

Exotic Atoms

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GGSWBS'12, Tbilisi, Georgia

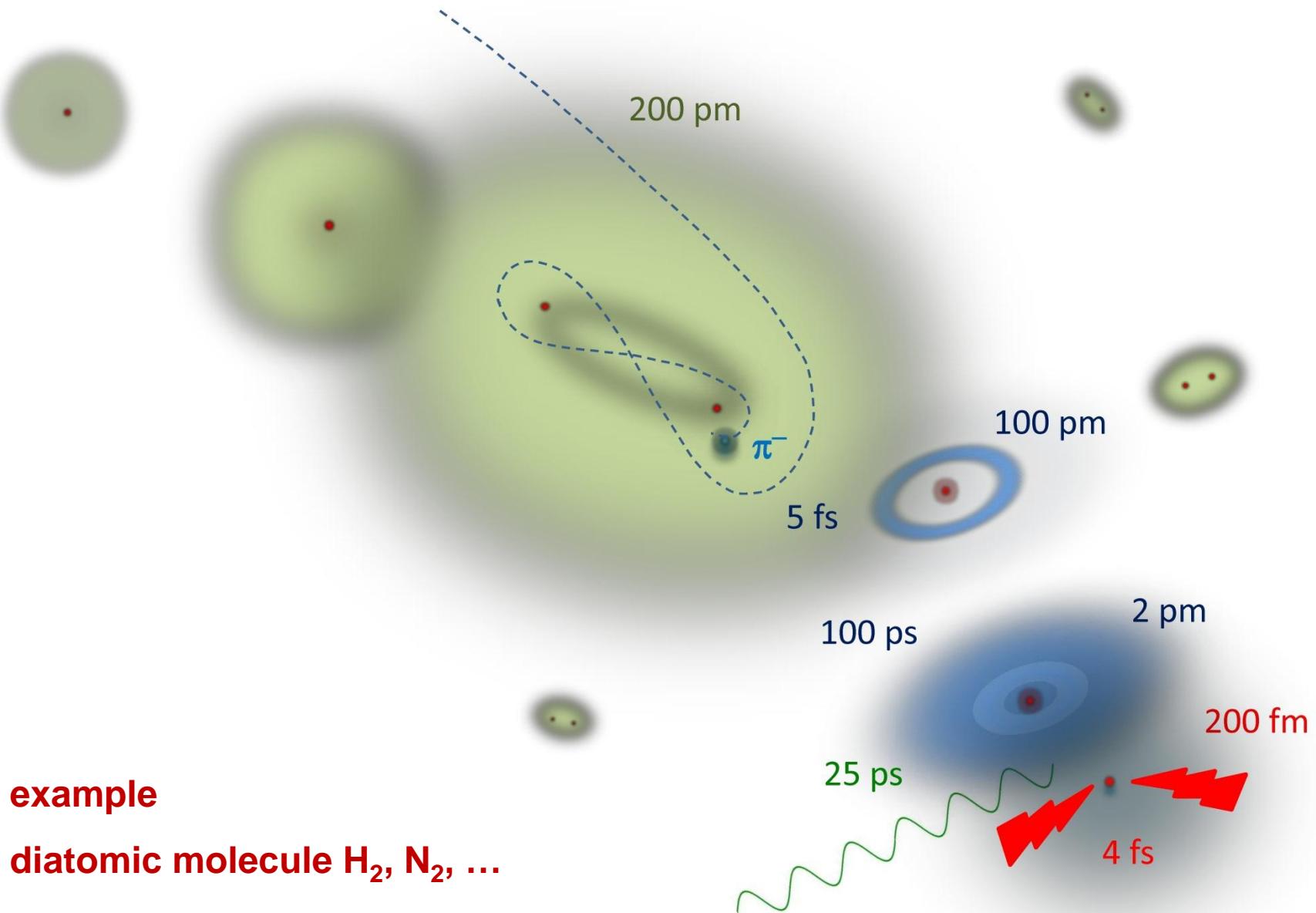
5th Georgian – German School and Workshop in Basic Science

August 9, 2012

- EXOTIC ATOM
- HISTORY
- EXPERIMENT *3 items*
- PHYSICS POTENTIAL *5 examples*

EXOTIC ATOM

Replace electrons by heavier negatively charged particles



example

diatomic molecule H_2 , N_2 , ...

HISTORY

- *Prediction*

1947

$\tau_{\text{capture}} \ll \tau_{\text{meson}}$

Fermi & Teller

- *First X-ray experiment*

1952

pion

π^- C

Nal

1953

muon

..., μ^- Pb *fine structure splitting* ,...

Nal

1965

kaon

K $^-$ He

prop. counter

1969/70

sigma

Σ^- S, Σ^- K

Ge(Li)

1970

antiproton \bar{p} Tl

Ge(Li)

- *FACILITIES*

1974 ...

pions, muons

Paul-Scherrer-Institut (PSI), *TRIUMF, LAMPF*

1983-1996

antiprotons

Low-Energy-Antiproton-Ring *LEAR, AD*

kaons

no dedicated KAON facility yet @KEK, DAΦNE

(X-ray) spectroscopy

- Nal(Tl)
- dedicated semiconductor detectors
- crystal spectrometers
- laser excitation

| | |
|---------------------------------|------------------------|
| 1952 | $\Delta E/E = 30\%$ |
| 1985 ... | $\Delta E/E = 2\%$ |
| 1985 π , 1994 \bar{p} ... | $\Delta E/E = 10^{-4}$ |
| 1996 ... | $\Delta E/E = 10^{-6}$ |

$\Delta E/E$

30%

2%

10^{-4}

10^{-6}

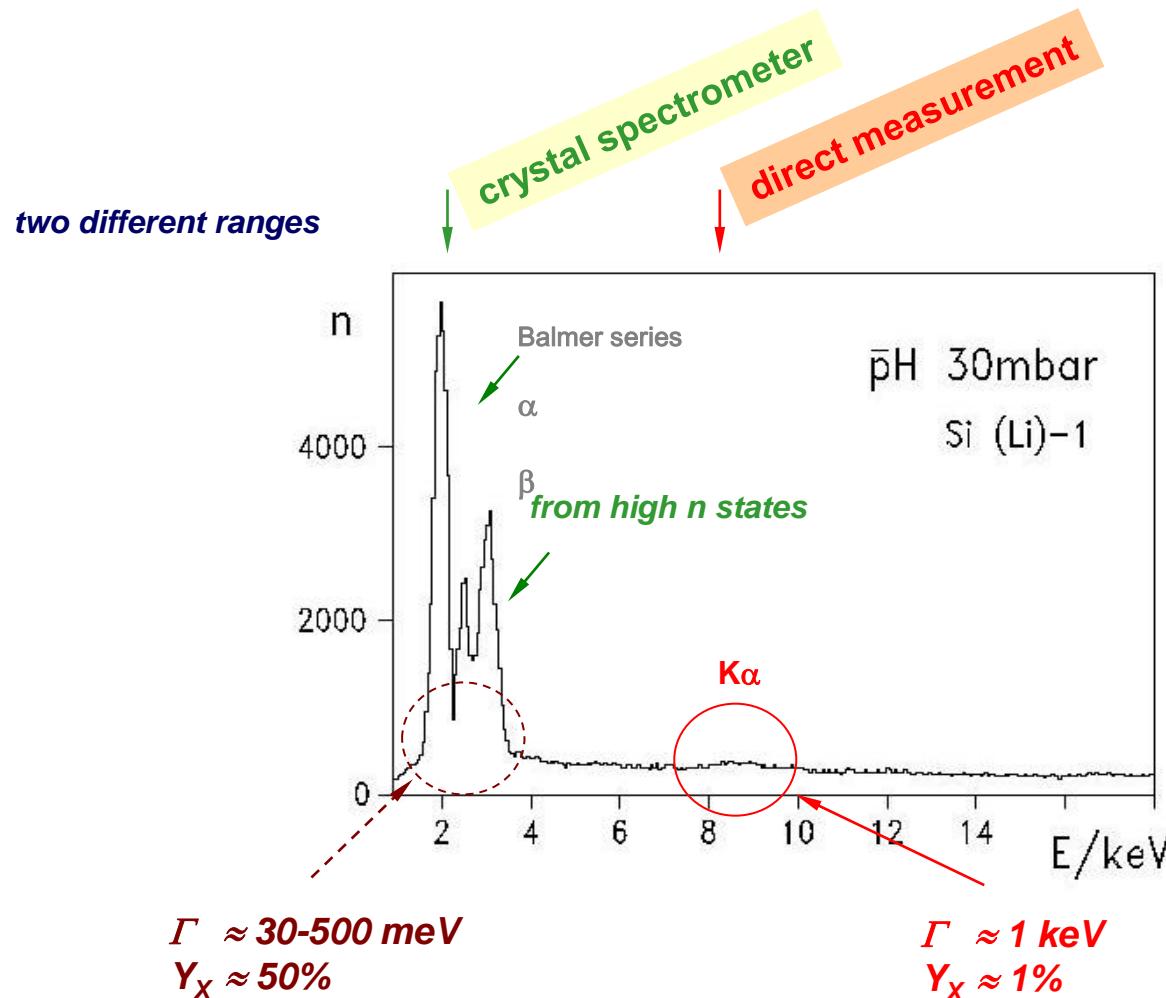
energy resolution

WARM UP:

any X-RAY SPECTRUM

ANTIPROTONIC HYDROGEN

Lyman and Balmer series



PS175: K. Heitlinger et al., Z. Phys. A 342 (1992) 359

EXPERIMENT I

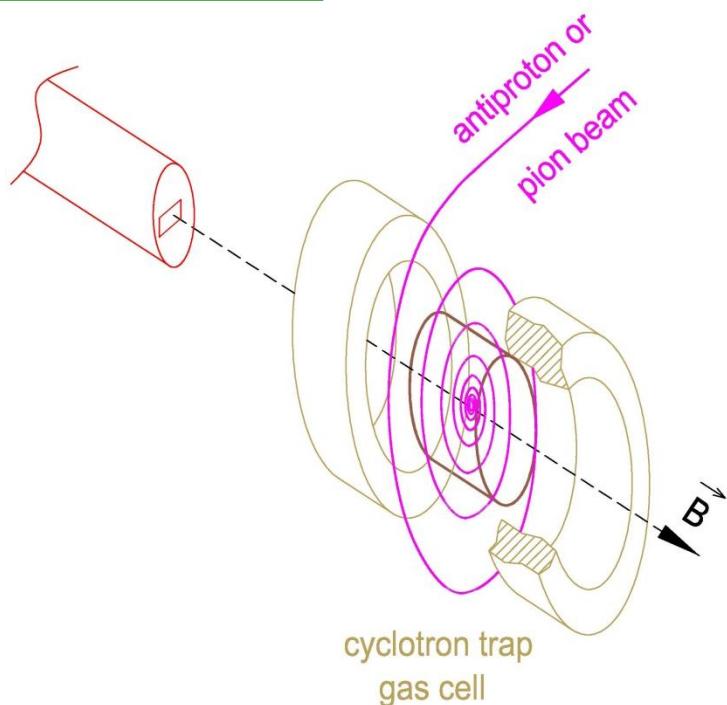
How to produce a suitable amount of exotic atoms?

CYCLOTRON TRAP

concentrates particles

super-conducting split coil magnet

X-ray detector



"wind up" range curve

in (weakly) focusing magnetic field

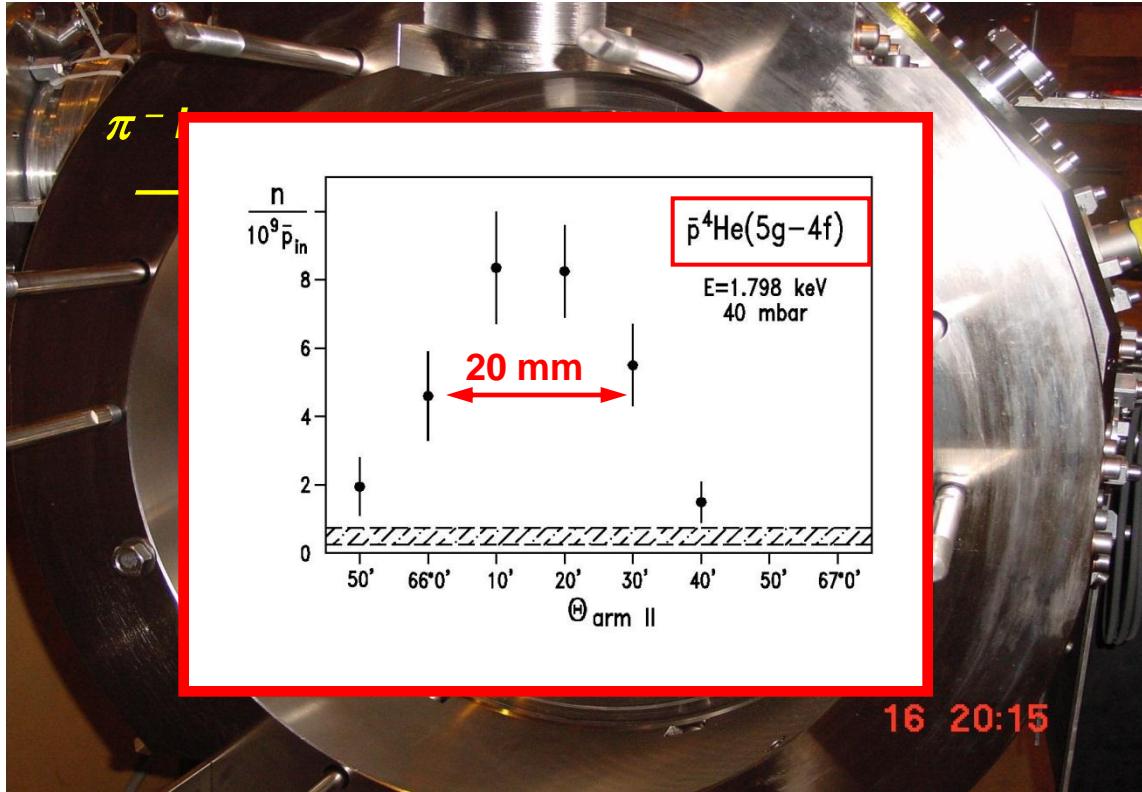
increase in stop density

pions (PSI) $\times 200$
antiprotons (LEAR) $\times 1.000.000$

⇒ high X - ray line yields

⇒ bright X - ray source

DEGRADERS and CRYOGENIC TARGET
inside
CYCLOTRON TRAP II
super-conducting split coil magnet



EXPERIMENT II

How to achieve ultimate energy determination and resolution?

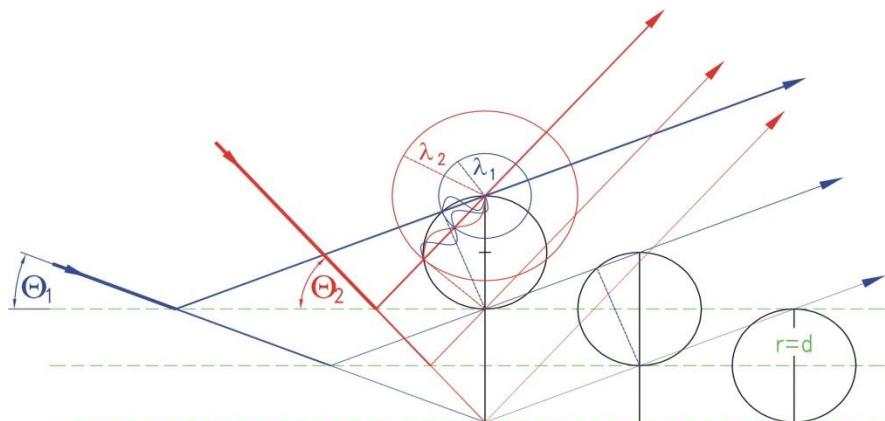
together with

sufficient count rate?

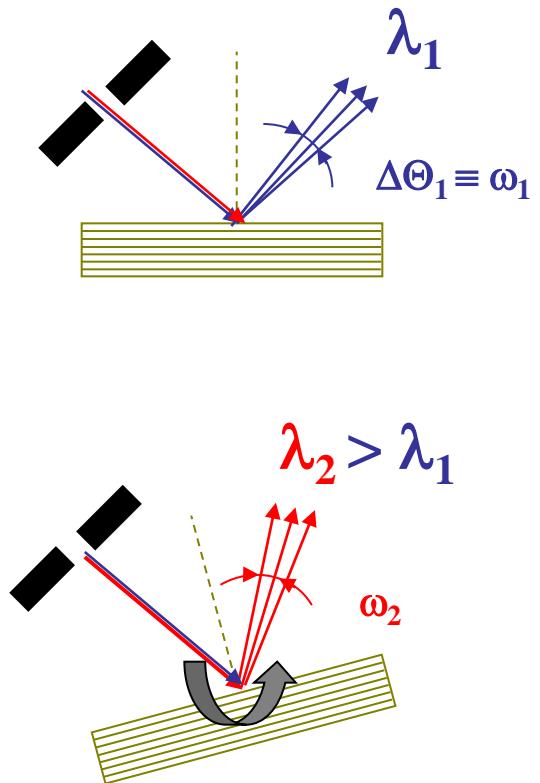
BRAGG'S LAW $n\lambda=2d \cdot \sin\theta_B$

n order of diffraction
 λ wave length
d spacing of diffracting planes
 θ_B Bragg angle

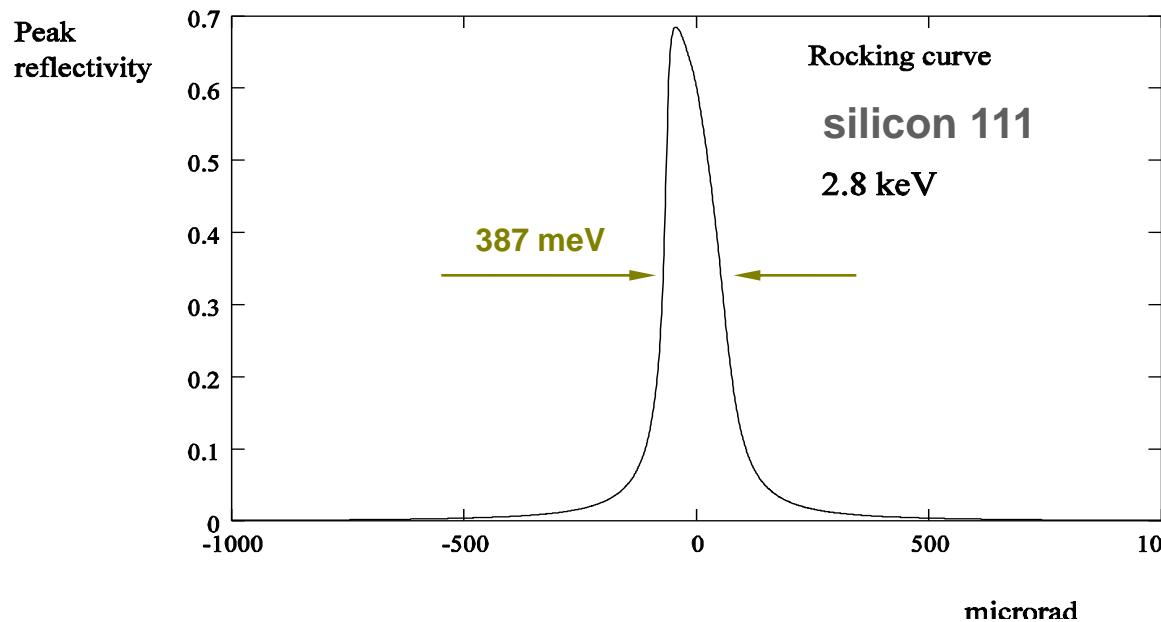
ω angular spread of reflection



τ_e extinction length *coherent reflection*
 τ_a absorption length *incoherent*
usually $\tau_e \ll \tau_a$



calculated CRYSTAL RESPONSE



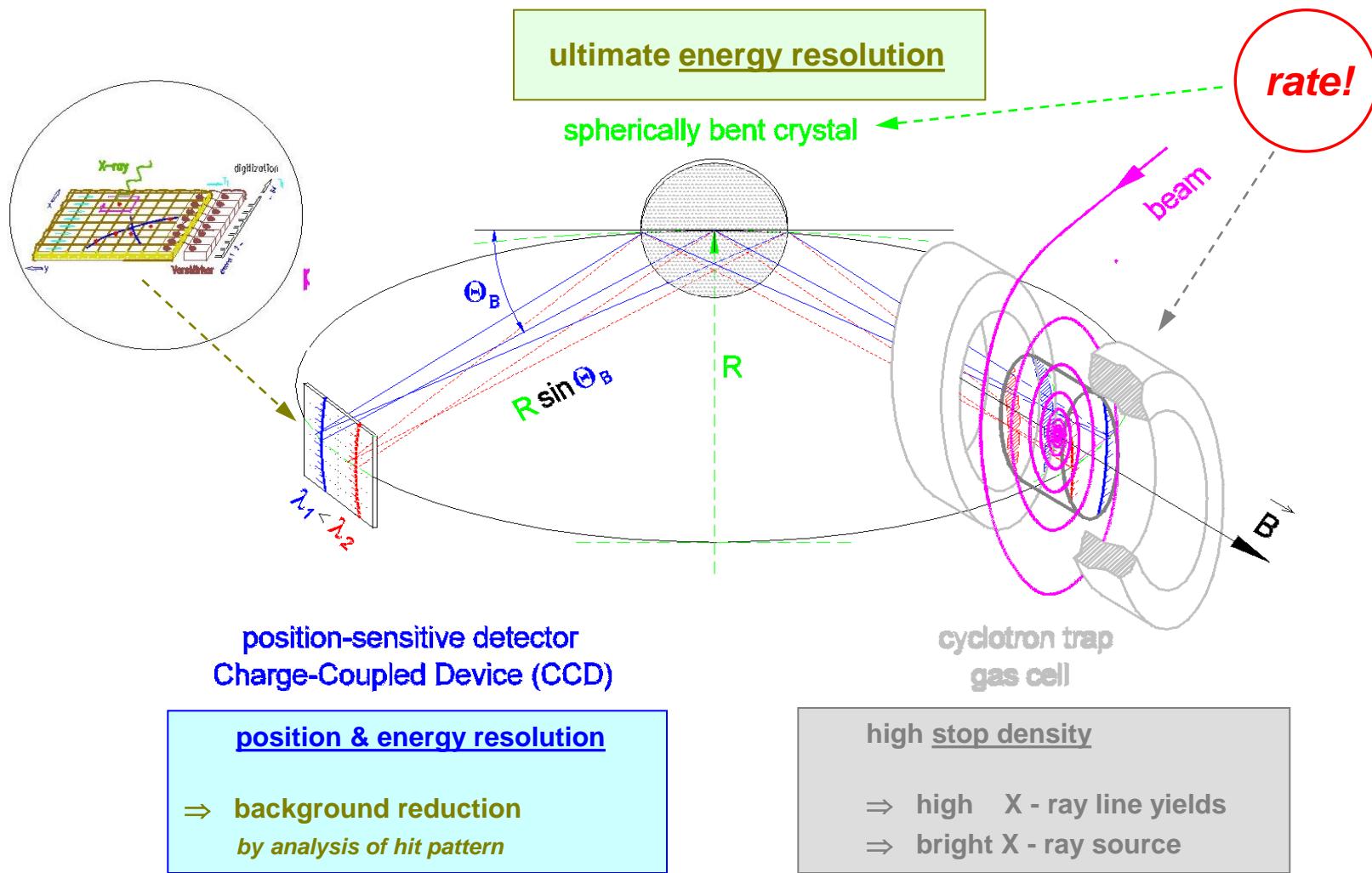
diffraction theory

*XOP2 code
plane crystal*

for real crystal mounting?

no narrow few keV γ lines

Johann-type SET-UP

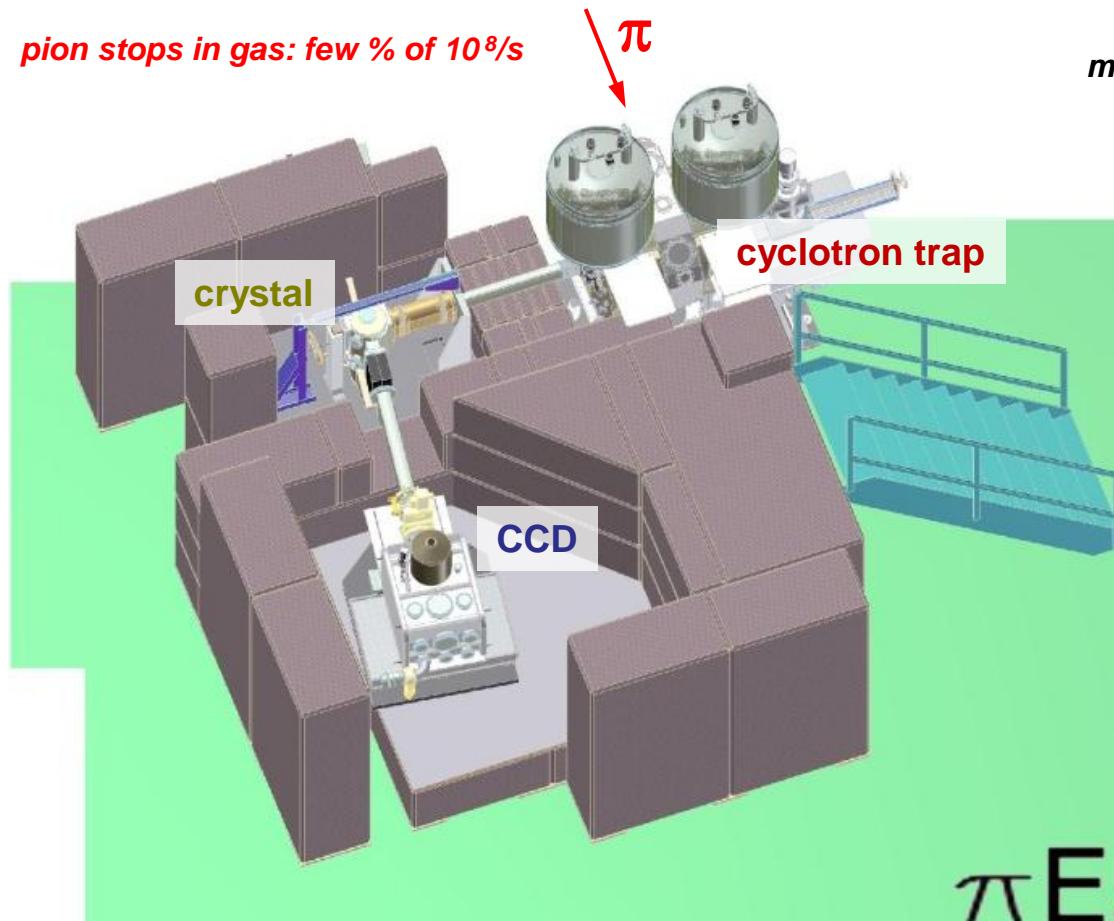


L. Simons, Physica Scripta 90 (1988), Hyperfine Int. 81 (1993) 253

PIONIC HYDROGEN collaboration - SET-UP at PSI

pion stops in gas: few % of 10^8 /s

π



crystal spectrometer setup

$\pi H(4-1)$ and $\pi D(3-1)$ $\Theta_{Bragg} \approx 40^\circ$

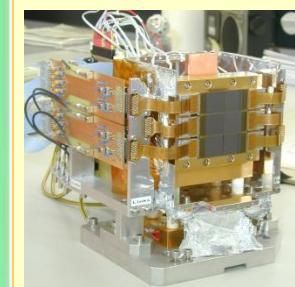
PSI experiments R-98.01 and R-06.03

measurements $\pi H(2-1), \pi H(3-1), \pi H(4-1)$
 $\pi D(3-1)$
 $\mu H(3-1)$

BRAGG CRYSTAL Si 111
spherically bent



FOCAL PLANE DETECTOR
 3×2 CCD array

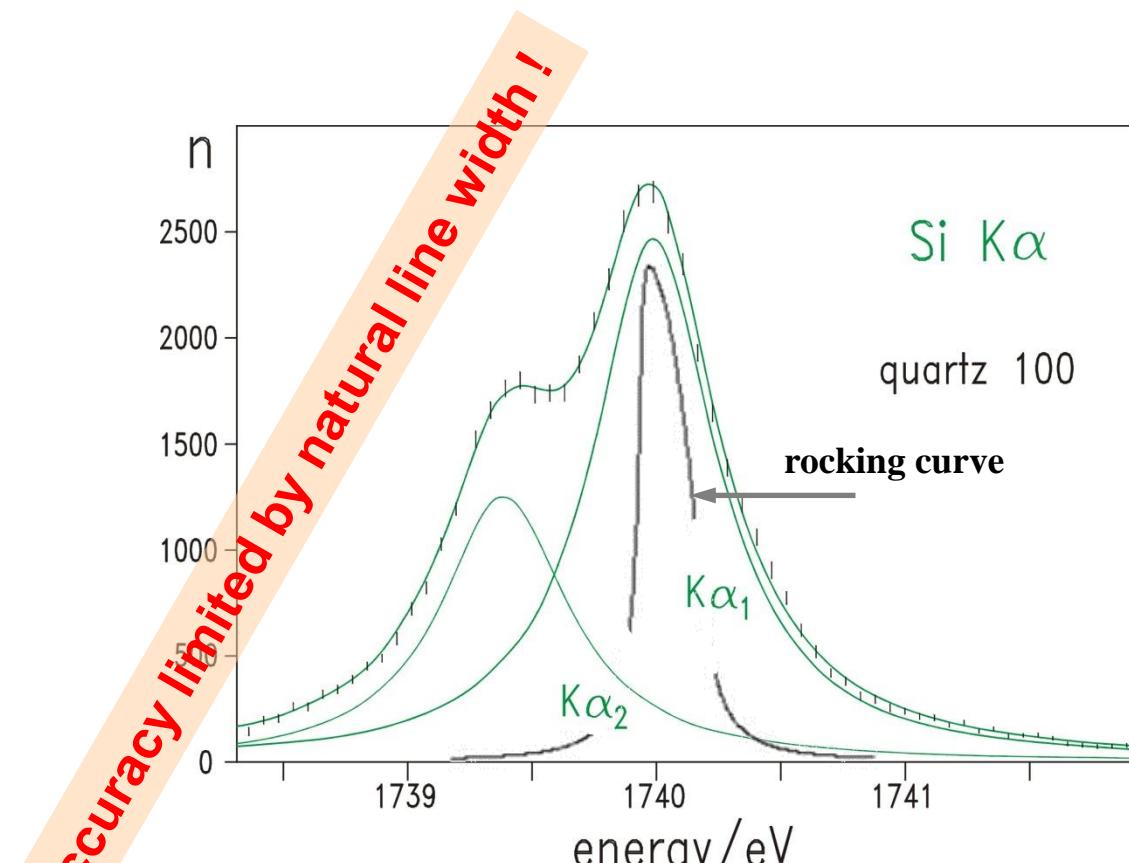


see talk by
M. Jabua
Fr 14:30

EXPERIMENT III

How to measure the resolution of the crystal spectrometer ?

CALIBRATION by fluorescence X-rays



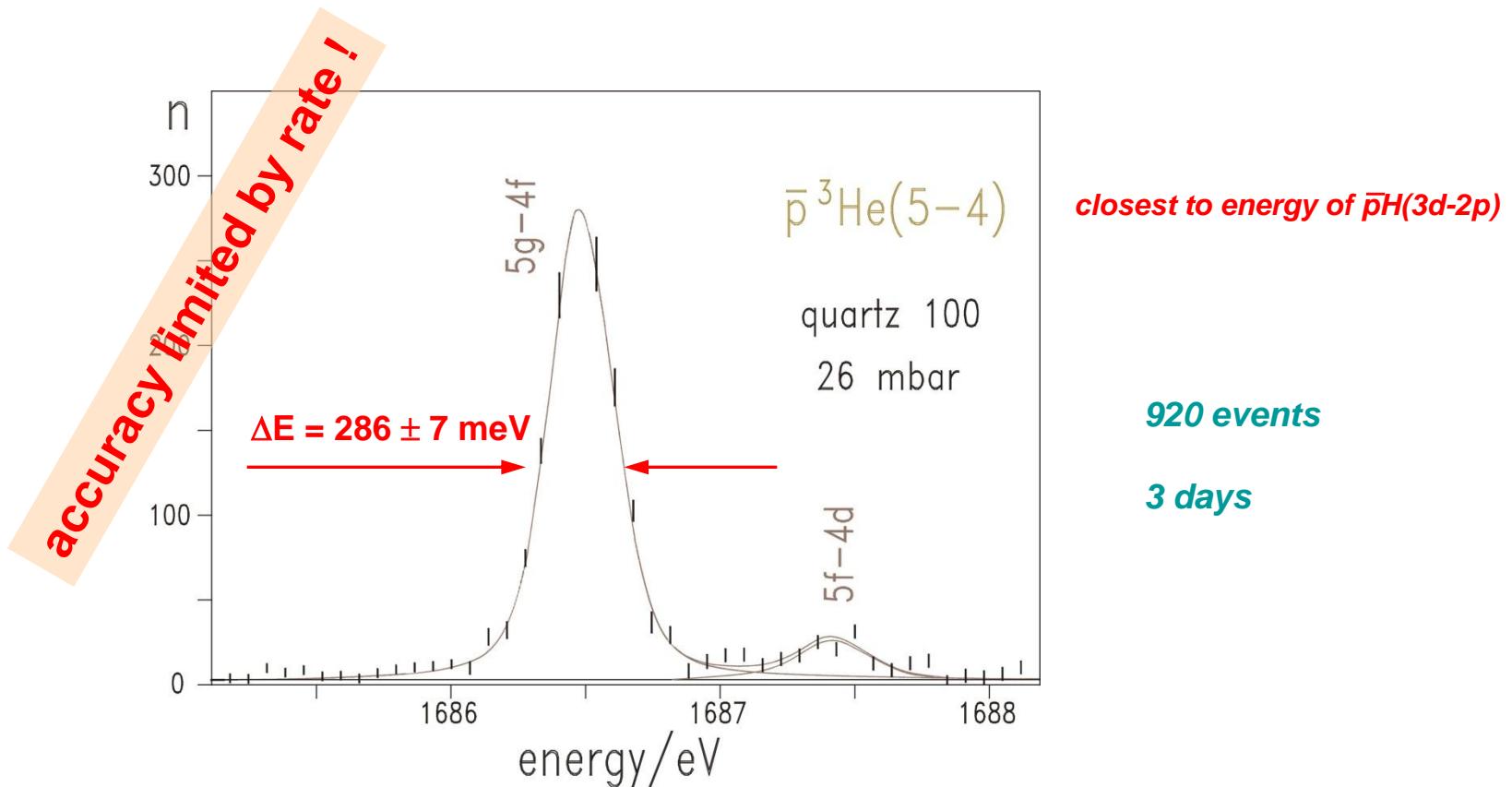
closest to energy of $\bar{p}H(3d-2p)$

excitation
of Si X-rays
by means of
X-ray tube

high rate

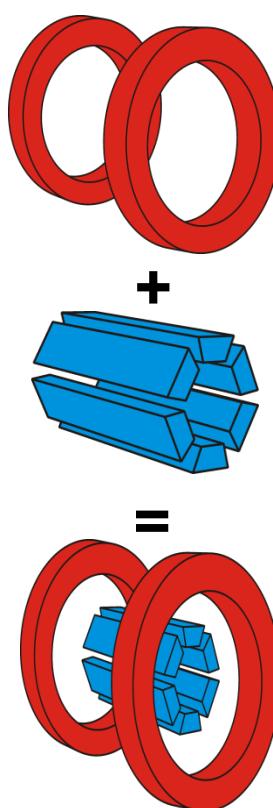
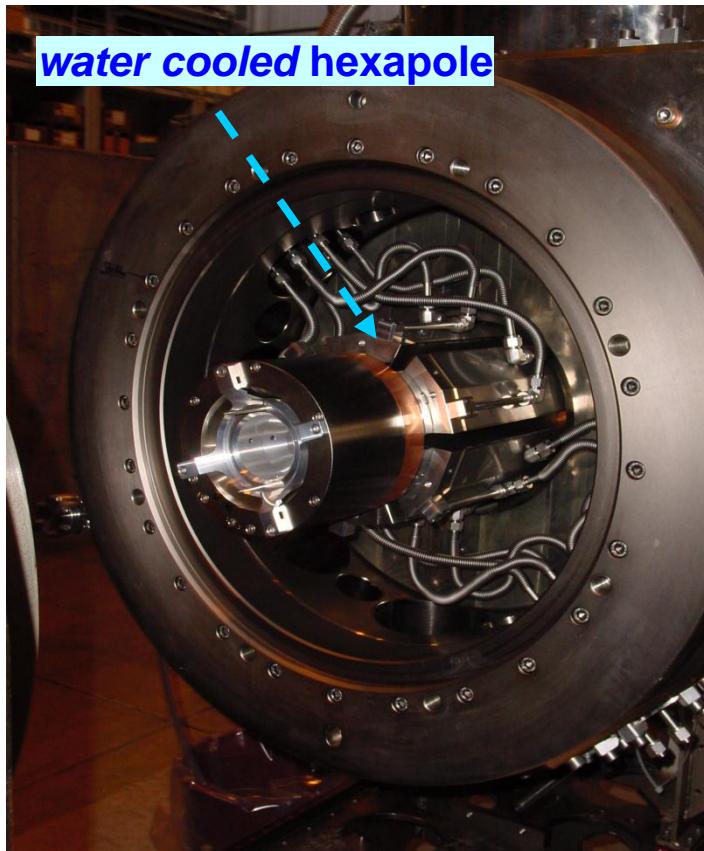
large line width and satellites - resolution hardly measurable

RESPONSE FUNCTION *from exotic atoms*



SPECTROMETER RESPONSE

new approach (PSI) ECRIT



Superconducting coils

- *cyclotron trap*

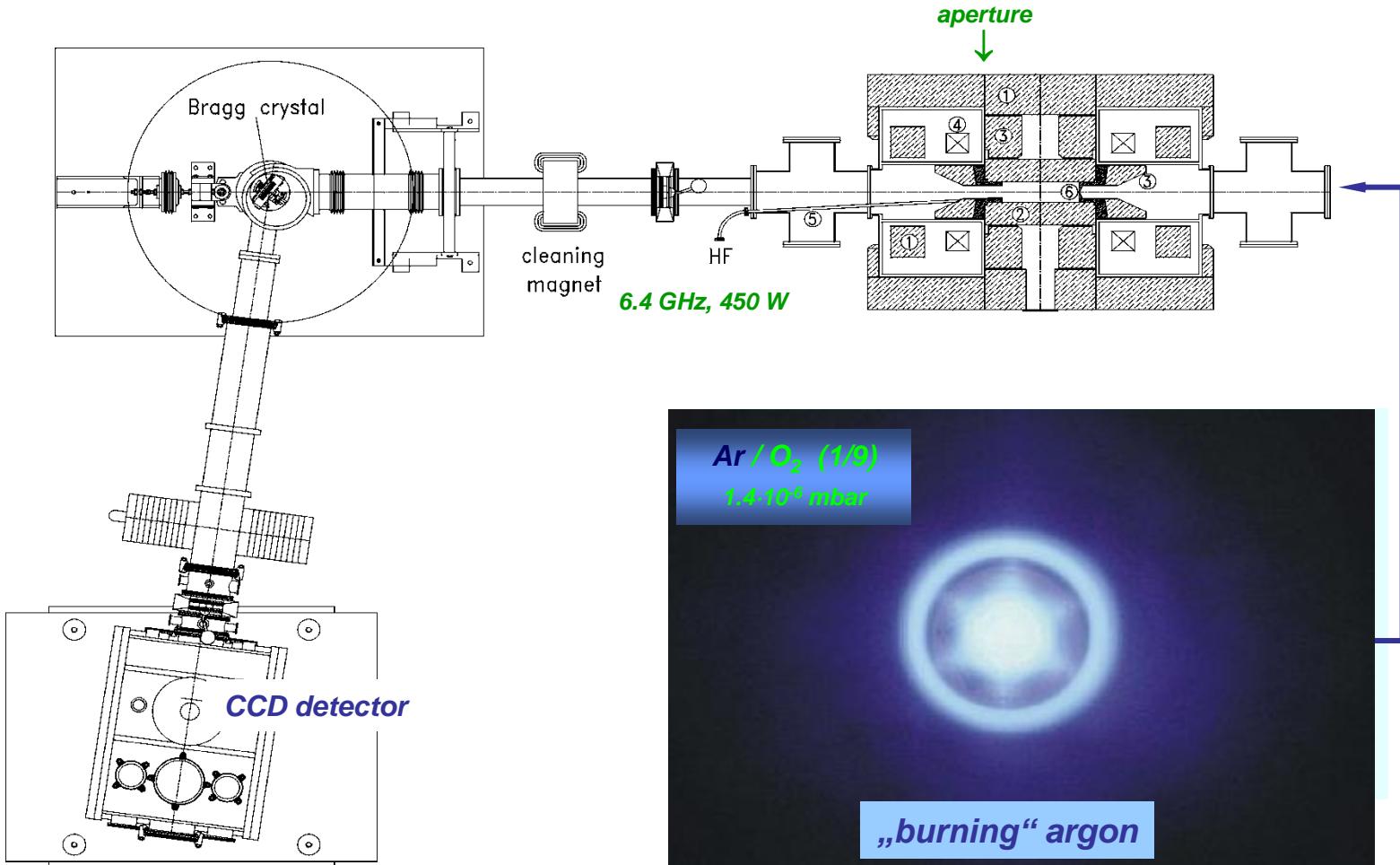
permanent hexapole

- *AECR-U type*
- *1 Tesla at the hexapole wall*
- *open structure*

large mirror ratio = 4.3
 B_{max} / B_{min} !

CRYSTAL SPECTROMETER and PSI ECRIT

Electron Cyclotron Resonance Ion Trap
=
cyclotron trap (4) + hexapole magnet (2)

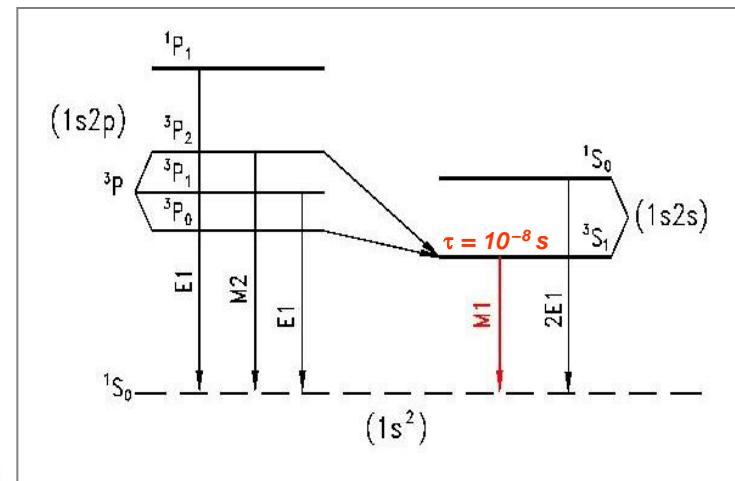
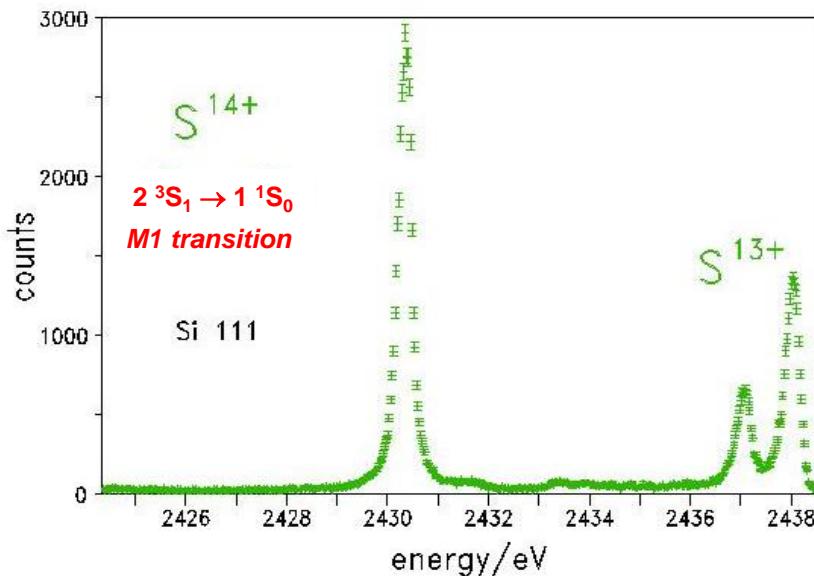


SPECTROMETER RESPONSE at πH Lyman ENERGIES

M1 transitions in He - like S $\leftrightarrow \pi H(2p-1s)$

Cl $\leftrightarrow \pi H(3p-1s)$

Ar $\leftrightarrow \pi H(4p-1s)$



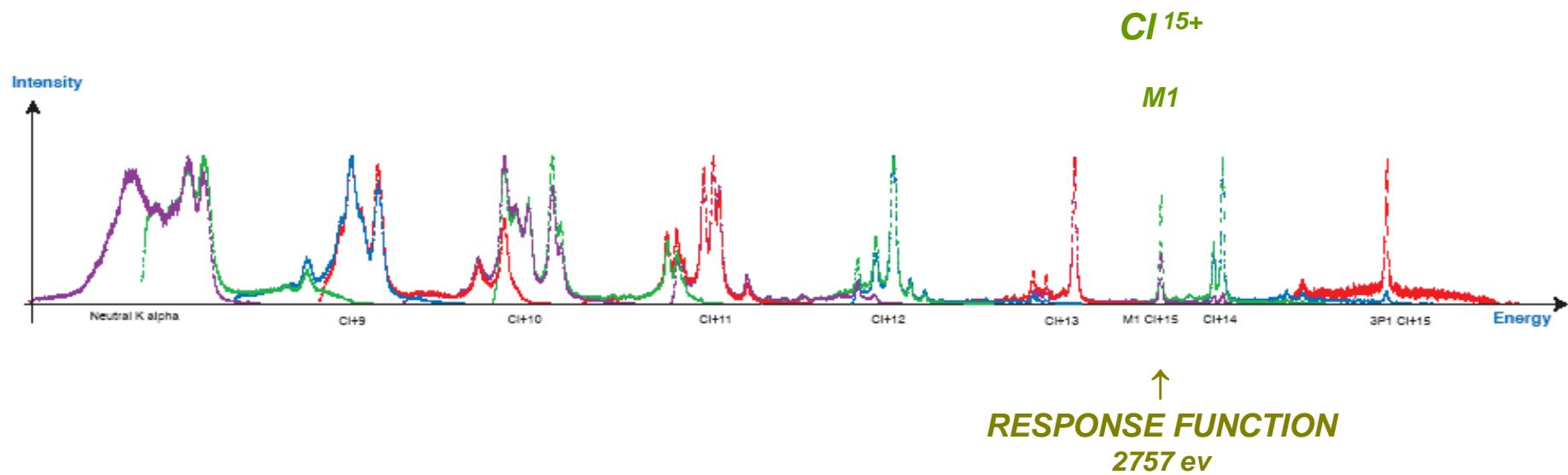
30000 events in line (3 h) \leftrightarrow tails can be fixed with sufficient accuracy

to be compared with Monte-Carlo ray tracing folded with plane crystal response

D.F.Anagnostopoulos et al., Nucl. Instr. Meth. B 205 (2003) 9

D.F.Anagnostopoulos et al., Nucl. Instr. Meth. A 545 (2005) 217

CHLORINE SKY LINE



PHYSICS POTENTIAL

LEAR experiments

PS 175 cyclotron trap

L. Simons et al.

PS 207 antiprotonic hydrogen

PSI experiments

R-97.02 pion mass

R-98.01 pionic hydrogen

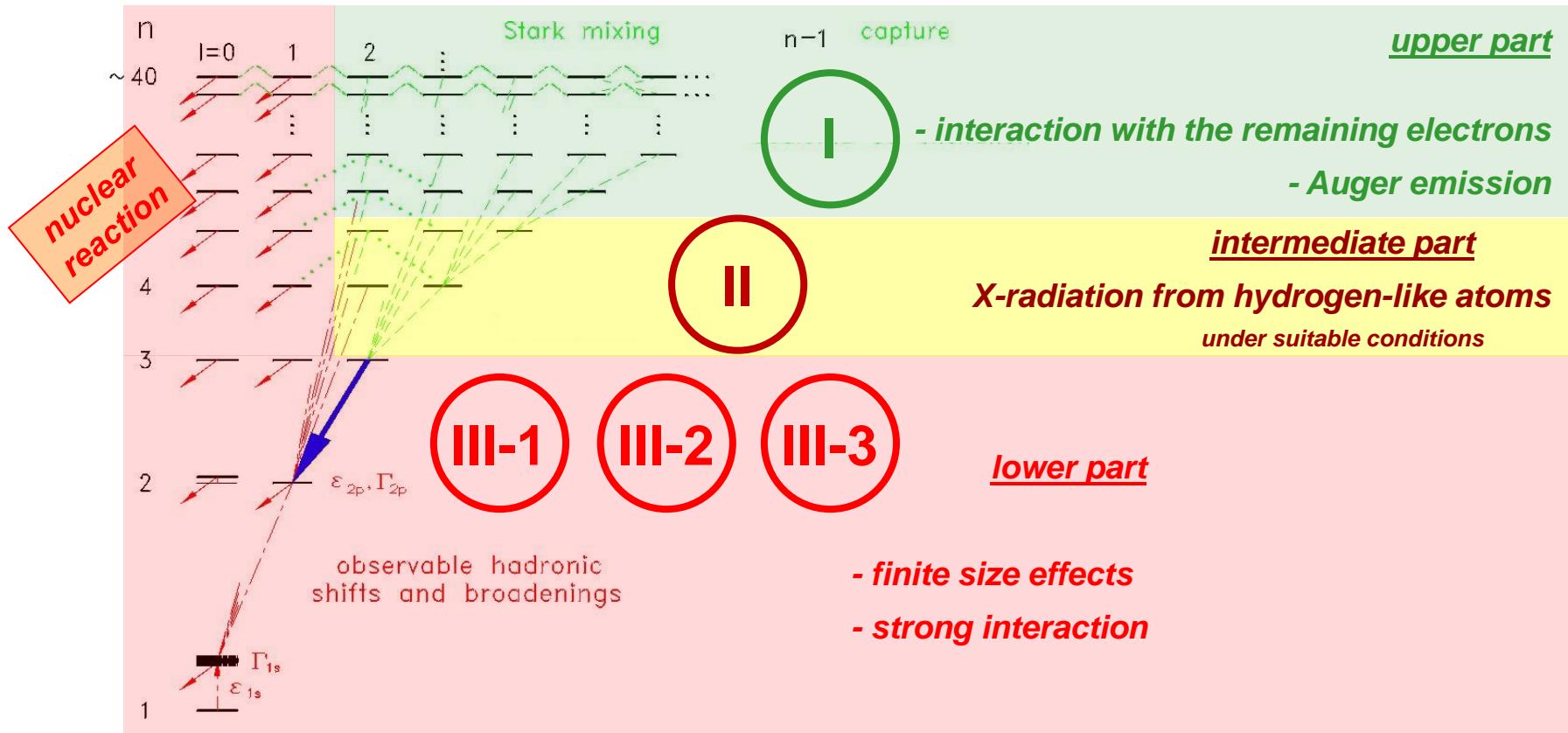
R-06.03 pionic deuterium

R-98.02 muonic hydrogen Lamb shift

A. Antognioni, F. Kottman, R. Pohl et al.

LEVEL SCHEME and CASCADE

particle capture when slowed down to a few eV kinetic energy into high-lying atomic levels



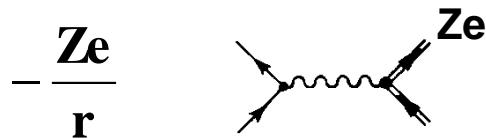


CAPTURE and DE-EXCITATION

multi-particle systems

ATOMIC BINDING ENERGY

$$E_B = E_{\text{Coulomb}}$$

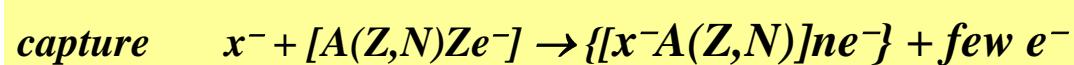


$$+ \Delta E_{\text{QED}}$$



self energy + *vakuum polarisation* + *higher orders*

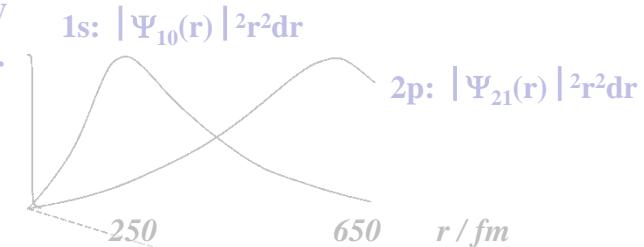
$$+ \Delta E_{\text{screening}}$$



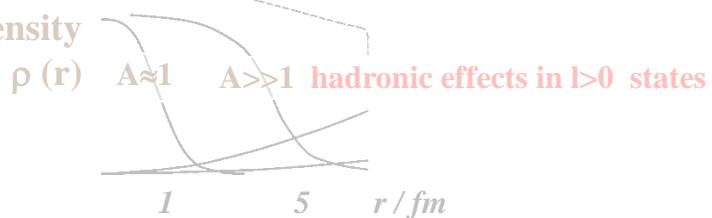
$$+ \Delta E_{\text{finite size}}$$

$$+ \Delta E_{\text{strong interaction}}$$

probability density
 $|\Psi_{nl}(r)|^2 r^2 dr$



nuclear density
 $\rho(r)$



CAPTURE and UPPER PART of the ATOMIC CASCADE antiprotonic atom

where?

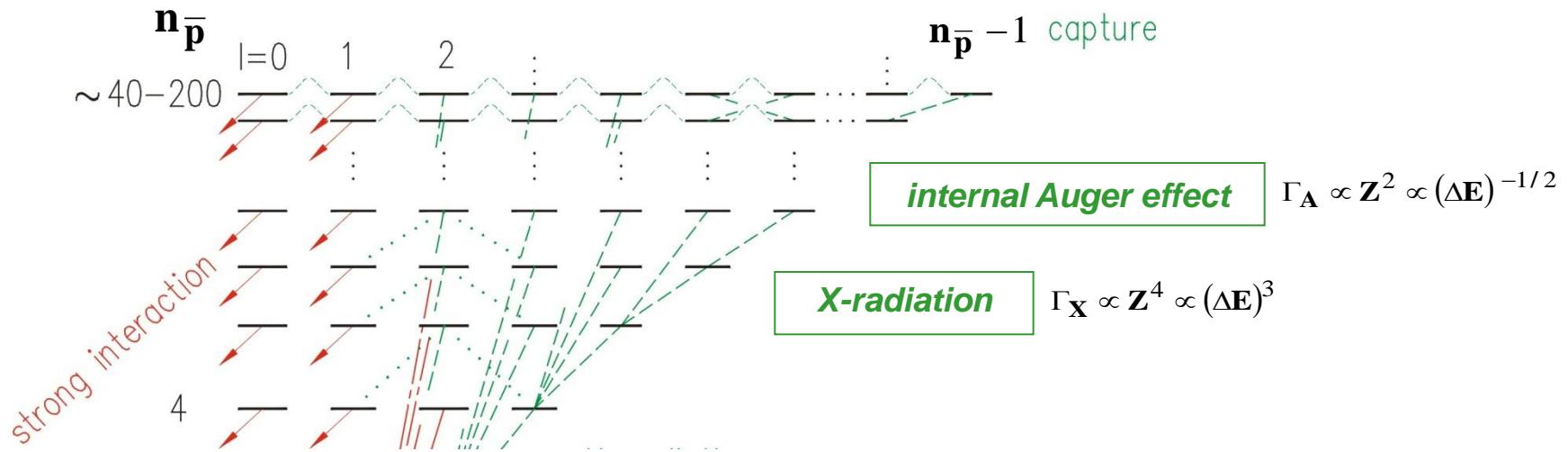
$$n_{\bar{p}} \approx 40 \cdot n_e$$

probability?

$$\Gamma_{\text{capture}} \propto Z$$

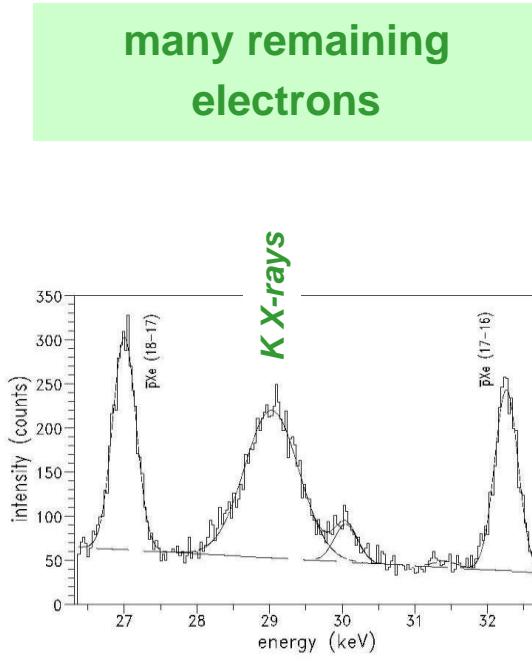
how?

$$\text{Pop}(n, \ell) \propto (2\ell + 1) \cdot e^{-\alpha\ell}$$

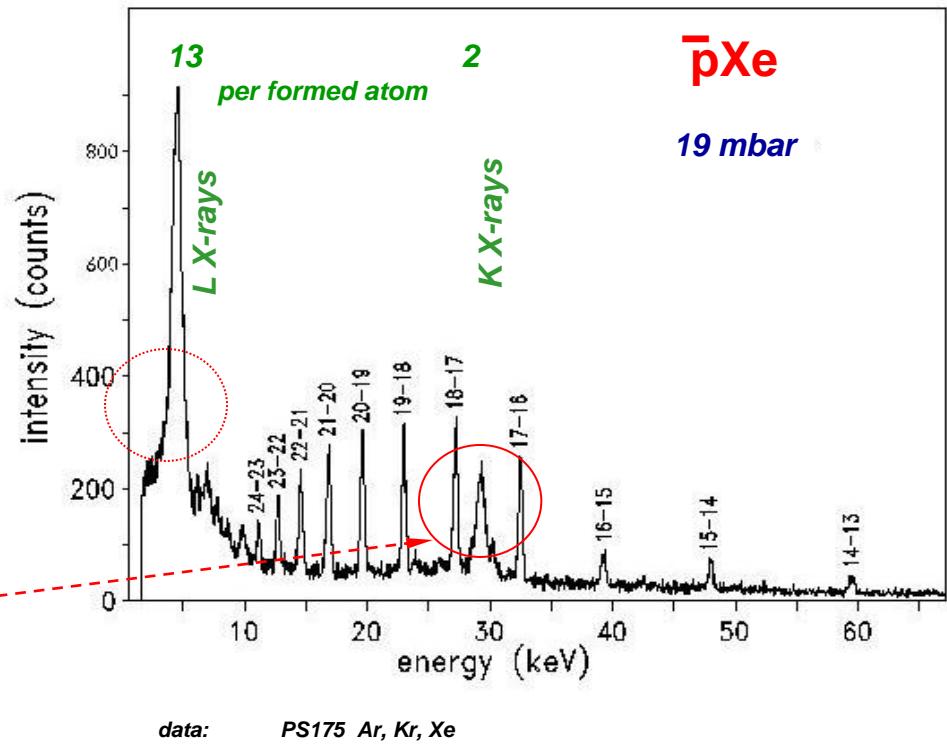


competition between AUGER and RADIATIVE DE-EXCITATION
electrons are peeled off like onion shells

ELECTRONIC & ANTIPIROTOMIC X-RAYS - XENON



many unresolved lines ?



Reanalysis: D.G., K.Rashid, B. Fricke, P. Indelicato, L.M. Simons,
Eur. Phys. D 47 (2008) 11

OUTLOOK - high resolution spectroscopy
- coincidence experiments X-rays / Auger electrons



CHARGED PION MASS

How to measure the mass of a short-lived particle?

life time $\tau_{\pi^\pm} = 26 \cdot 10^{-9}$ s

\Rightarrow *use a hydrogen-like systems*

ATOMIC BINDING ENERGY

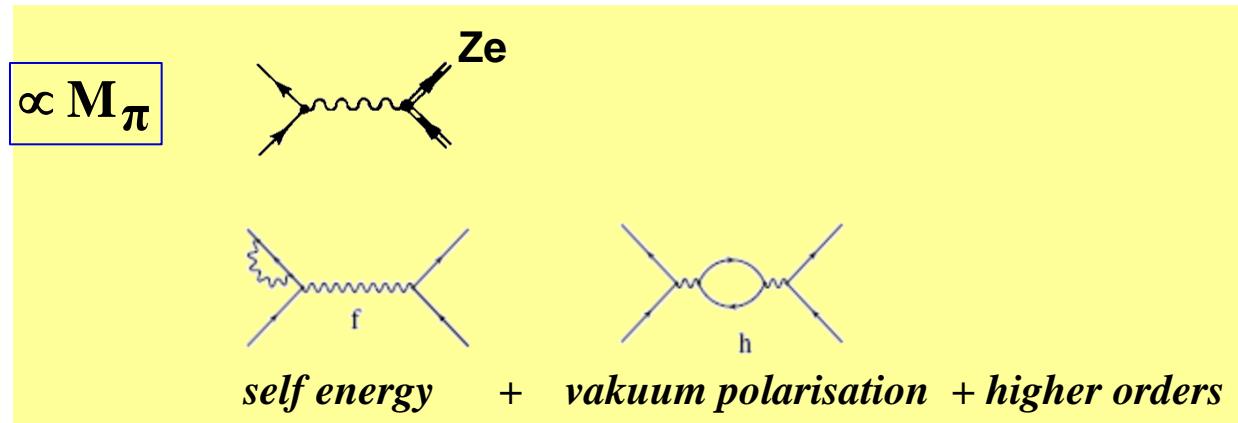
$$E_B = E_{\text{Coulomb}}$$

$$+ \Delta E_{\text{QED}}$$

$$+ \Delta E_{\text{screening}}$$

$$+ \Delta E_{\text{finite size}}$$

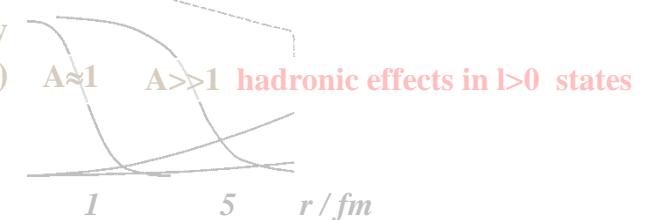
$$+ \Delta E_{\text{strong interaction}}$$



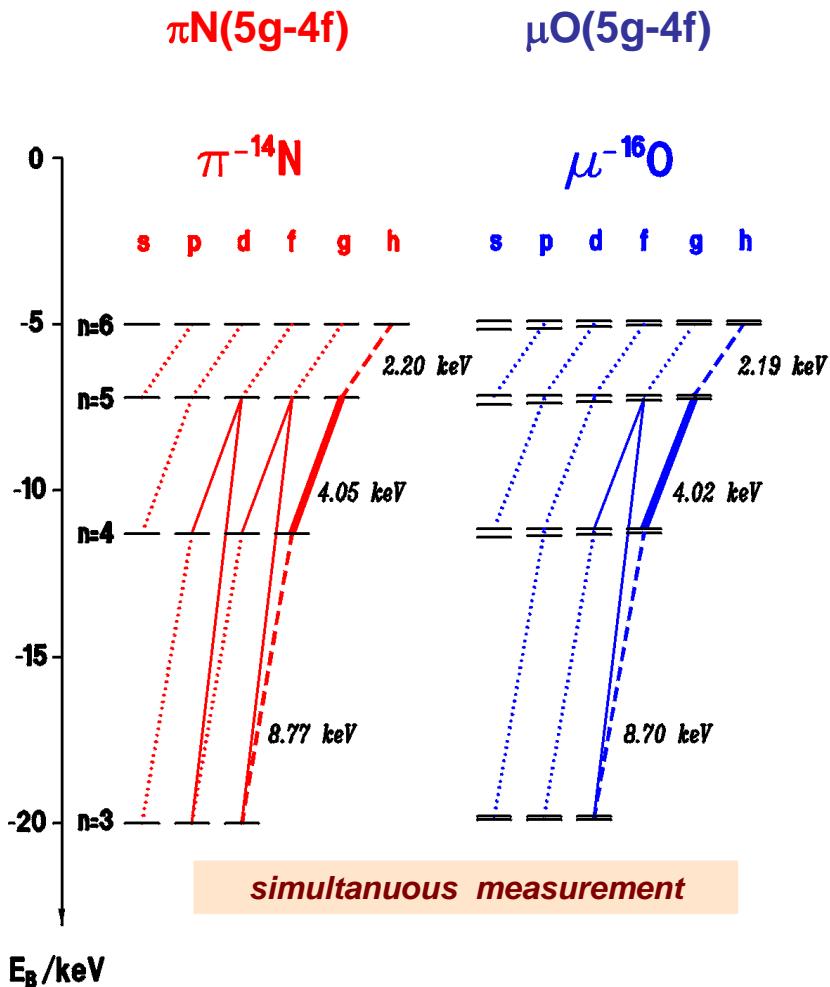
probability density
 $|\Psi_{nl}(r)|^2 r^2 dr$

1s: $|\Psi_{10}(r)|^2 r^2 dr$ 2p: $|\Psi_{21}(r)|^2 r^2 dr$

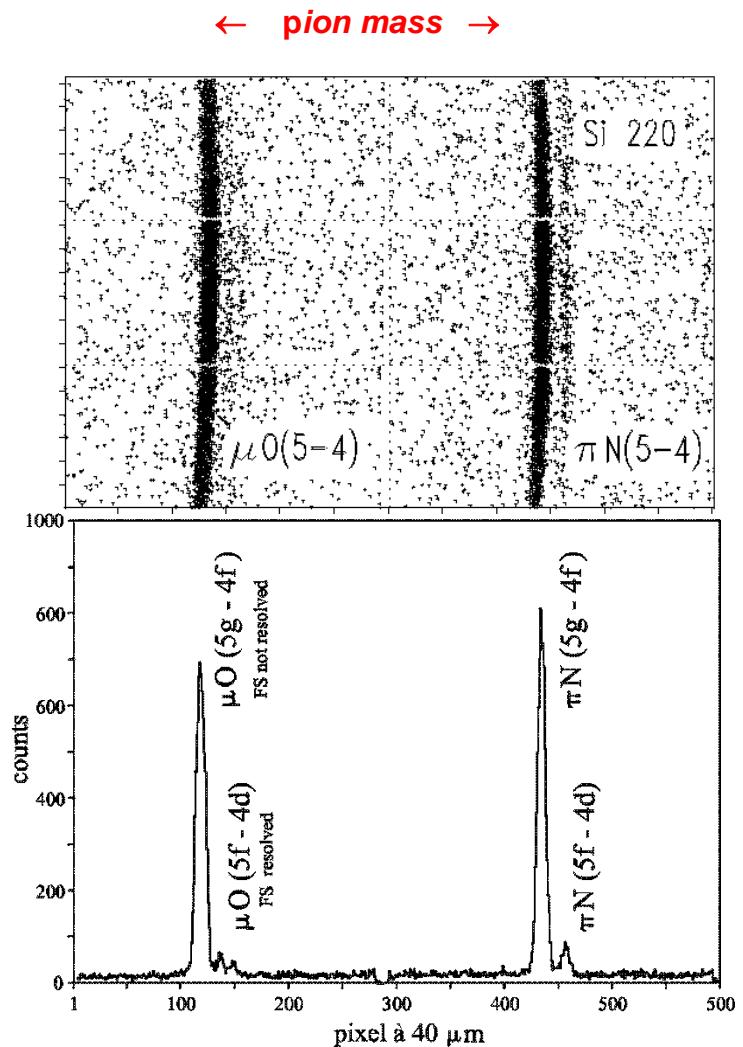
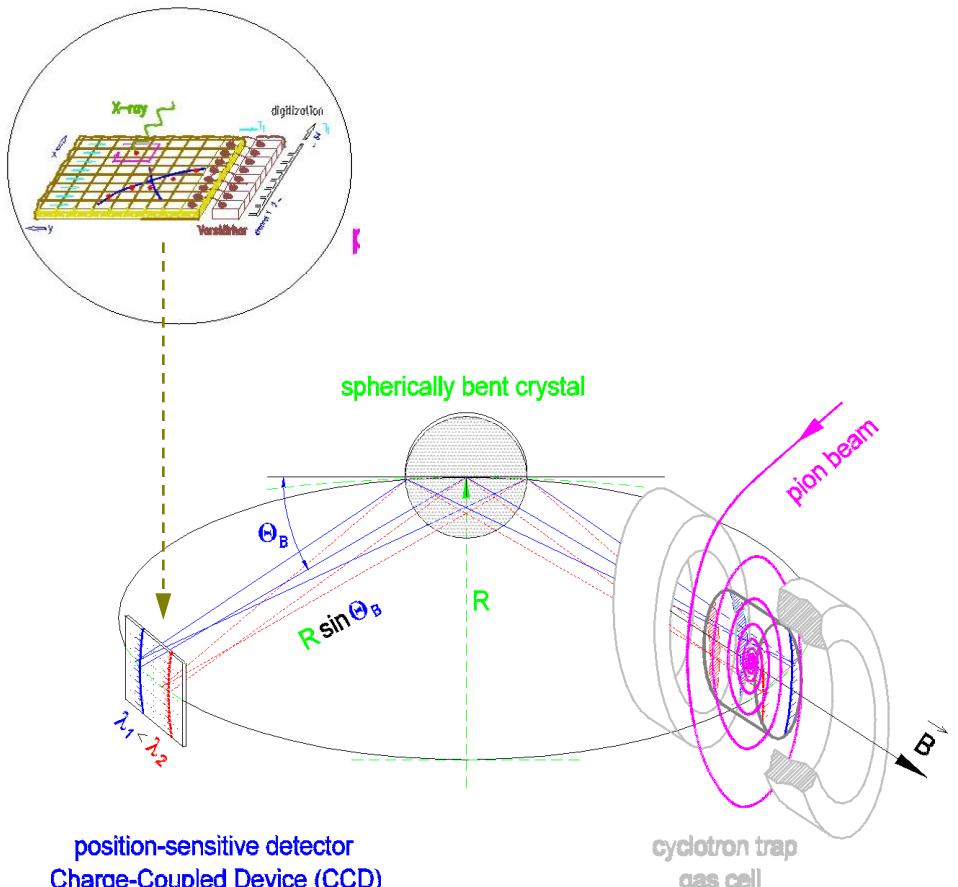
nuclear density
 $\rho(r)$



measurement calibration



- point like Coulomb potential
- no electron screening
- $E_{\mu\text{O}(5g-4f)} / E_{\pi\text{N}(5g-4f)} = m_\mu / m_\pi$



$$\Delta E/E \geq 1-2 \cdot 10^{-6}$$

III-1

PROTON CHARGE RADIUS

muonic hydrogen Lamb shift

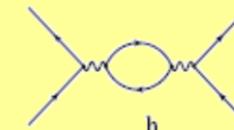
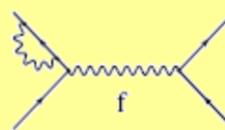
ATOMIC BINDING ENERGY

$$E_B = E_{\text{Coulomb}}$$

$$r \propto \frac{1}{M}$$



$$+ \Delta E_{\text{QED}}$$

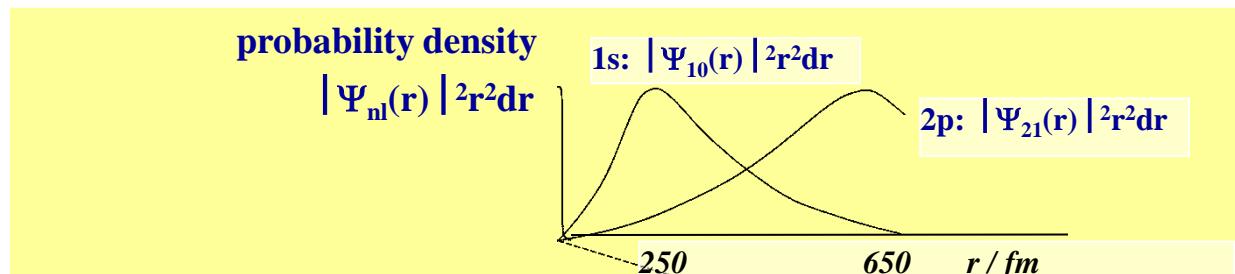


self energy + *vakuum polarisation* + *higher orders*

$$+ \Delta E_{\text{screening}}$$

capture $x^- + [A(Z,N)Ze^-] \rightarrow \{[x^-A(Z,N)]ne^- \} + \text{few } e^-$

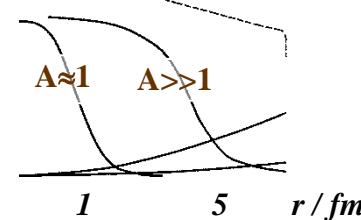
$$+ \Delta E_{\text{finite size}}$$



$$+ \Delta E_{\text{strong interaction}}$$

nuclear density $\rho(r)$

$A \approx 1$ $A \gg 1$



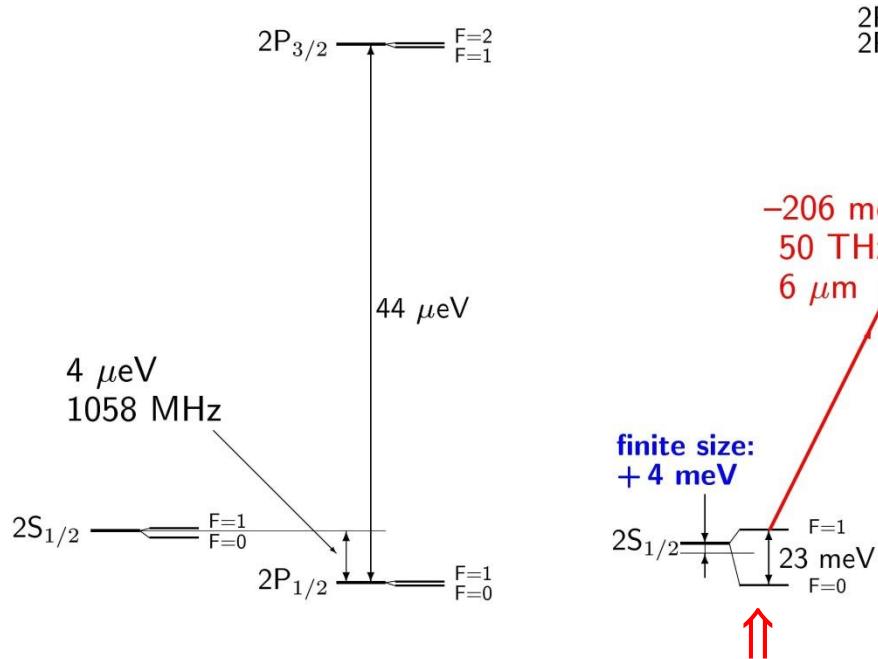
MUONIC HYDROGEN LAMB SHIFT

e^-p

large! $2 \cdot 10^5 \text{ fm}$

μ^-p

small! $1 \cdot 10^3 \text{ fm}$



very sensitive to proton charge radius

μH collaboration: see e.g. R. Pohl et al., *Hyperf. Int.* 193 (2009) 115; *Nature*, vol. 466, issue 7303, pp. 213-216 (2010)



proton charge radius

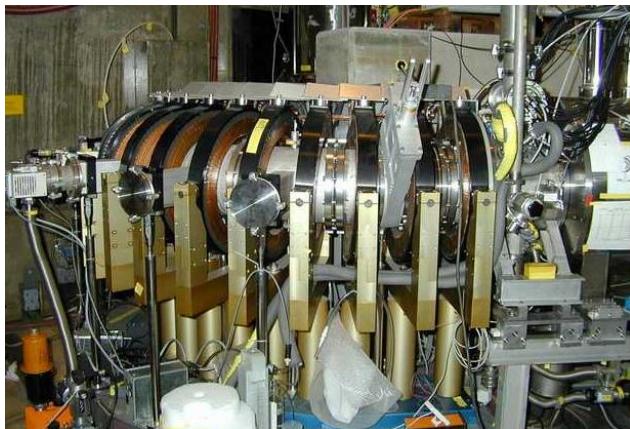
$(0.8768 \pm 0.0069) \cdot 10^{-15} \text{ m}$ *H spectroscopy*

$(0.897 \pm 0.018) \cdot 10^{-15} \text{ m}$ *electron scattering*

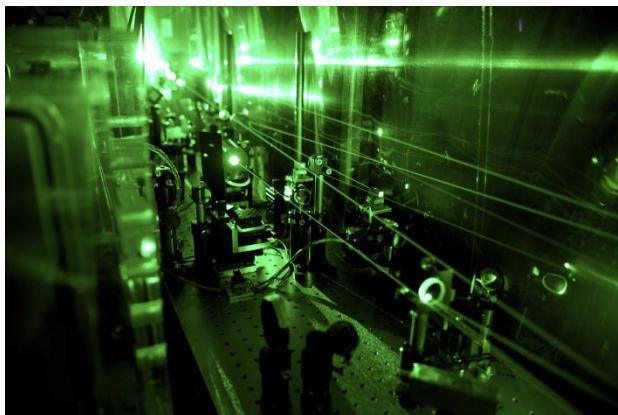
$(0.84184 \pm 0.00067) \cdot 10^{-15} \text{ m}$ *μH*
error $\rightarrow \approx \text{error} / 10 !$

MUONIC HYDROGEN LAMB SHIFT - EXPERIMENT

extraction channel



part of LASER system



1. Stop pions in cyclotron trap
2. extract decay muons to extraction channel
3. Form μ H in dilute hydrogen
4. Pump 2s-2p resonance with laser
5. Identify 2s-2p energy difference by resonance condition

III-2

STRONG INTERACTION

PION-NUCLEON SCATTERING LENGTHS

„QCD Lamb shift“

ATOMIC BINDING ENERGY

$$E_B = E_{\text{Coulomb}}$$



$$+ \Delta E_{\text{QED}}$$



self energy + *vakuum polarisation* + *higher orders*

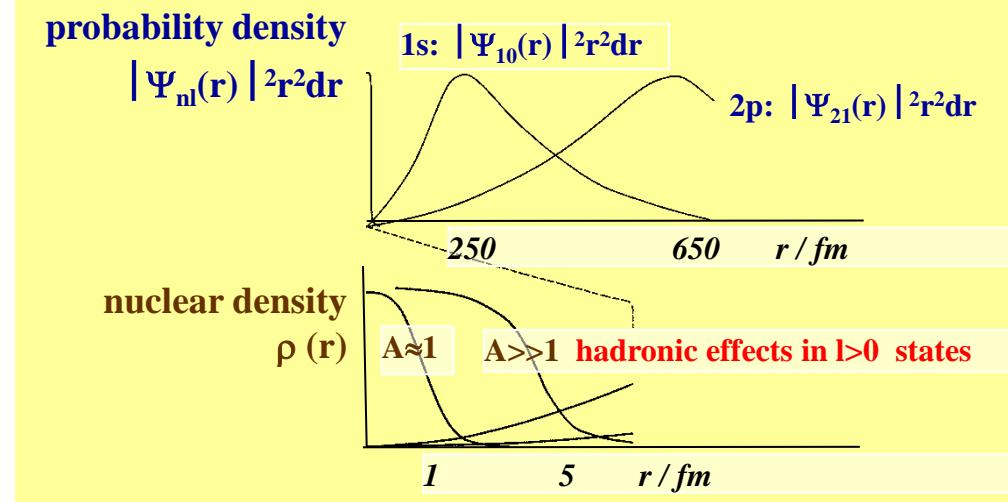
$$+ \Delta E_{\text{screening}}$$

capture



$$+ \Delta E_{\text{finite size}}$$

$$+ \Delta E_{\text{strong interaction}}$$



HYDROGEN & DEUTERIUM - ORIGIN OF Γ_{1s}



CEX scattering



radiative capture



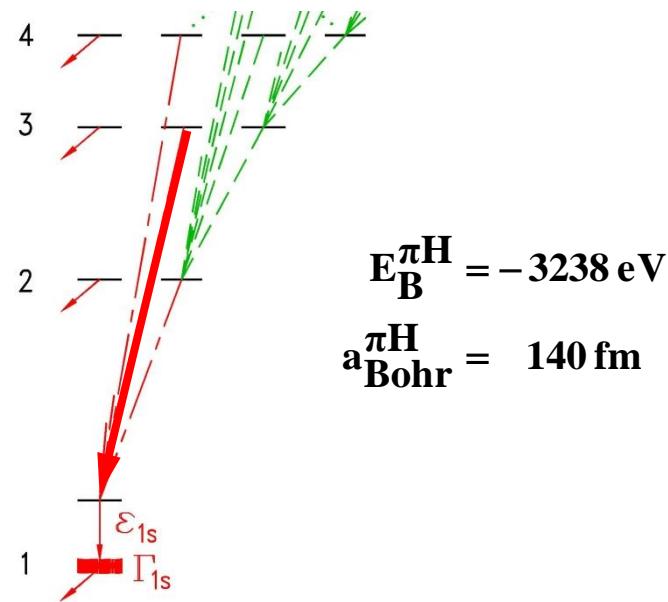
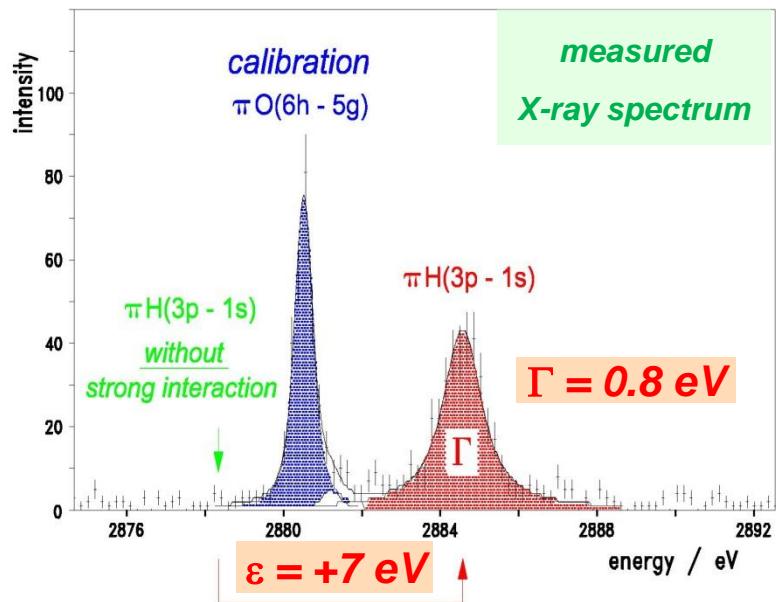
BR are well known from experiment



„true“ absorption



PIONIC HYDROGEN 3p-1s transition



| scattering lengths | | | | |
|--------------------|--|-----------------------|-----|-----|
| πH | $\varepsilon_{1s} \propto a_{\pi\text{-p} \rightarrow \pi\text{-p}}$ | $\propto a^+ + a^-$ | $+$ | ... |
| | $\Gamma_{1s} \propto (a_{\pi\text{-p} \rightarrow \pi^0\text{n}})^2$ | $\propto (a^-)^2$ | $+$ | ... |
| πD | $\varepsilon_{1s} \propto a_{\pi\text{-d} \rightarrow \pi\text{-d}}$ | $\propto 2 \cdot a^+$ | $+$ | ... |

| experiment | Trueeman correction | χPT * |
|-------------|---------------------|--------------------------|
| $\pm 0.2\%$ | $\dots \approx$ | $1\% + (-9.0 \pm 3.5)\%$ |
| $\pm 2.5\%$ | $\dots \approx$ | $1\% + (+0.5 \pm 1.0)\%$ |
| $\pm 1.3\%$ | $\dots \approx$ | $1\% + \pm 4\%$ |

* J. Gasser et al., Phys. Rep. 456 (2008) 167
M. Hoferichter et al., Phys. Lett. B 678 (2009) 65
V. Baru et al., Phys. Lett. B 694 (2011) 473

PIONIC DEUTERIUM SHIFT

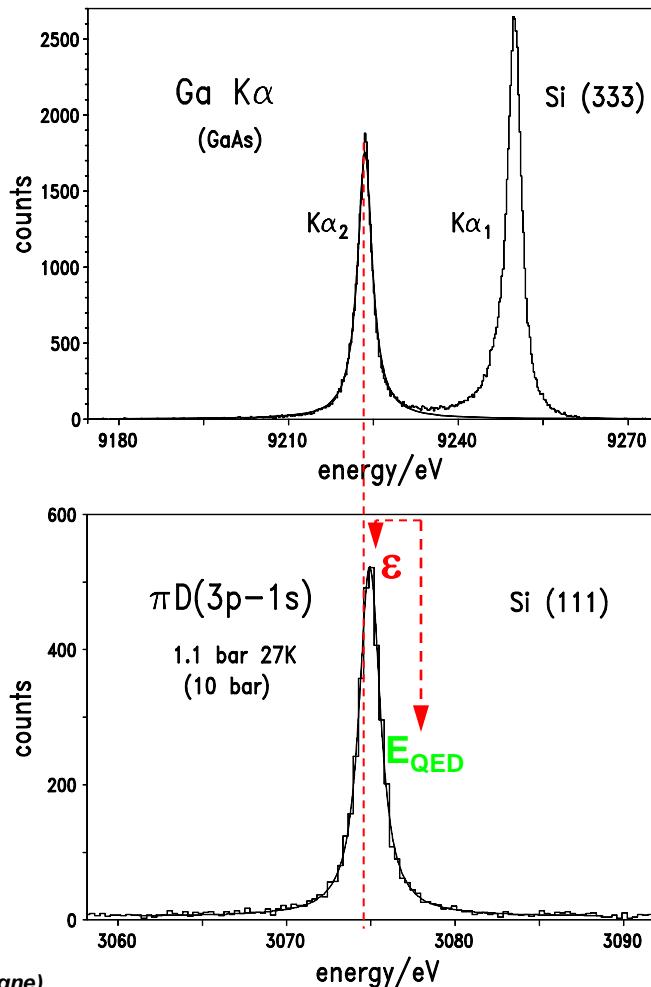
energy calibration

Ga K α

strong interaction

$\pi D(3p-1s)$

T.Strauch, PhD thesis: (FZJ, Univ. Cologne)



$$\varepsilon = -2 \text{ eV}$$

target material: GaAs

by chance: tabulated energy
also
from GaAs

identical Bragg angle

3 bar
10 bar
22 bar

to identify molecule formation

which scattering length?

$\pi H(np - 1s)$ energy shift ε_{1s} \Rightarrow $a_{\pi-p \rightarrow \pi-p}$

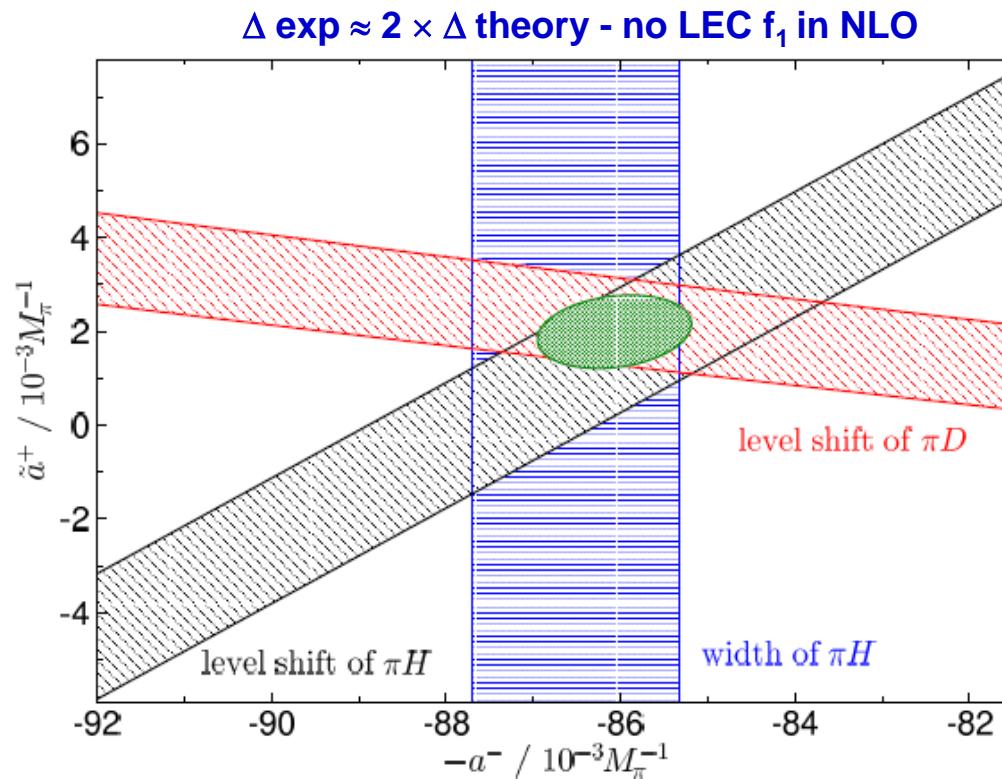
$\pi H(np - 1s)$ level width Γ_{1s} \Rightarrow $a_{\pi-p \rightarrow \pi^0 n}$

$\pi D(np - 1s)$ level shift ε_{1s} \Rightarrow $a_{\pi-p \rightarrow \pi-p} + a_{\pi-n \rightarrow \pi-n}$

two independent scattering length - all others linked by isospin

!!! $\pi D(np - 1s)$ level width Γ_{1s} \Rightarrow $\Im a_{\pi-d \rightarrow nn + nn\gamma}$

πN isospin scattering lengths a^+ and a^-



$\Delta \text{exp} \ll \Delta \text{theory} - \text{LEC } f_1$

$\Delta \text{exp} \ll \Delta \text{theory} - \text{LEC } f_1$

- consistency ✓
- $a^+ > 0 !$

FIG. 2: Combined constraints in the $\tilde{a}^+ - a^-$ plane from data on the width and energy shift of πH , as well as the πD energy shift.

χ PT: V. Baru, C. Hanhart, M. Hoferichter, B. Kubis, A. Nogga, and D. R. Phillips, Phys. Lett. B 694 (2011) 473

data: πH - R-98.01 : D. Gotta et al., Lect. Notes Phys. 745 (2008) 165 (preliminary)

πD - R-06.03 : Th. Strauch et al., Eur. Phys. J. A 47 (2011) 88 (final)

III-3

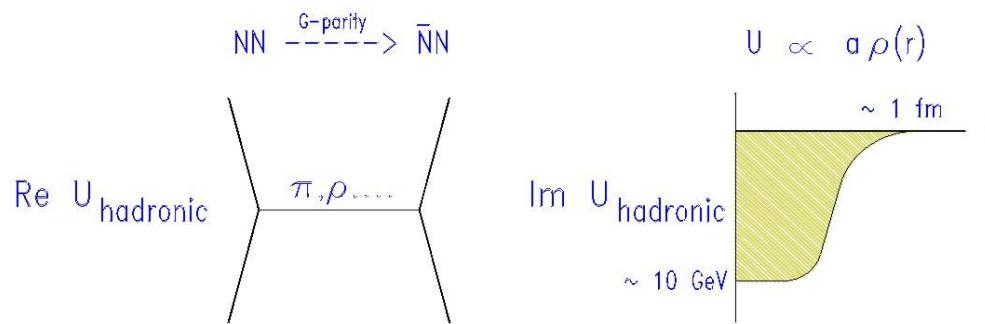
NUCLEON-ANTINUCLEON

SPIN-SPIN and SPIN-ORBIT INTERACTION

THEORETICAL DESCRIPTION

$$V_{\text{Coulomb}} + U_{\text{hadronic}}$$

$$U_{\text{hadronic}} = \begin{array}{l} \text{meson exchange} \\ \text{scattering: } \bar{p}p \leftrightarrow \bar{p}p \\ \bar{p}p \leftrightarrow \bar{n}n \end{array} + \begin{array}{l} \text{annihilation} \\ \bar{p}p \rightarrow \text{mesons} \end{array}$$



$\varepsilon, \Gamma \longleftrightarrow \text{medium + long-range part of } \bar{N}N \text{ interaction}$

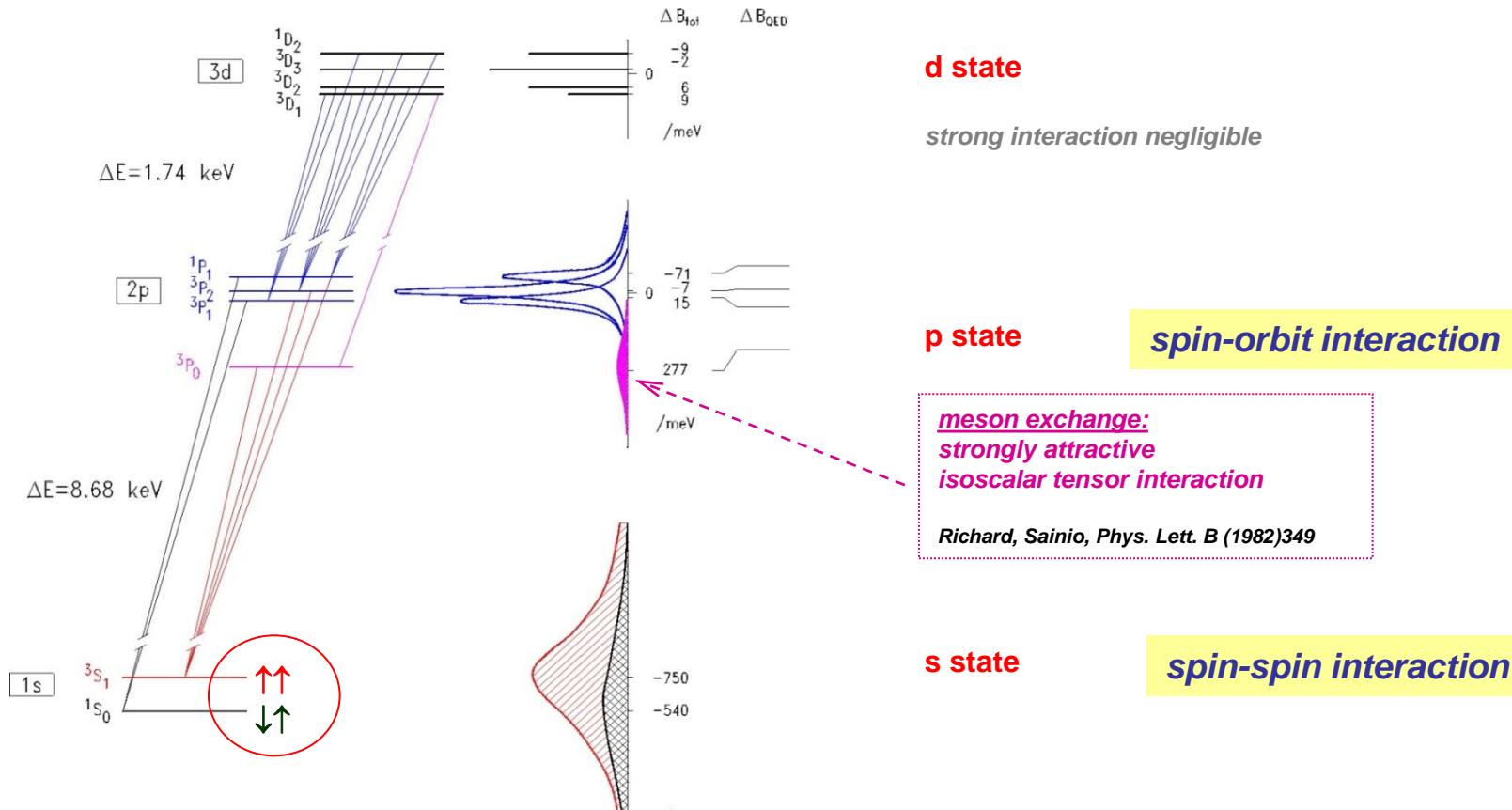
Buck, Dover, Richard, Ann. Phys. (NY) 121 (1979) 47

*spin-spin "deuteron"
spin-orbit effects*

no microscopic theory

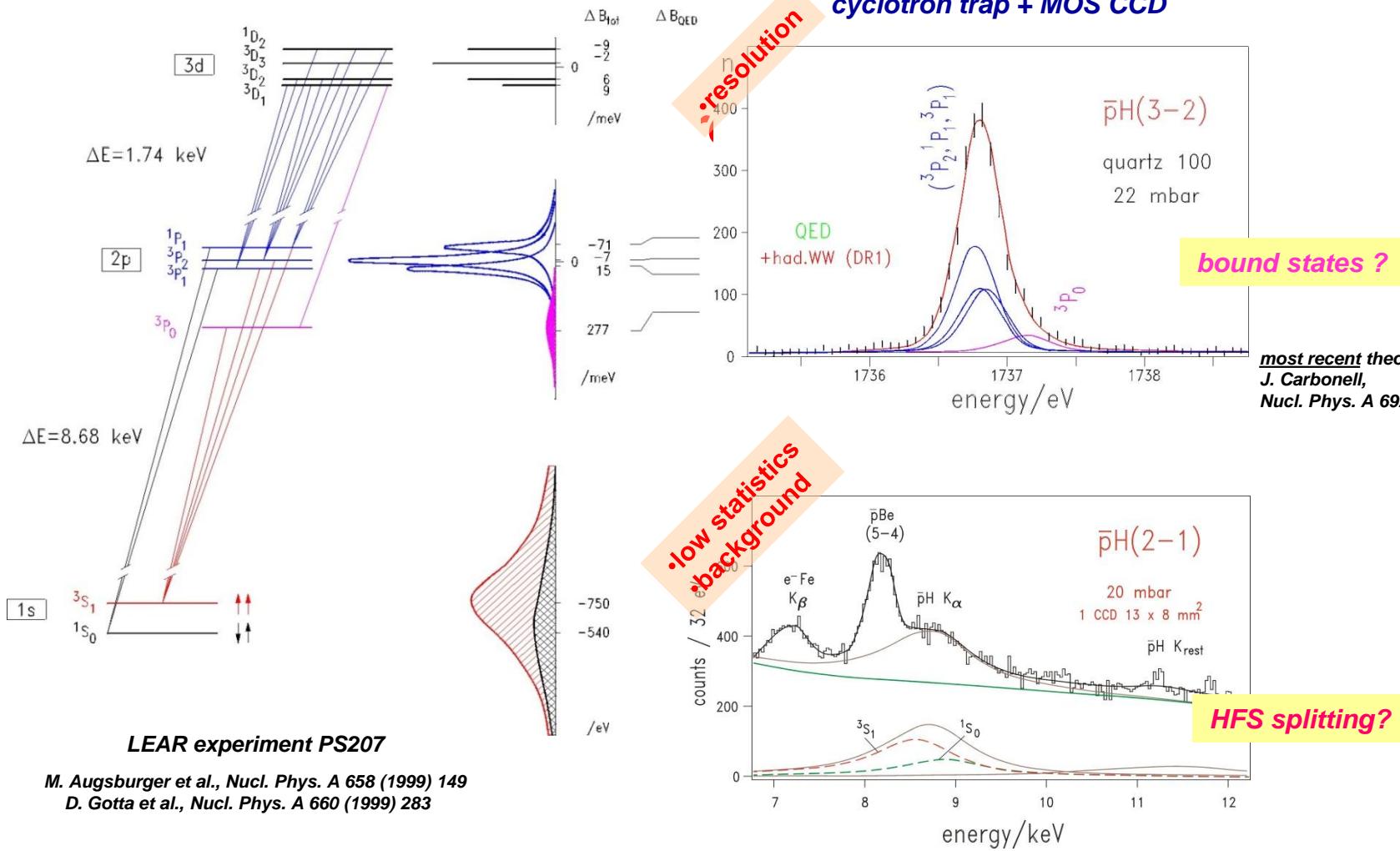
☞ **check spin dependence !**

PROTONIUM - s & p state strong-interaction effects



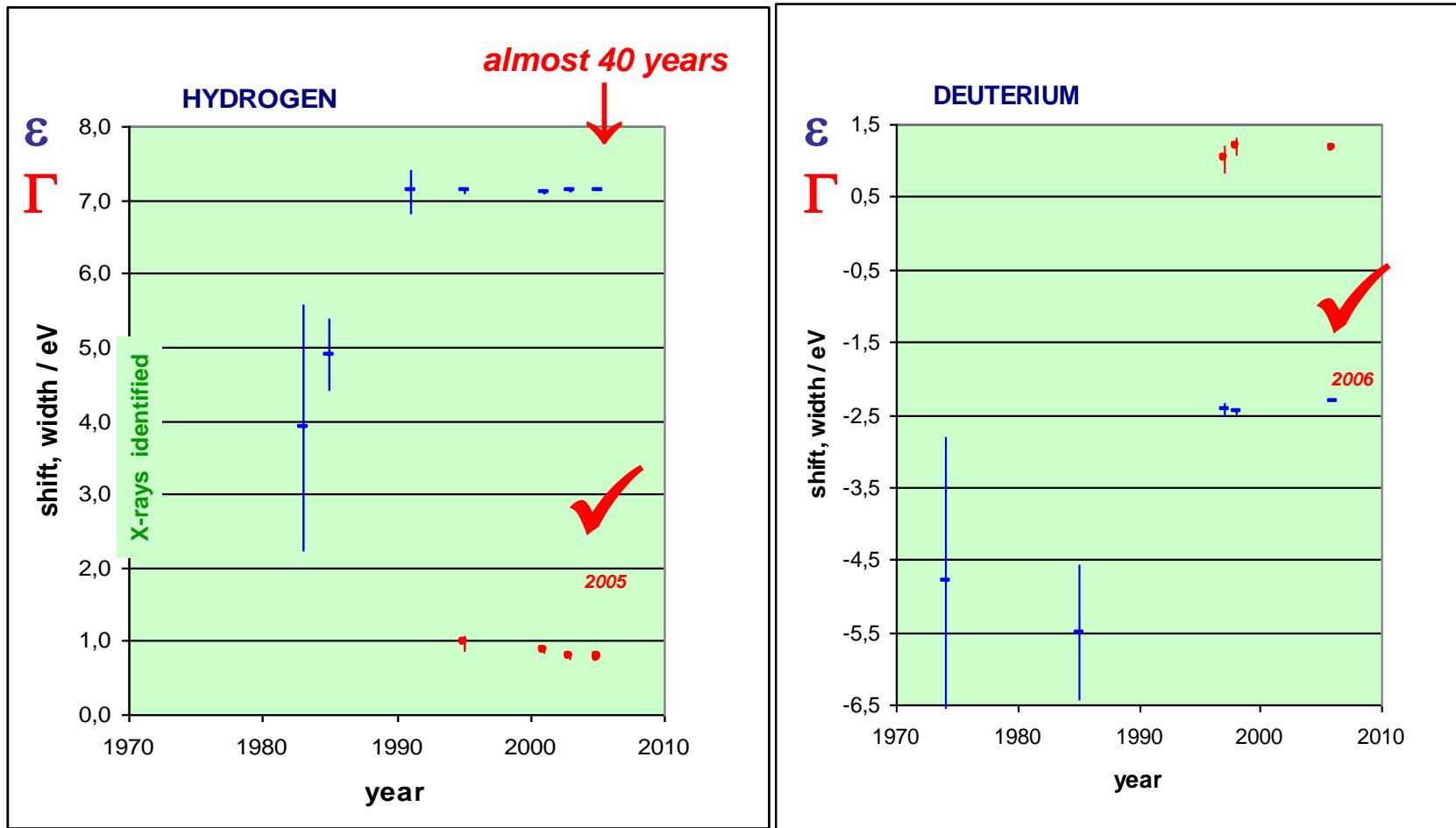
$\varepsilon > 0 (<0) \equiv$ attractive (repulsive) interaction

PROTONIUM - EXPERIMENT

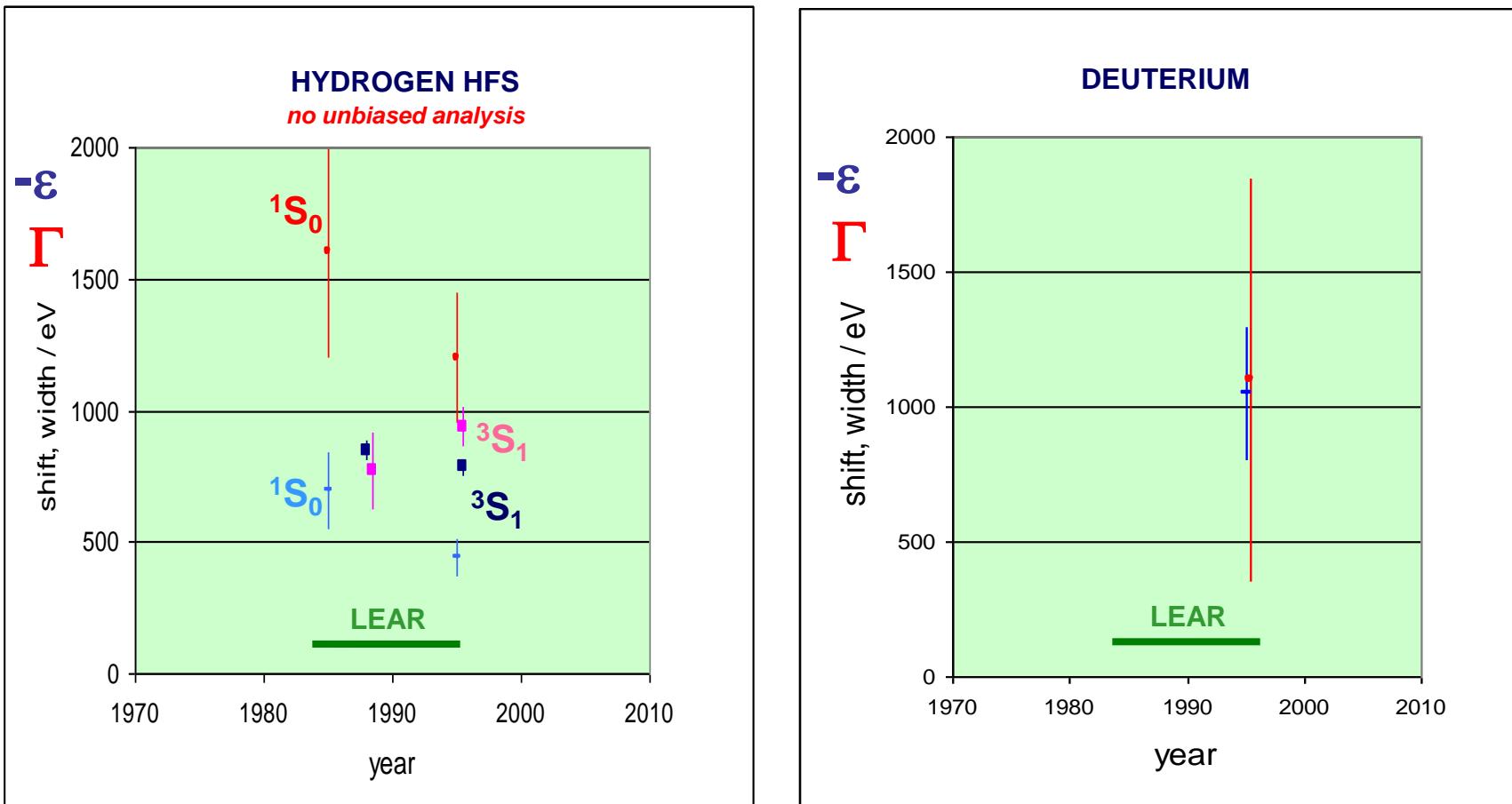


SUMMARY

PIONIC HYDROGEN STORY



ANTIPROTONIC HYDROGEN STORY s -wave



still a lot to do !

