



R. Talman

#### EDM with E and B-fields at COSY



A. Lehrach









At injection spin vectors aligned





At injection spin vectors aligned



After some time the spin vectors are all out of phase in the horizontal plane



in the horizontal plane

### SCT tests at the COoler SYnchrotron (FZJ)



- Momentum p < 3.7 GeV/c
- Circumference: 183 m
- Polarized protons and deuterons
- Manipulation of beam size and polarization

Dedicated SCT studies at the COSY facility

Supported with a spin tracking code: COSY-INFINITY

#### GOAL:

## Benchmark the COSY-INFINITY code against the EDM feasibility tests performed at the COSY storage ring

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WORK PLAN:

Simulation of beam and spin dynamics in the COSY storage ring:

- Spin tune calculation
- Contribution of synchrotron and betatron oscillations to the spin tune spread
- Estimation of the SCT
- RF cavity compensation
- Correction with sextupoles

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- Repetitive system: only a one turn map has to be computed: this makes it much faster than ray tracing codes that trace each individual particle through the system
- Only after successful benchmarking, the code can be used for designing an innovative dedicated ring for EDM measurements

### Spin Tune and Spin Coherence Time

#### SINGLE PARTICLE

• The spin tune  $\nu = G\gamma$  is the number of revolutions of the spin vector around the spin invariant axis in one turn

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#### **BEAM OF PARTICLES**

- Particles with different displacements (Δx, Δy, Δp/p) have different spin tunes spin tune spread Δν
- It is related to the spin coherence time:

$$au_{\rm SC} \propto 1/|\Delta \nu|$$

### Spin tracking: Reference Particle

- Deuterons with p = 970 MeV/c
- Cyclotron frequency f<sub>cyc</sub>
- Motion on the reference orbit: it goes through the center of all magnets



$$\Delta x = \Delta y = 0$$
 ;  $\Delta p/p = 0$ 



#### Longitudinal motion

Momentum dispersion in the beam  $\longrightarrow$  Particles with  $\Delta p/p = (p' - p)/p \neq 0$ 

Different velocities  $\longrightarrow$  Different G $\gamma$ 

#### Longitudinal motion



#### Longitudinal motion



#### SYNCHROTRON OSCILLATIONS

#### Longitudinal motion



Longitudinal motion

$$\Delta \boldsymbol{\nu} = \langle \boldsymbol{\nu} \rangle - \langle \boldsymbol{\nu}_{\mathsf{RP}} \rangle$$

RF OFF:

\_Δ**ν** ∝ Δp/p



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#### **Transverse motion**





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• The RF cavity keeps all particles on average isochronous:



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#### **Simulations**

Scaling using the beta functions:

 $\Delta x_{exp} = 5 \text{ mm}$  $\tau_{exp} = 11.4 \text{ s}$ 

(Ed Stephenson's note on SCT)

 $\epsilon \beta_x = (\Delta x)^2 \Rightarrow \Delta x_{COSY} = \sqrt{\frac{\beta_{x(exp)}}{\beta_{x(COSY)}}} \Delta x_{exp} = 2.73mm$ 

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![](_page_53_Figure_1.jpeg)

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#### Simulated SCT comparable to the measured one

### **Compensation of the Betatron Motion**

• Use of the sextupoles families in the arcs to cancel the spin tune spread due to the betatron motion

![](_page_54_Figure_2.jpeg)

### Simulation of the sextupoles effect

![](_page_55_Figure_1.jpeg)

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![](_page_56_Figure_1.jpeg)

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![](_page_57_Figure_1.jpeg)

![](_page_58_Figure_1.jpeg)

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![](_page_60_Figure_1.jpeg)

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![](_page_61_Figure_1.jpeg)

- The zero-crossing point is independent of the chosen  $\Delta x$  value
- Factor ~7 between simulated and measured k<sub>2</sub> values, suggesting the presence of unaccounted-for sextupole components in the ring

### Linearity check

Combining two sextupole families it is possible to correct also the vertical offset's effect:

![](_page_62_Picture_2.jpeg)

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![](_page_64_Figure_2.jpeg)

- The two straight lines cross each other simultaneous compensation is possible
- Due to acceptance problems of the COSY ring, no data for the vertical offset case will be available

- EDM is a high sensitive probe of new physics
- New frontier: search of charged particles EDM in storage rings
- EDM experiment demands SCT >  $10^3$  s
- Feasibility tests performed at the COSY storage ring
- **COSY-INFINITY** code benchmarked against these tests:

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Promising tool for the design of a new generation of storage rings to be used for EDM search

KHANK YOU FOR THE ATTENTION