

# Oxygen Isotope Effects in Novel Superconductors

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# Discovery of the isotope effect in mercury

## Isotope Effect in the Superconductivity of Mercury\*

EMANUEL MAXWELL

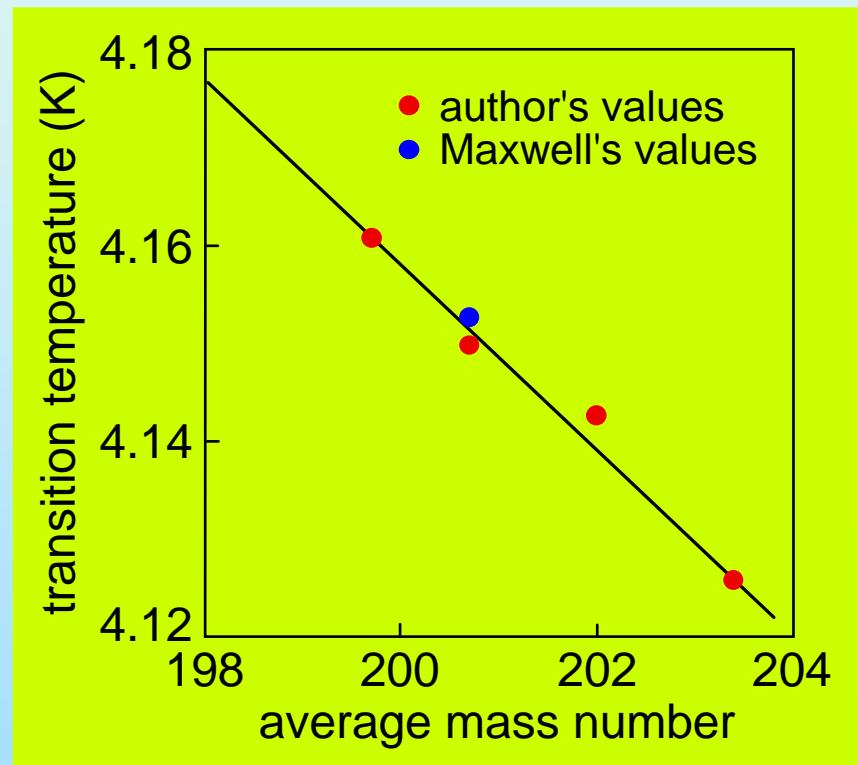
*National Bureau of Standards, Washington, D. C.*  
March 24, 1950

Phys. Rev. 78, 477 (1950)

## Superconductivity of Isotopes of Mercury\*

C. A. REYNOLDS, B. SERIN, W. H. WRIGHT, AND L. B. NESBITT  
*Rutgers University, New Brunswick, New Jersey*  
March 24, 1950

Phys. Rev. 78, 487 (1950)



$$T_c \propto M^{-\alpha} \quad \Rightarrow \quad \alpha = 0.43(6)$$



## The Nobel Prize in Physics 1972

"for their jointly developed theory of superconductivity, usually called the BCS-theory"



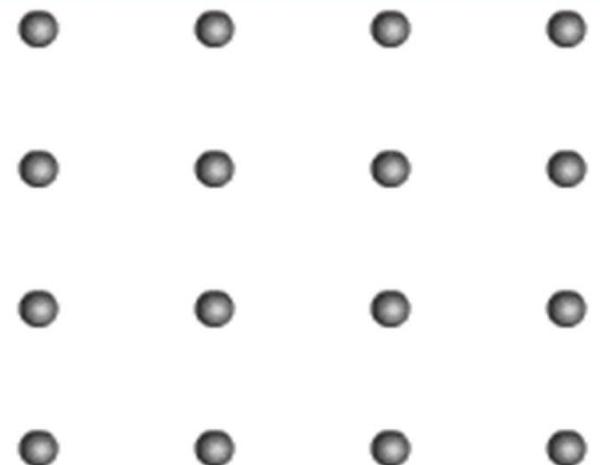
John Bardeen



Leon Neil Cooper

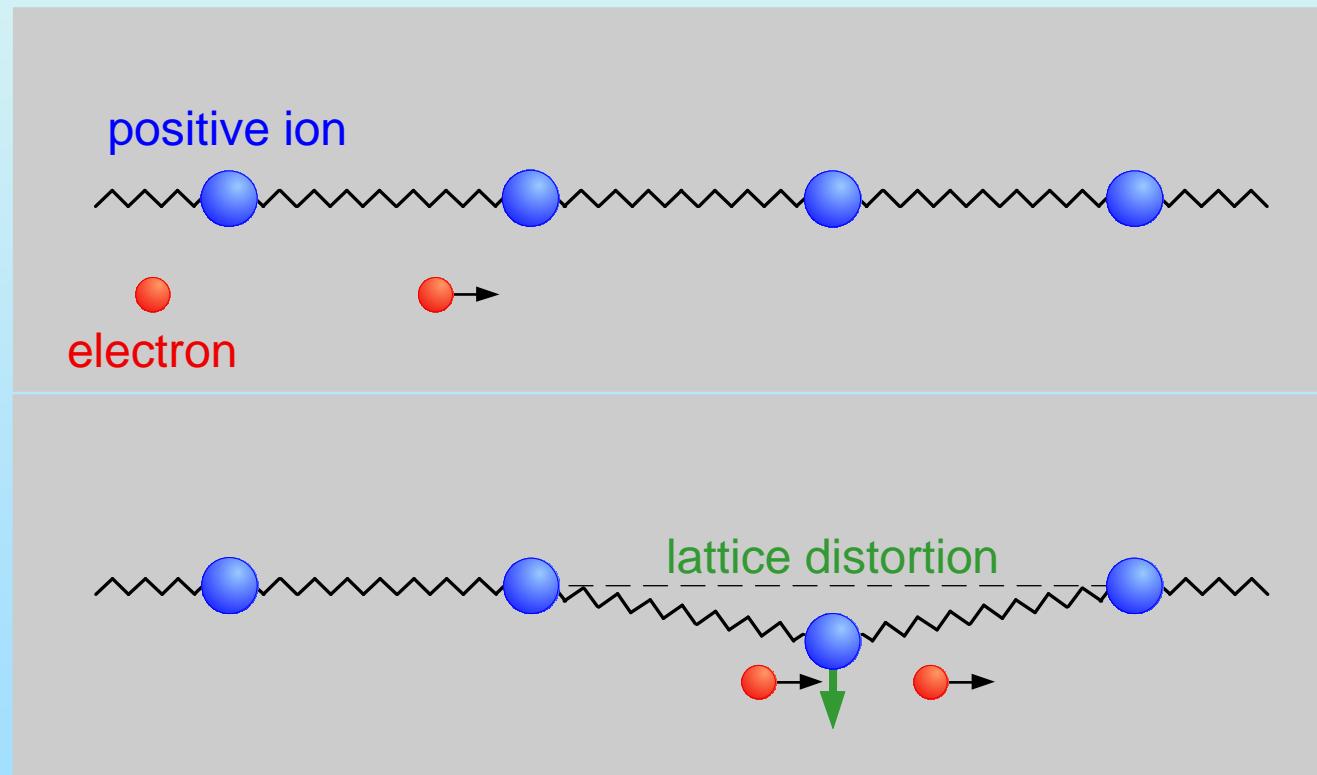


John Robert  
Schrieffer



ზეგამტარობის მექანიზმი :  
ელექტრონების დაწყვილება -  
კუპერის წყვილები

phonons



# Isotope effect

BCS theory (1957)

$$T_c \propto \omega_D \exp(-1/\lambda)$$

$$T_c \propto M^{-\alpha} \quad \alpha = -d \ln T_c / d \ln M$$

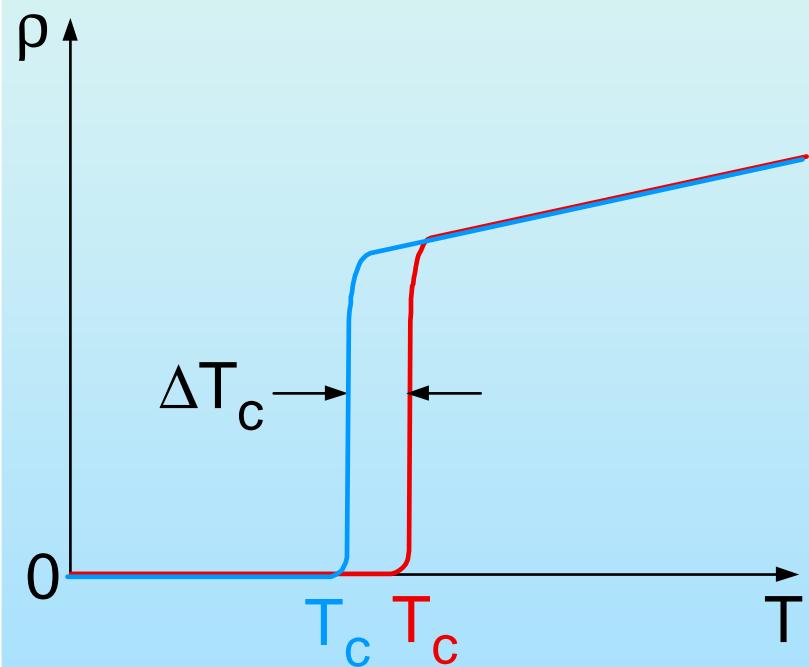
$$\alpha_{BCS} = 1/2$$

$\omega_D$  : typical phonon frequency (Debye frequency)

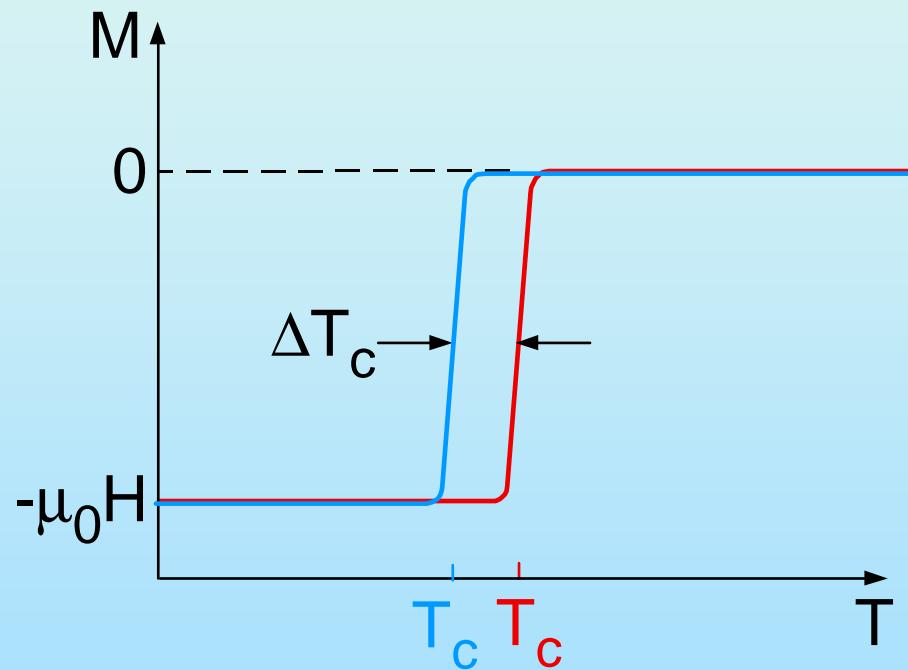
$\lambda$  : electron-phonon coupling constant

## Isotope effect on $T_c$

resistivity  $\rho$



magnetization  $M$



$$M_{\text{blue}} > M_{\text{red}}$$

$$T_c \propto M^{-\alpha}$$

$$\alpha = d \ln T_c / d \ln M$$

# Isotope effect

Experimental results for “simple” metals

Material	Symbol	T <sub>c</sub>	α
Cadmium	Cd	0.5	0.5
Carbon (fullerene)		30	0.25
Lead	Pb	7.2	0.48
Mercury	Hg	4.1	0.5
Molybdenum	Mo	0.9	0.37
Osmium	Os	0.7	0.20
Rhenium	Re	1.7	0.23
Ruthenium	Ru	0.5	0±0.05
Thallium	Tl	2.4	0.50
Tin	Sn	3.7	0.47
Zinc	Zn	0.9	0.45
Zirconium	Zr	0.6	0±0.05

## Theoretical models

**exchange of virtual bosons in a polarizable medium**

pairing  $\Leftrightarrow$  attractive interaction between electrons

$$k_B T_C \approx E_0 \exp(-1/\lambda)$$

$E_0$ : energy scale of the interaction  
 $\lambda$  : coupling constant (weak coupling)

# Theoretical models of superconductivity

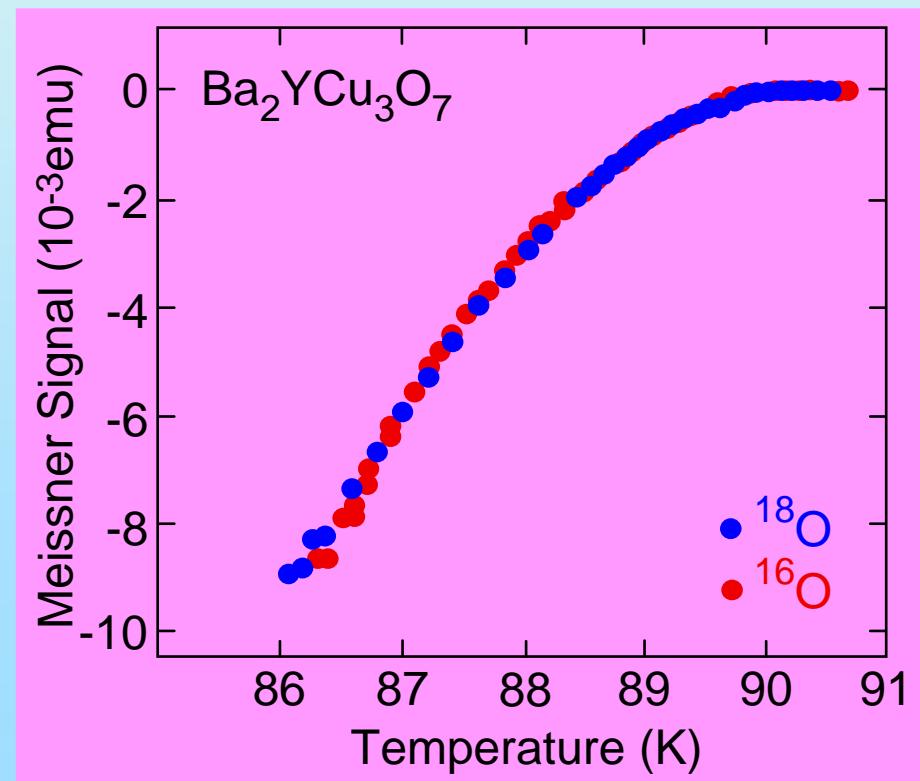
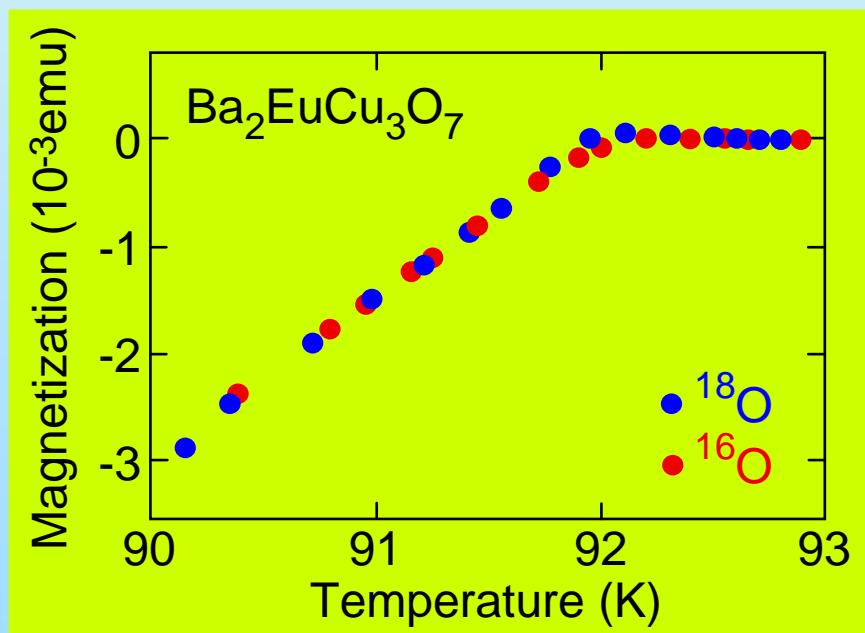
polarizable medium	excitation (virtual boson)	type of carrier
crystal lattice	phonon phonon	electron/ defect electron  polaron (electron + lattice deformation)
electron system	plasmon exziton	electron  electron
spin system	spin fluctuations (magnon)	electron

Isotope Effect in the High- $T_c$  Superconductors  $\text{Ba}_2\text{YCu}_3\text{O}_7$  and  $\text{Ba}_2\text{EuCu}_3\text{O}_7$ 

B.Batlogg, R.J.Cava, A.Jayaraman, R.B.van Dover, G.A.Kourouklis,<sup>(a)</sup>S.Sunshine, D.W.Murphy,  
L.W.Rupp, H.S.Chen, A.White, K.T.Short, A.M.Mujsce, and E.A.Rietman

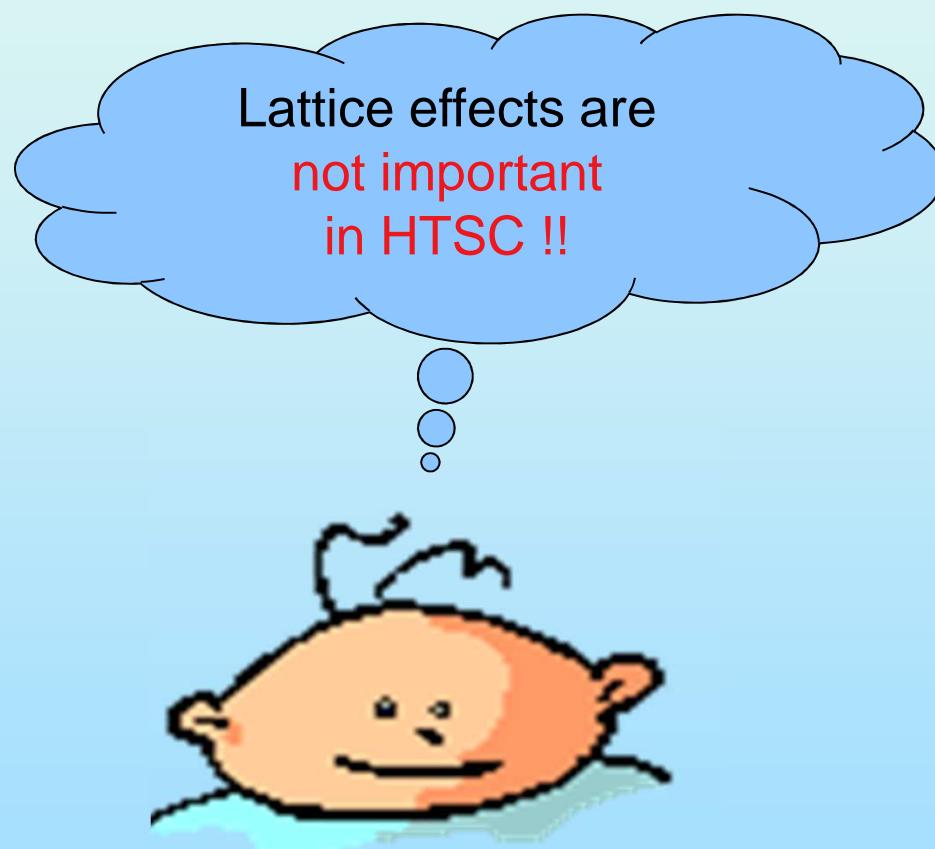
AT&T Bell Laboratories, Murray Hill, New Jersey 07974

(Received 24 April 1987)



## Oxygen-isotope effect on $T_c$ in $\text{YBa}_2\text{Cu}_3\text{O}_7$ : Early results

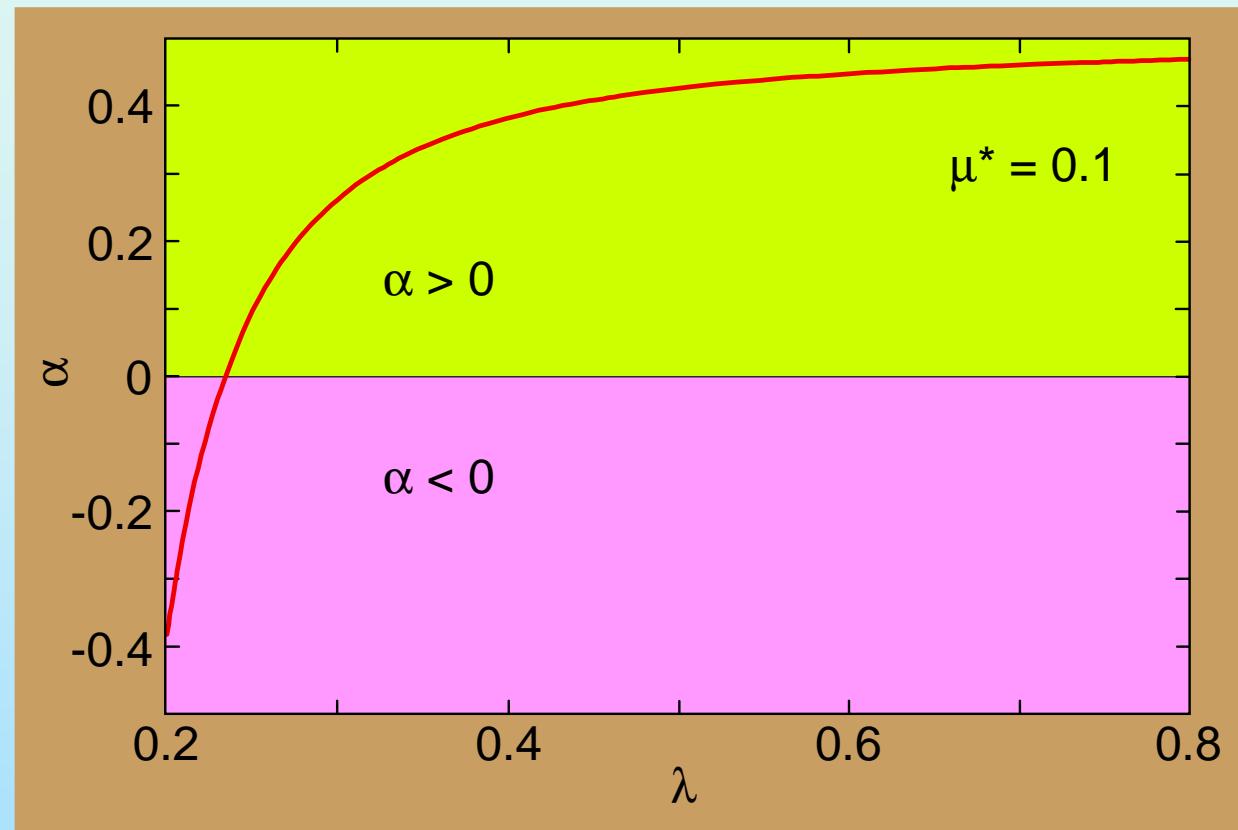
System	$T_c$ (K)	$^{18}\text{O}$ (%)	$\Delta T_c$ (K)	$\alpha_o$	Reference
$\text{YBa}_2\text{Cu}_3\text{O}_7$	92.1	75	< 0.1	$0 \pm 0.02$	Batlogg et al. (1987)
$\text{EuBa}_2\text{Cu}_3\text{O}_7$	92.15	75	< 0.1	$0 \pm 0.02$	Batlogg et al. (1987)
$\text{YBa}_2\text{Cu}_3\text{O}_7$	90.0	(90)	< 0.3	$0 \pm 0.027$	Bourne et al. (1987)
$\text{YBa}_2\text{Cu}_3\text{O}_7$	92.1	90	0.5	$0.05$	Leary et al. (1987)
	91.4	75	0.3	$0.04$	
	91.5	73	0.4	$0.05$	



Is this correct?

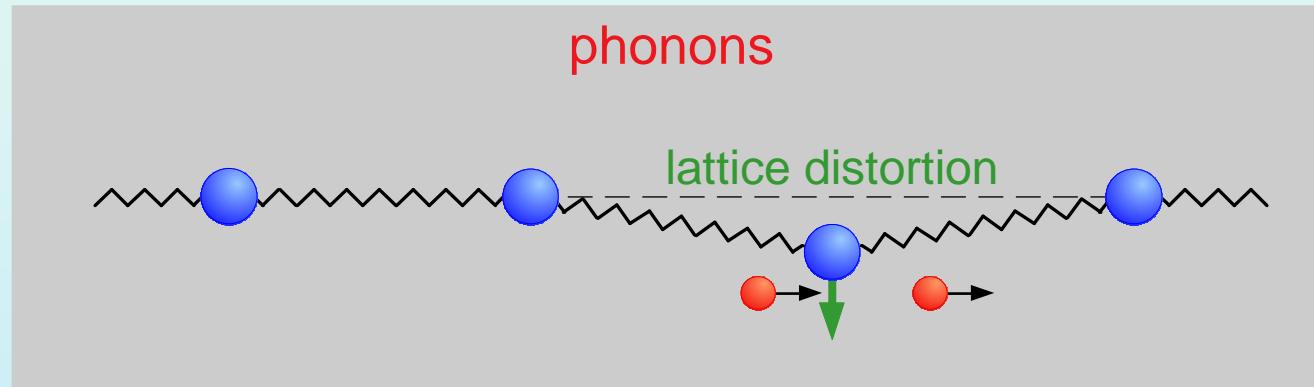
- Isotope effect is **small** ⇒ electron-phonon interaction is **not important**
- Isotope effect is **large** ⇒ electron-phonon interaction is **very important**
- Need reliable experiments and adequate theory to answer this question!

## Isotope effect exponent $\alpha$

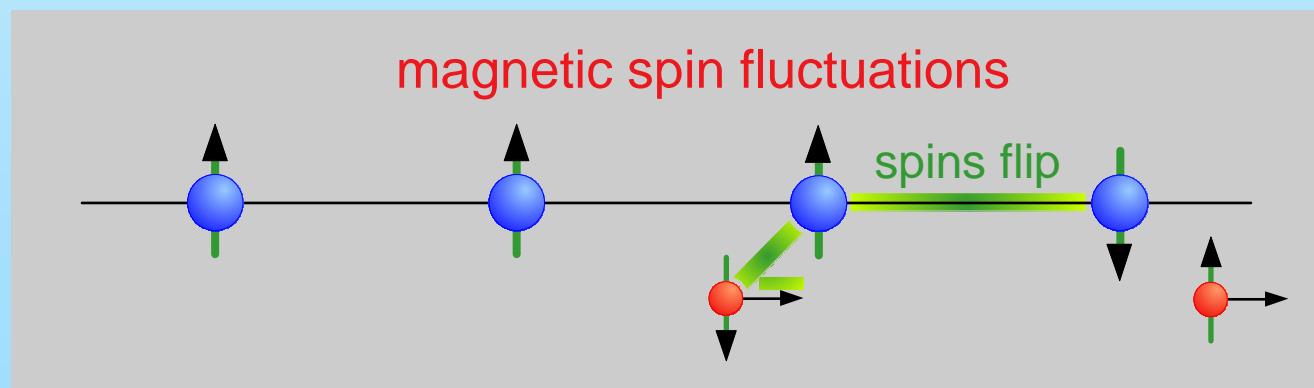


$$\alpha = \frac{1}{2} \left( 1 - \frac{(1+\lambda)(1+0.62\lambda)\mu^{*2}}{[\lambda-\mu^*(1+0.62\lambda)]^2} \right)$$

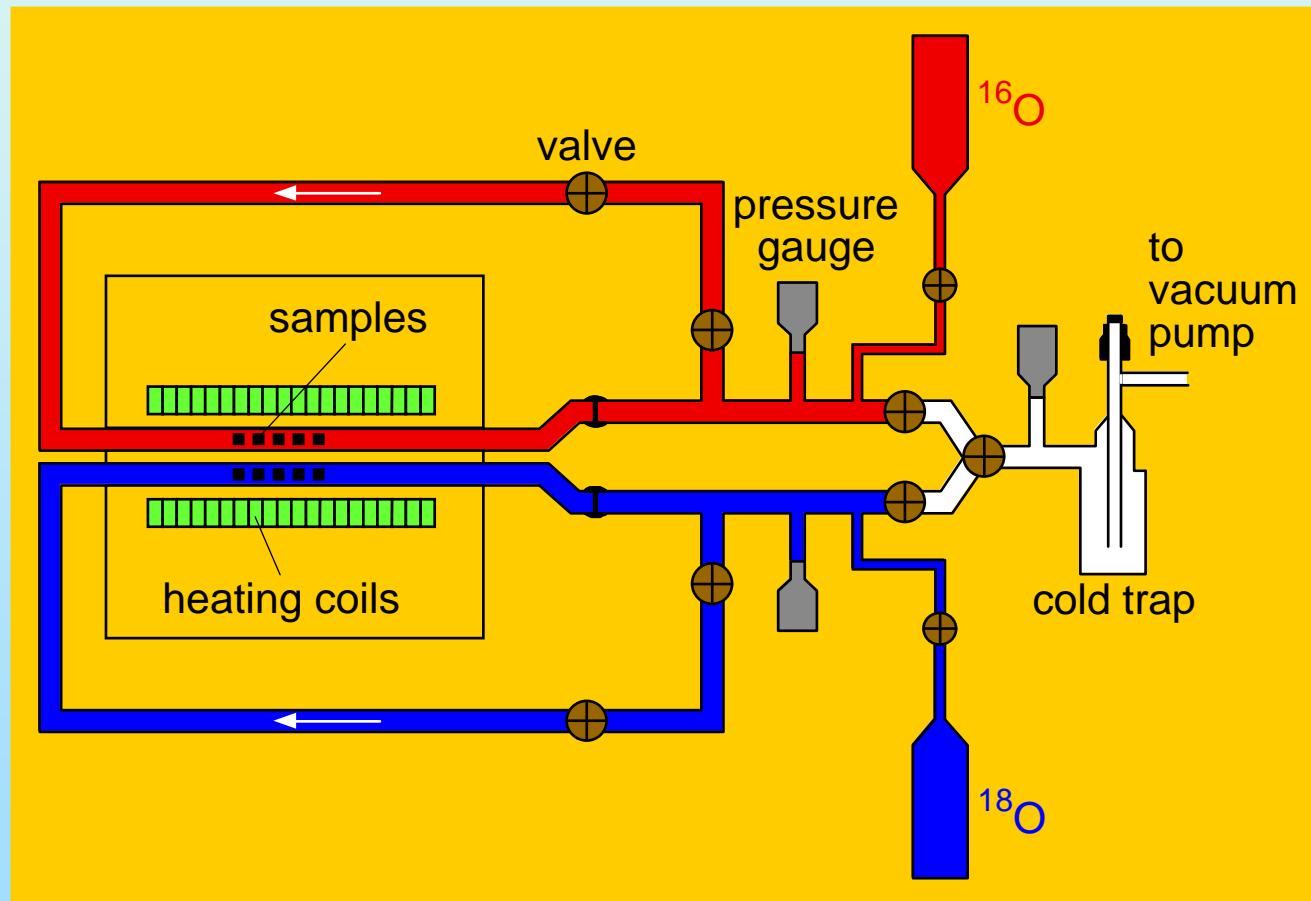
Mc Millan, Phys. Rev. 167, 331 (1968)



and/or ?

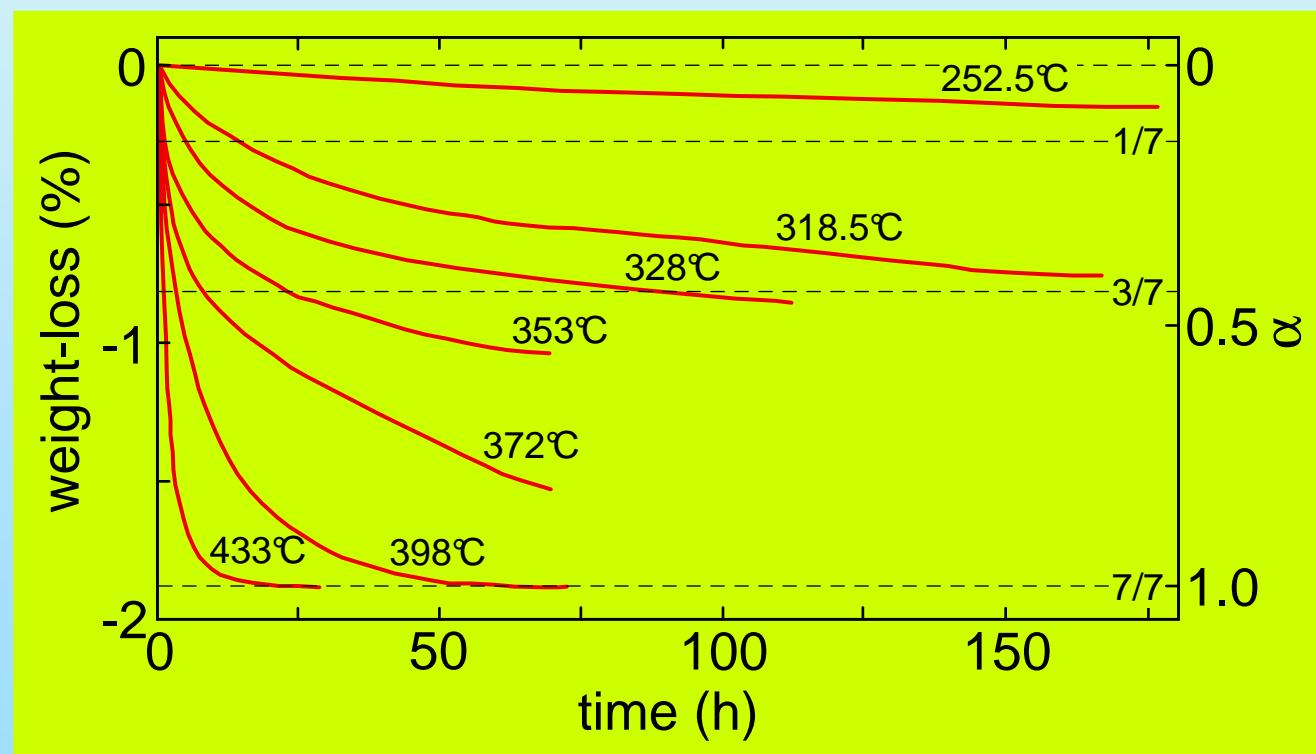


# Experimental set-up for the preparation of $^{16}\text{O}/^{18}\text{O}$ samples

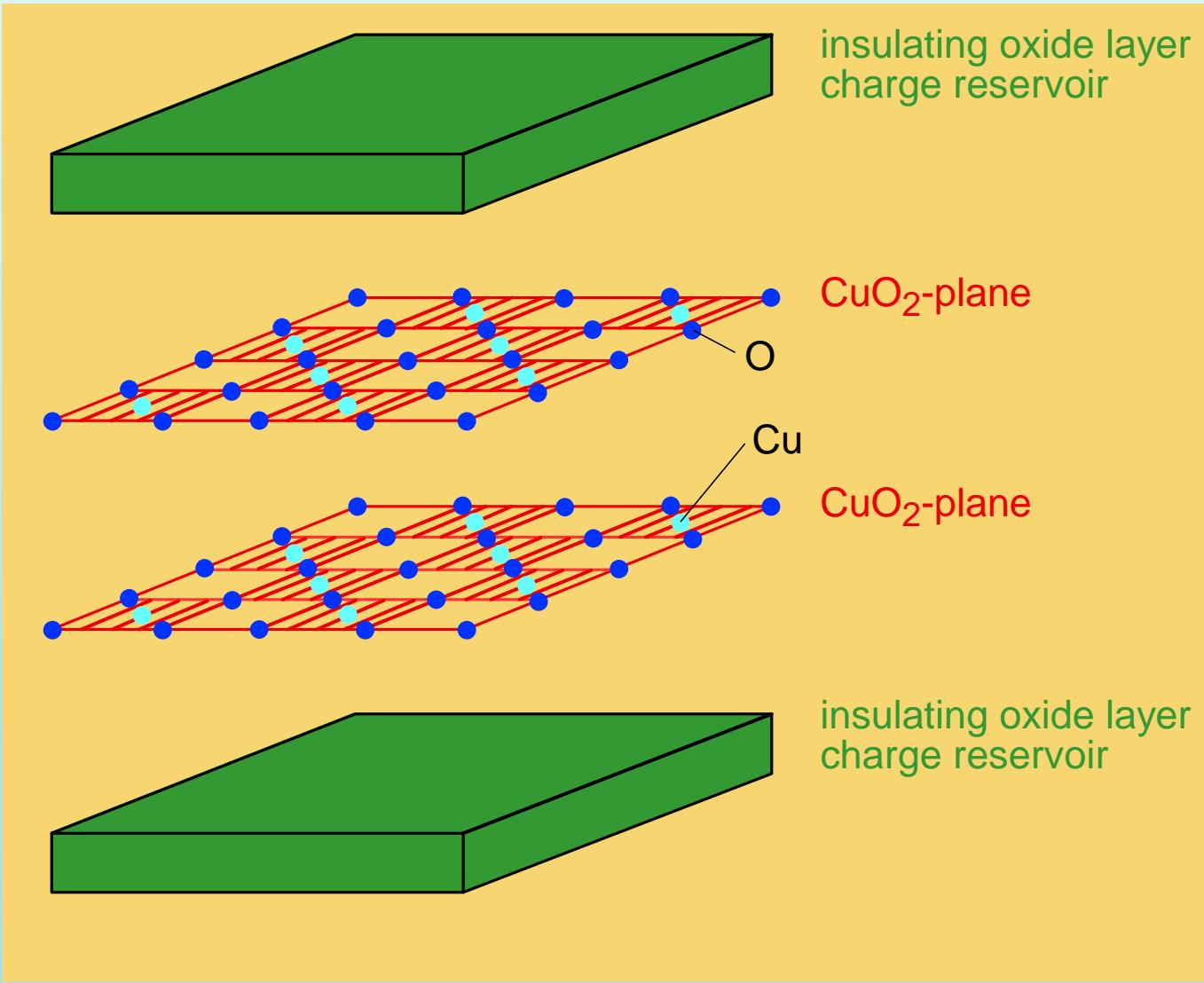


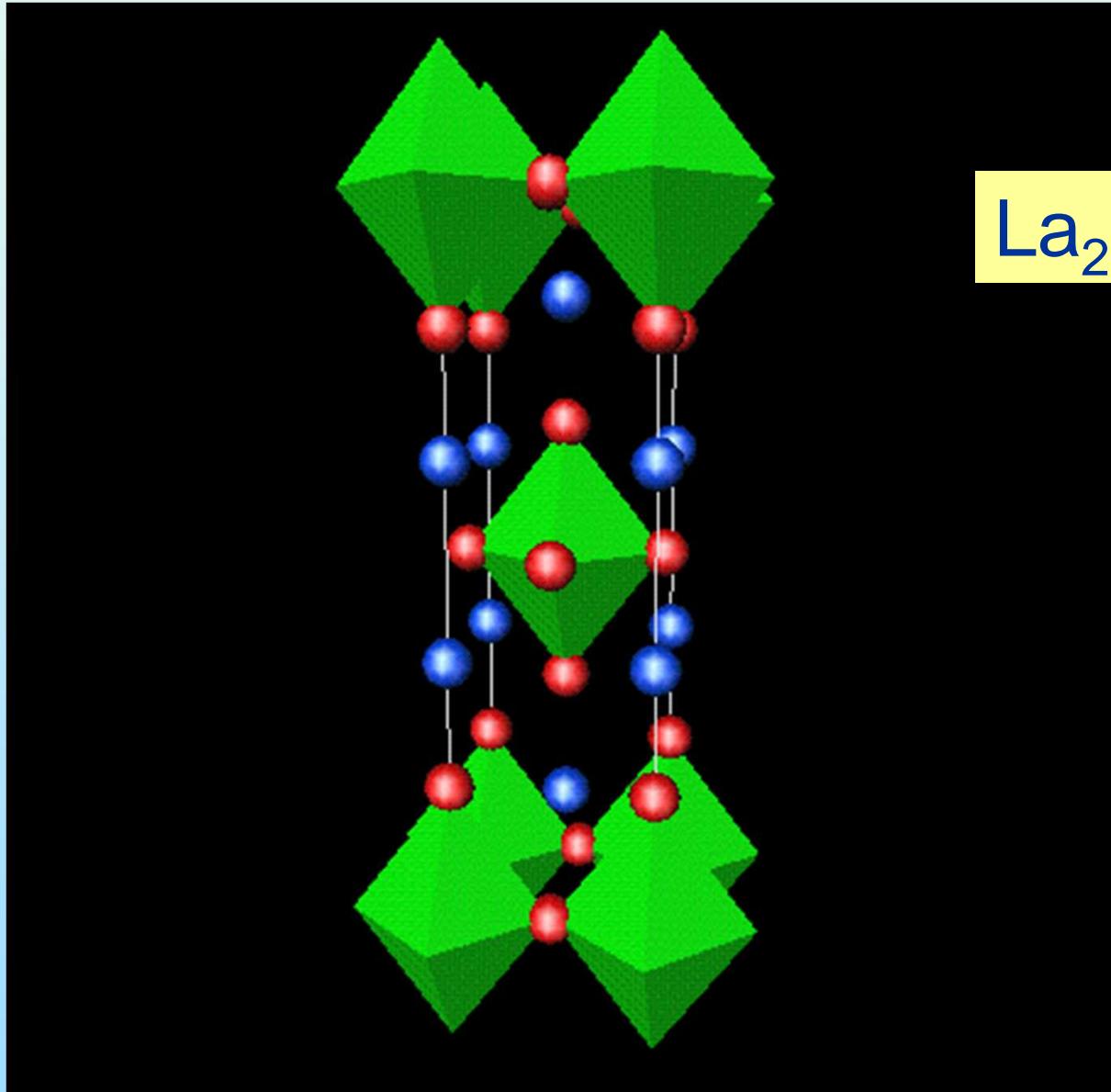
## Experimental set-up for the preparation of $^{16}\text{O}/^{18}\text{O}$ samples

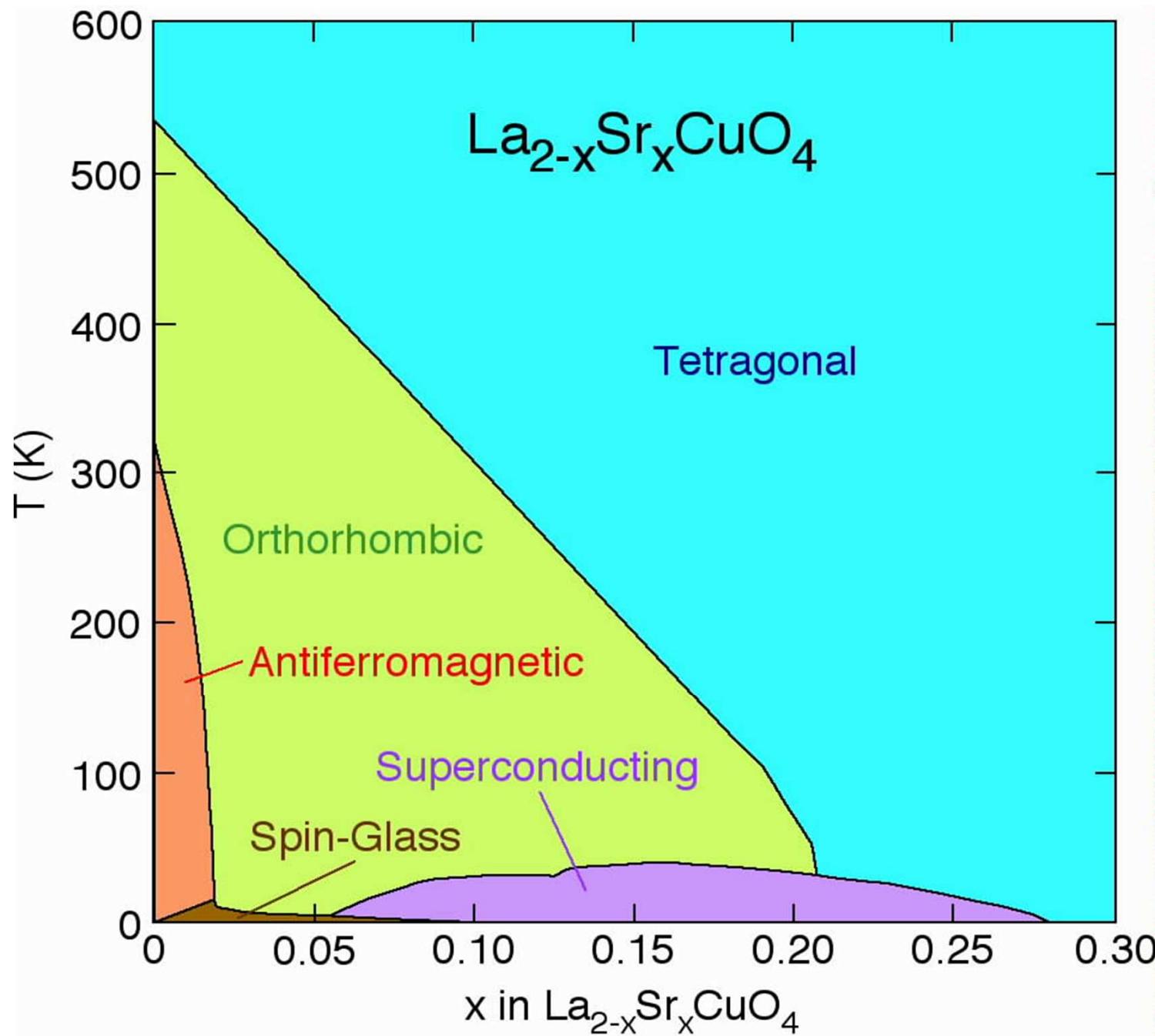
Thermogravimetric curves during isothermal oxygen exchange in Y123 substituted with  $^{18}\text{O}$



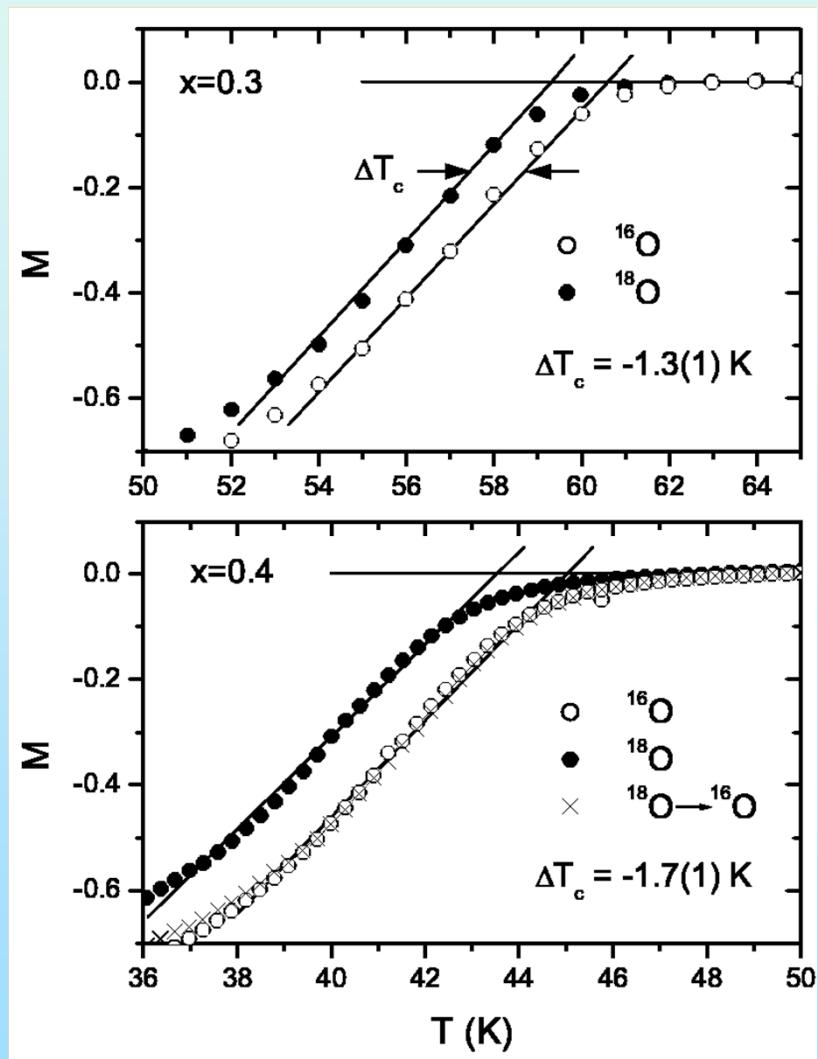
## Schematic structure of cuprate superconductors





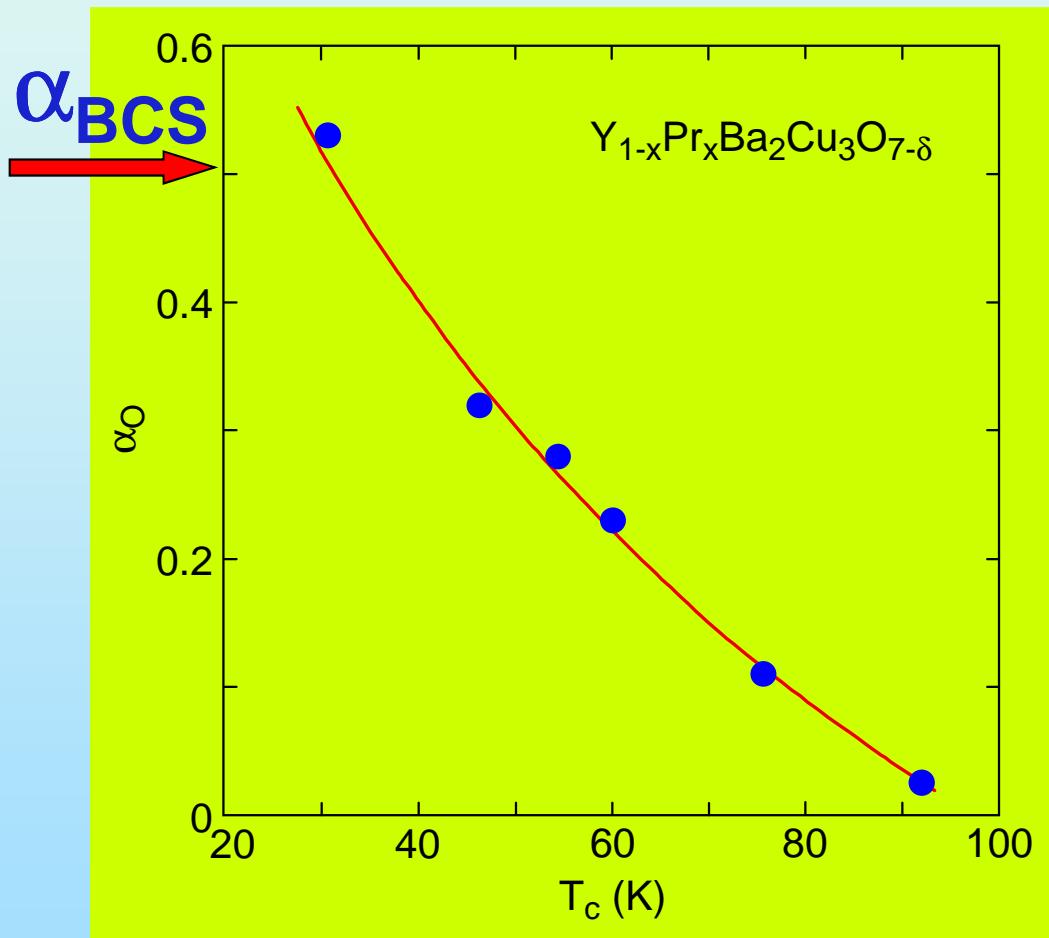


## $\text{Y}_{1-x}\text{Pr}_x\text{Ba}_2\text{Cu}_3\text{O}_{7-\delta}$



Normalized magnetization curves:  
1 mT, field cooled

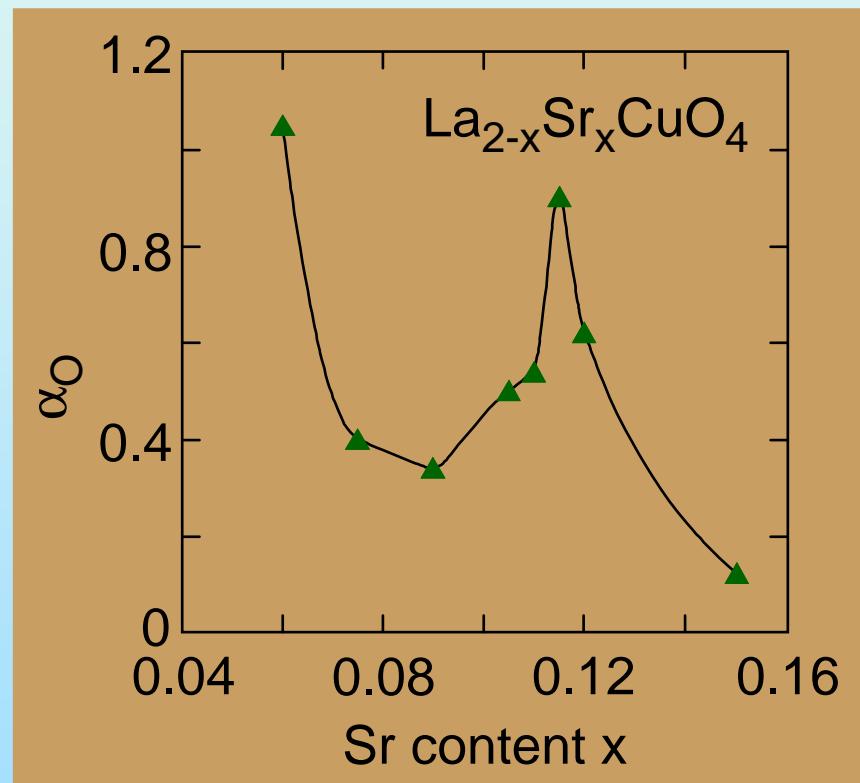
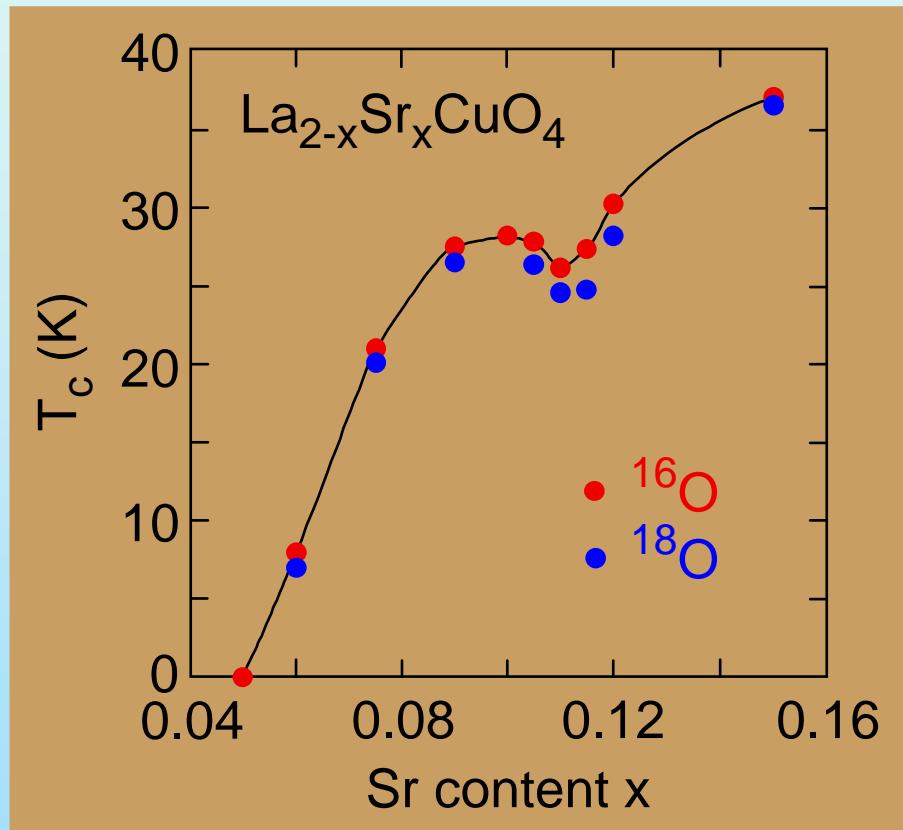
## Oxygen-Isotope Effect on $T_c$



$$\alpha_O = - \frac{\Delta T_c / T_c}{\Delta M_O / M_O}$$

Franck et al., Phys.Rev. B **44**, 5318 (1991)

## OIE on $T_c$ in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$

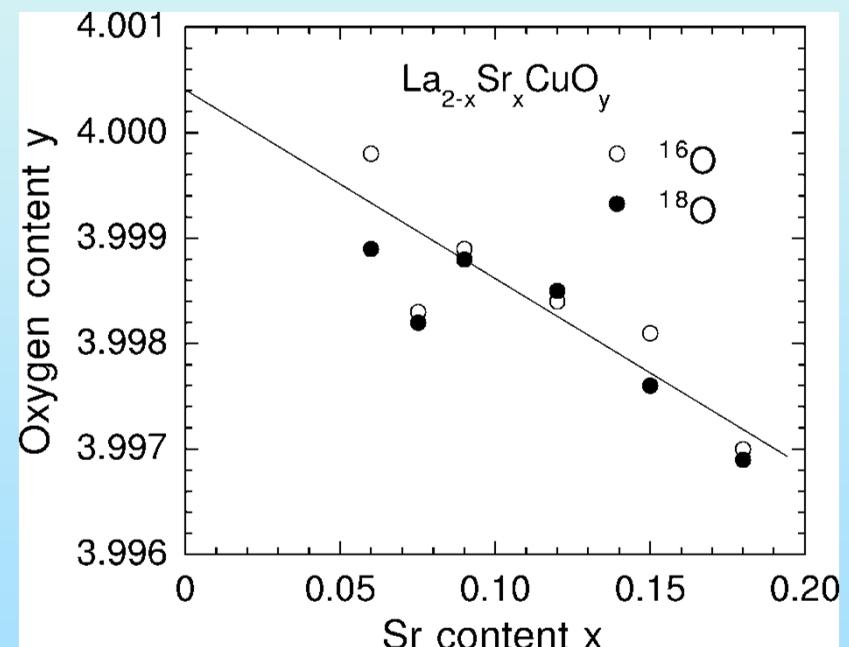


Zhao *et al.*, Nature **385**, 236 (1997)

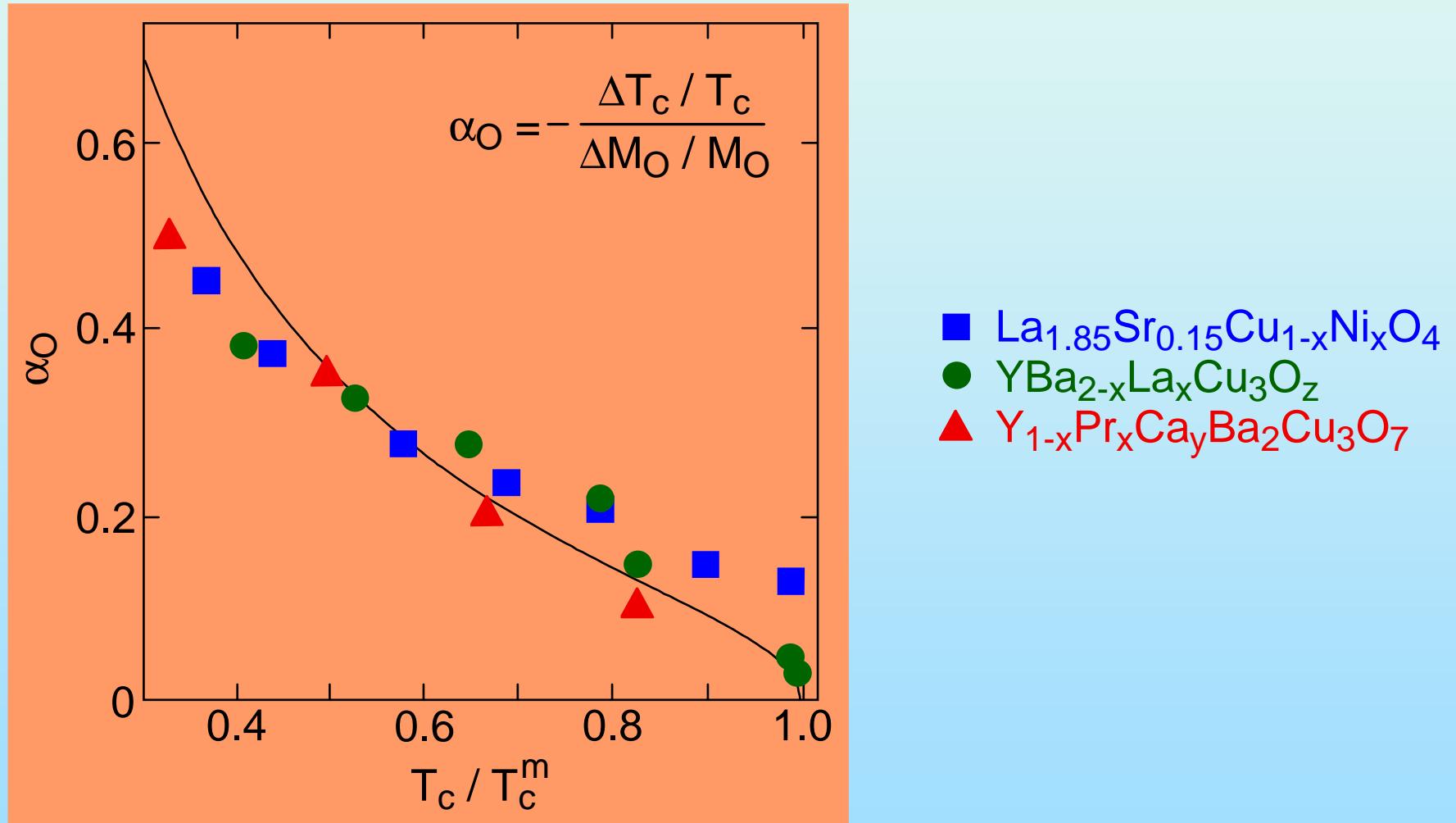
Zhao *et al.*, J. Phys.: Condens. Matter **10**, 9055 (1998)

## Precise volumetric analysis of the oxygen content in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_y$

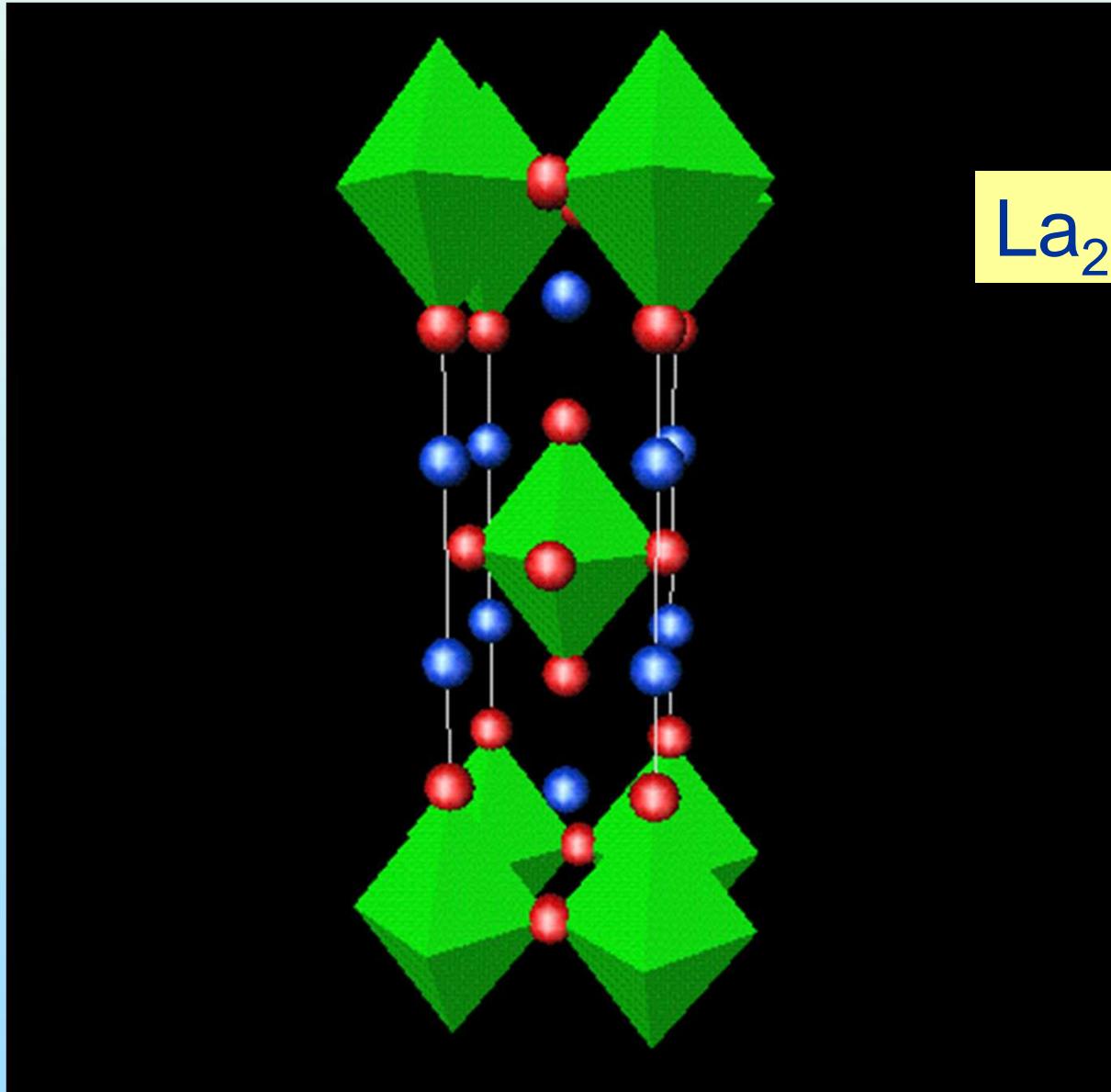
- Very accurate determination of the oxygen content usig a precise volumetric analysis
- Oxygen contents of sample pairs ( $^{16}\text{O}/^{18}\text{O}$ ) with identical x are the same within  $\pm 0.0002$  per Cu site
- $\Rightarrow$  difference in hole densities of the  $^{16}\text{O}$  and  $^{18}\text{O}$  samples is negligible
- $\Rightarrow$  large observed OIE are intrinsic



## Oxygen-isotope effect on $T_c$

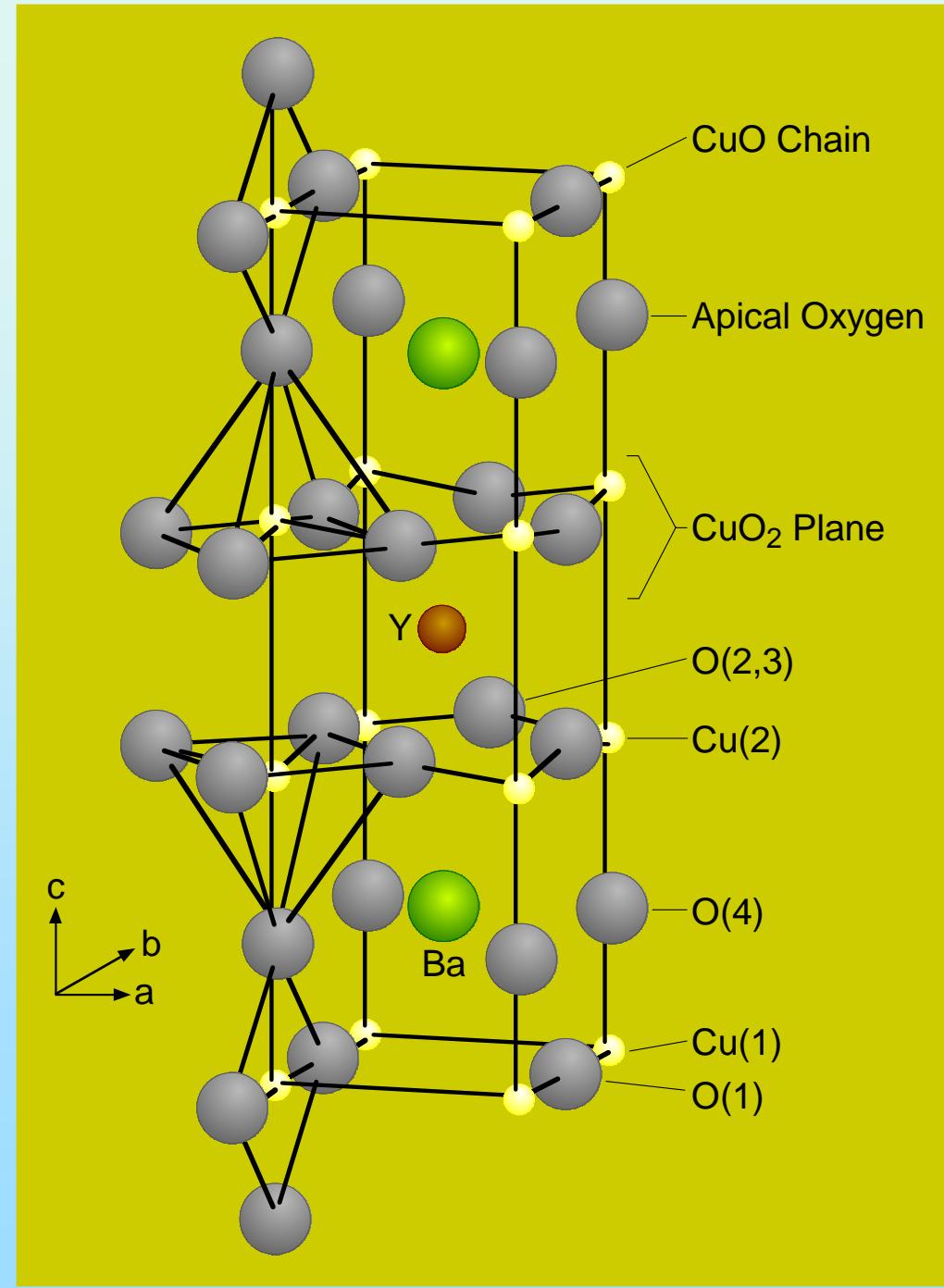


Schneider and Keller, PRL. **69**, 3374 (1992)

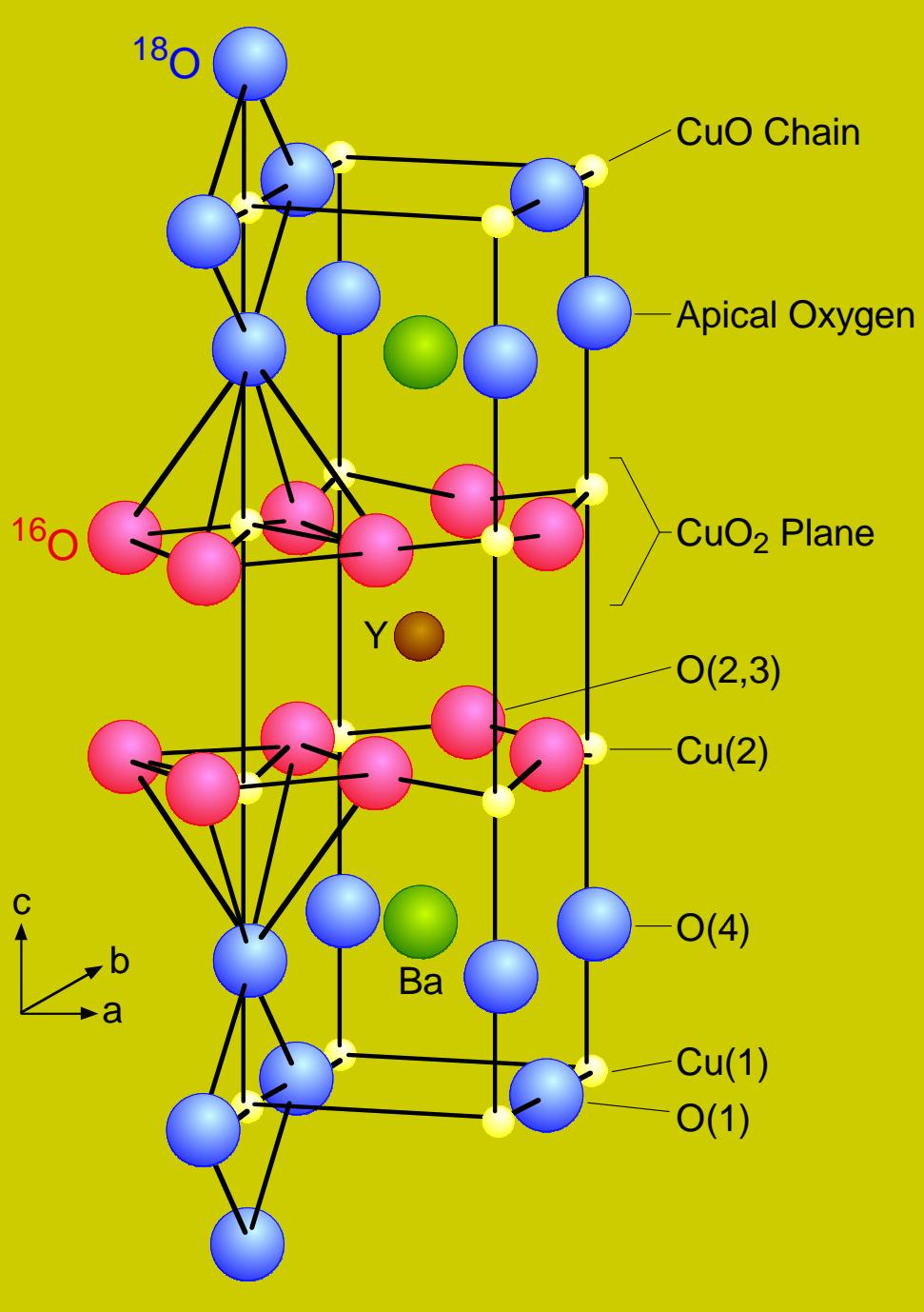


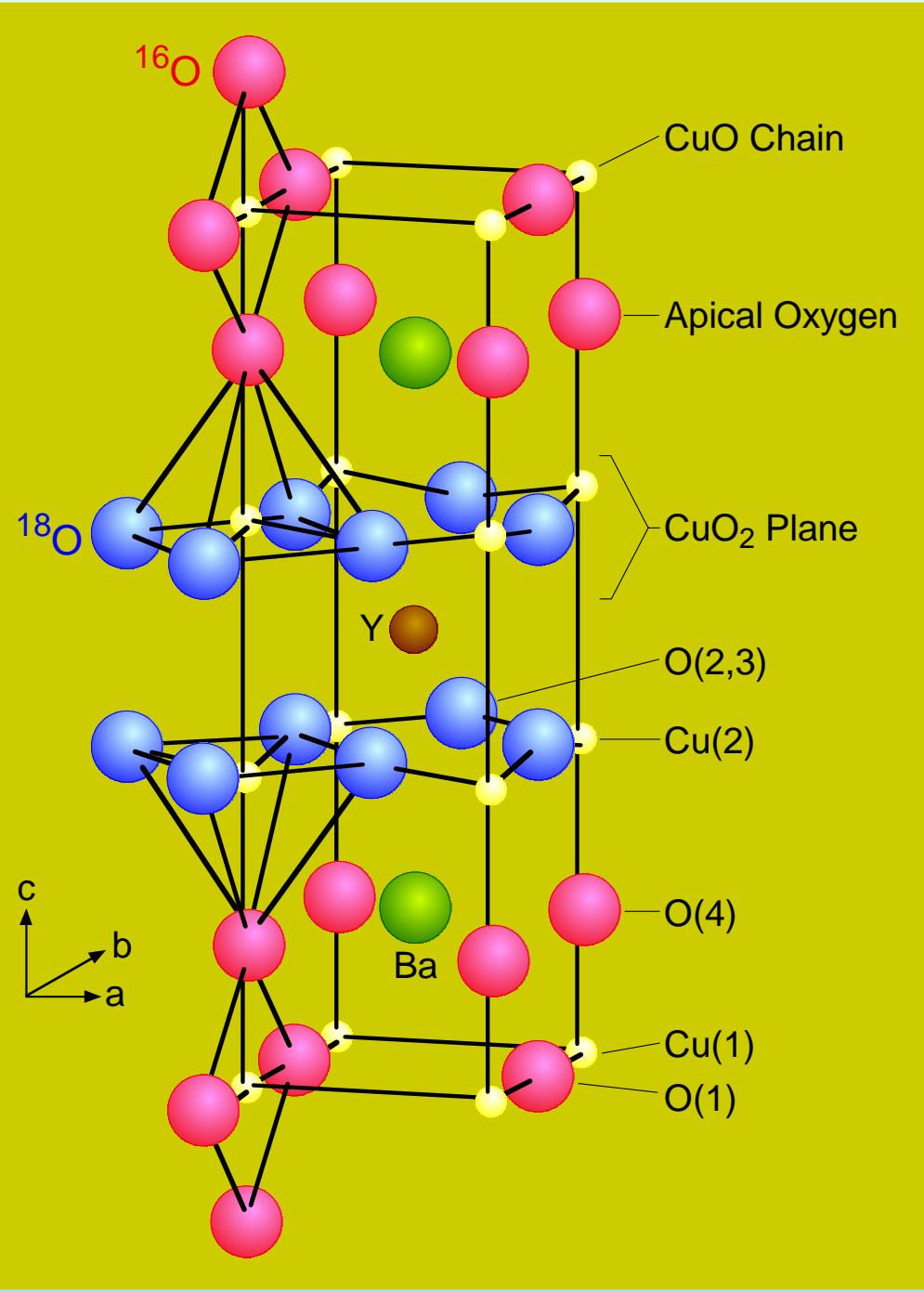
**Site-selective oxygen-isotope effect experiment ?**

# Structure of $\text{YBa}_2\text{Cu}_3\text{O}_x$

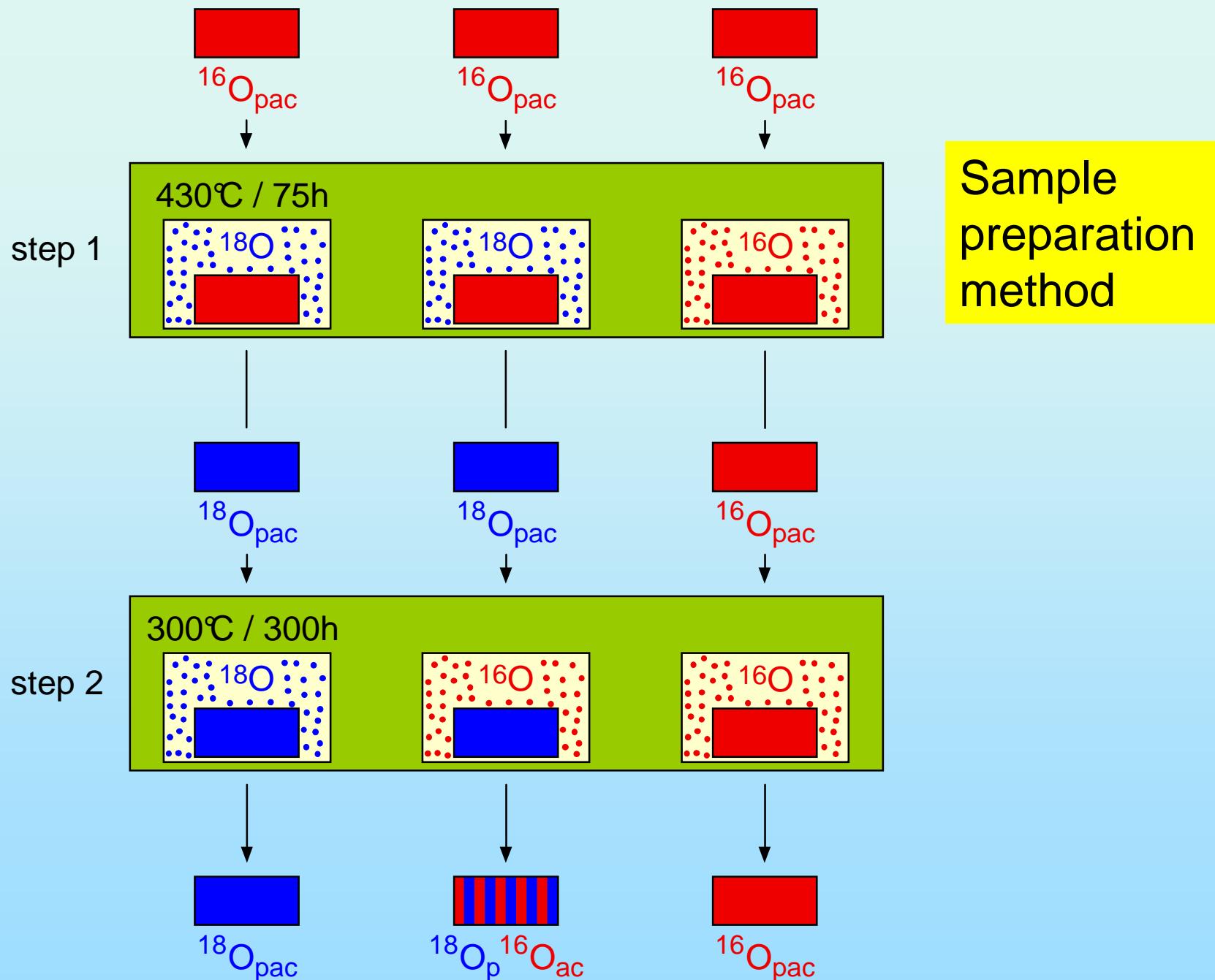


# Structure of $\text{YBa}_2\text{Cu}_3\text{O}_x$





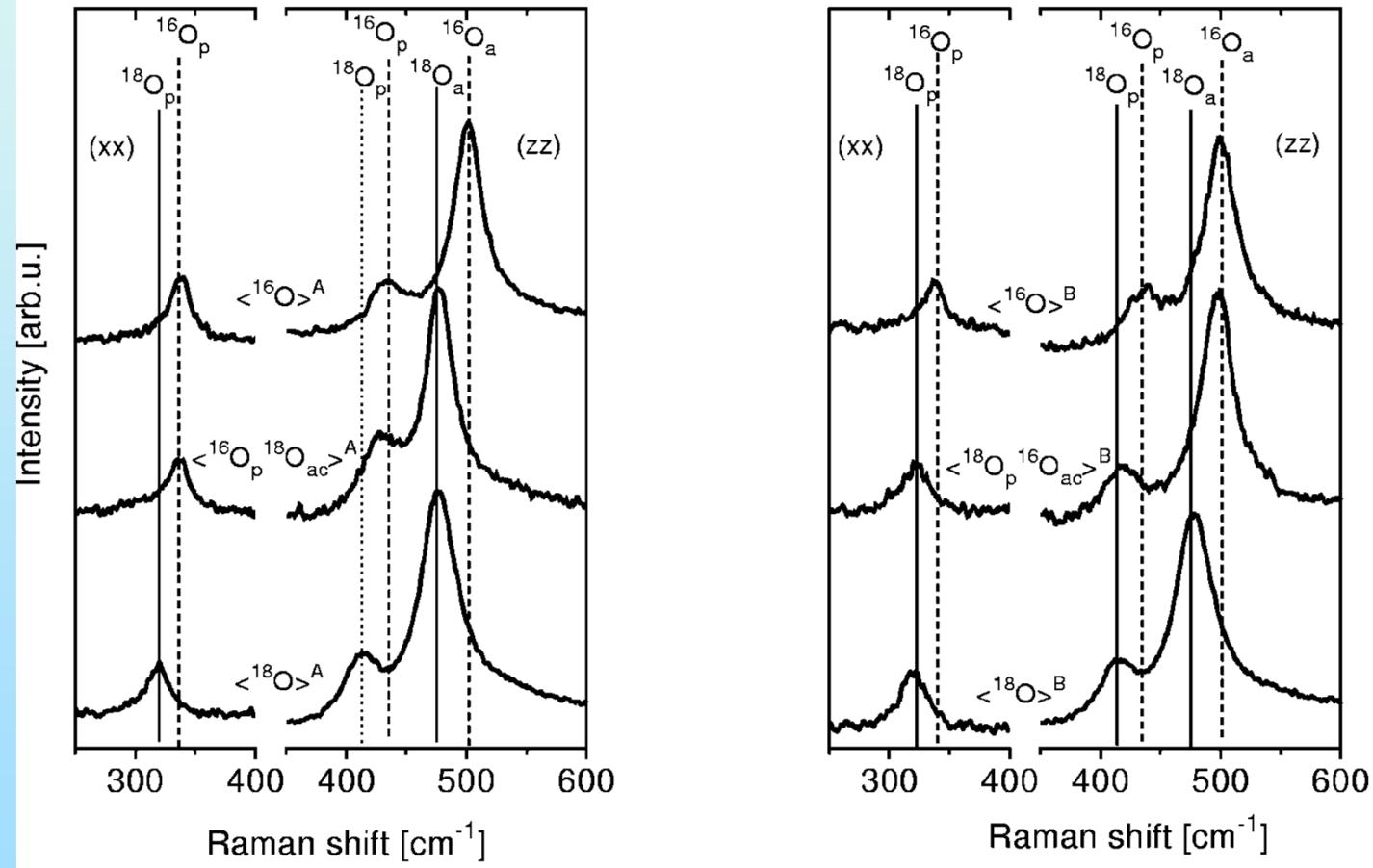
## Structure of $\text{YBa}_2\text{Cu}_3\text{O}_x$



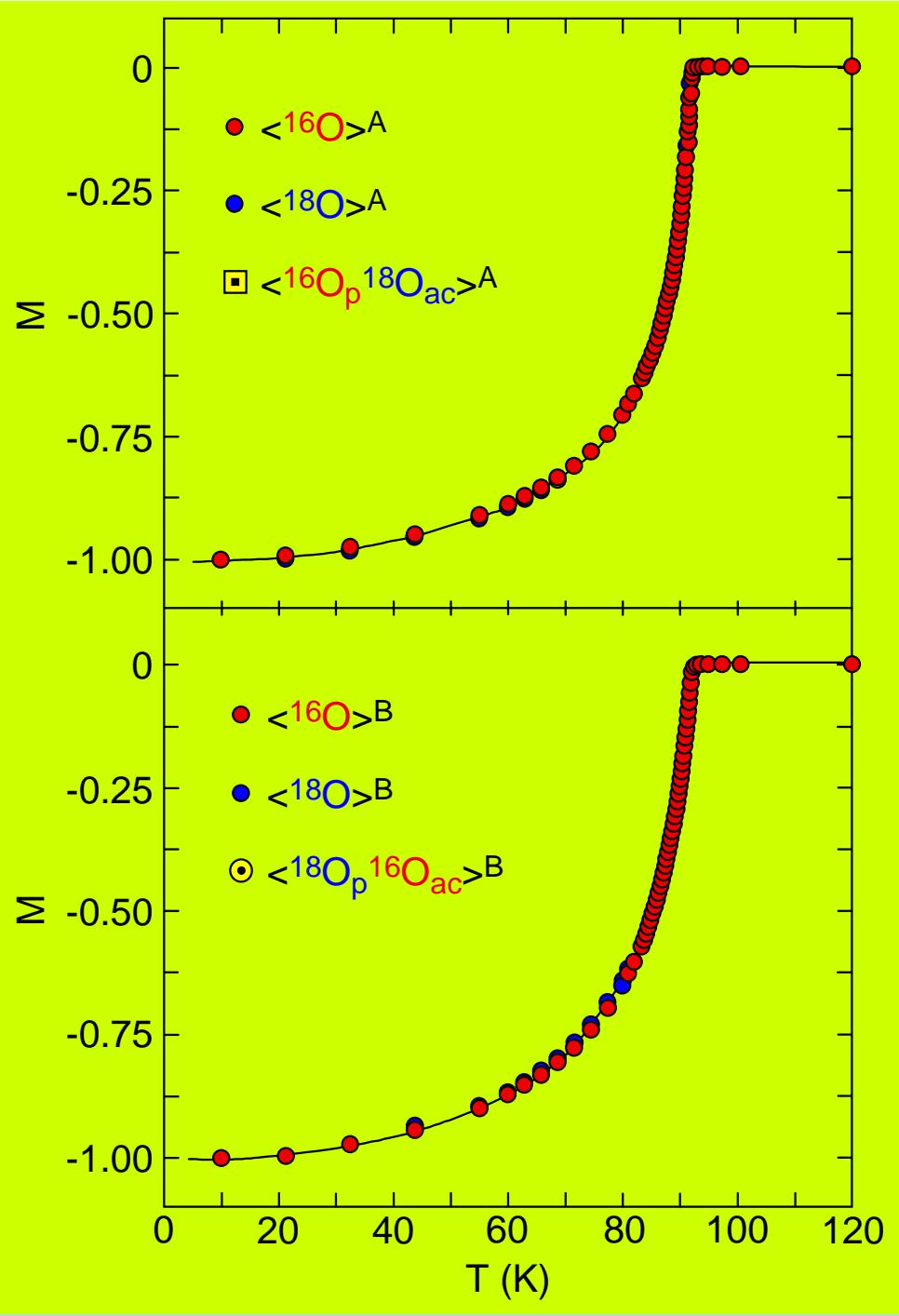
Zech *et al.*, "Anharmonic Properties of High- $T_c$  Cuprates" (1994)

# Raman spectra of $\text{YBa}_2\text{Cu}_3\text{O}_x$

⇒ test of site-selective  $^{16}\text{O}/^{18}\text{O}$  exchange

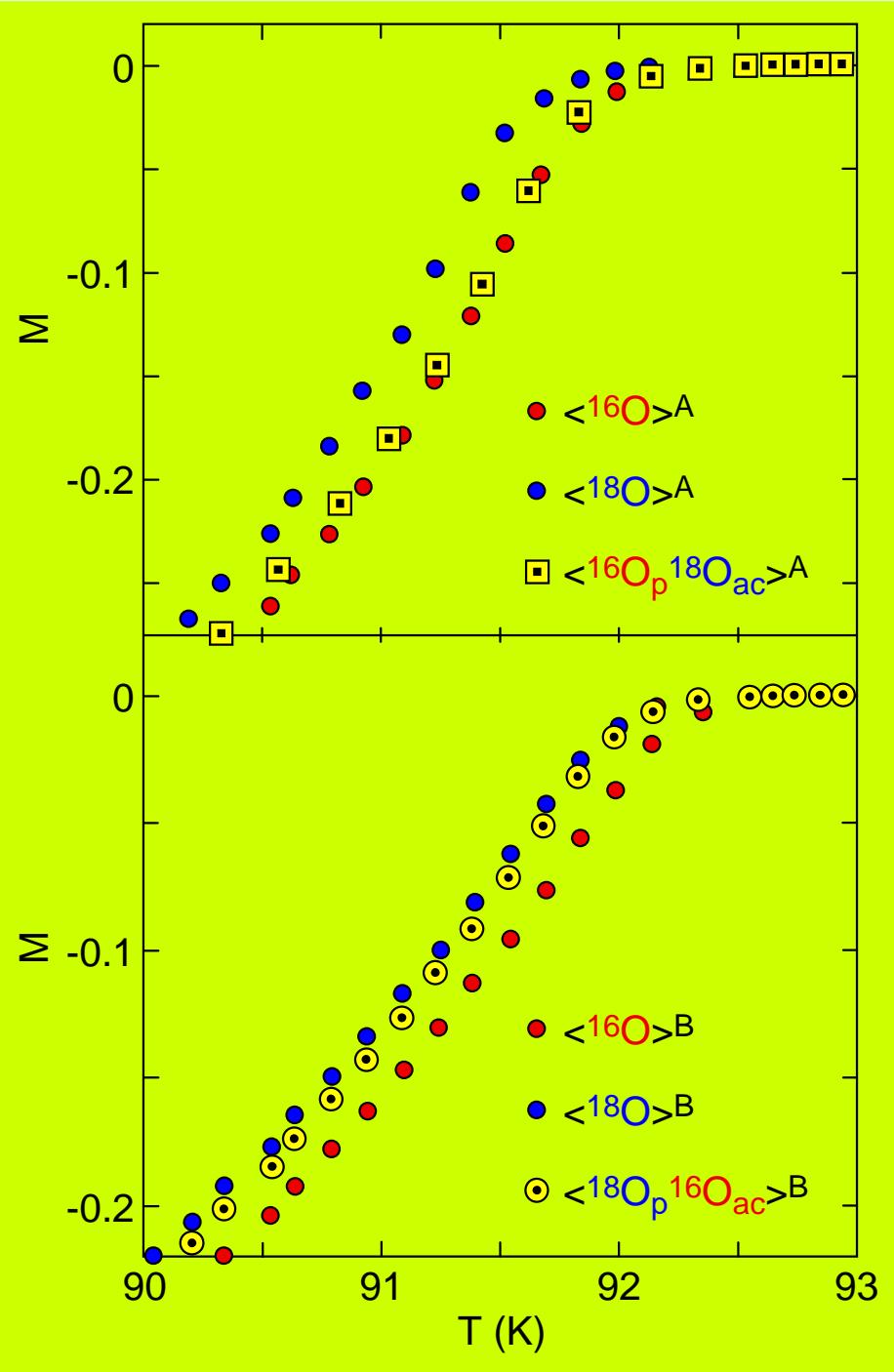


Zech *et al.*, Nature 371, 681 (1994)



Site-selective oxygen isotope effect  
in optimally doped  $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$

Zech *et al.*, Nature 371, 681 (1994)

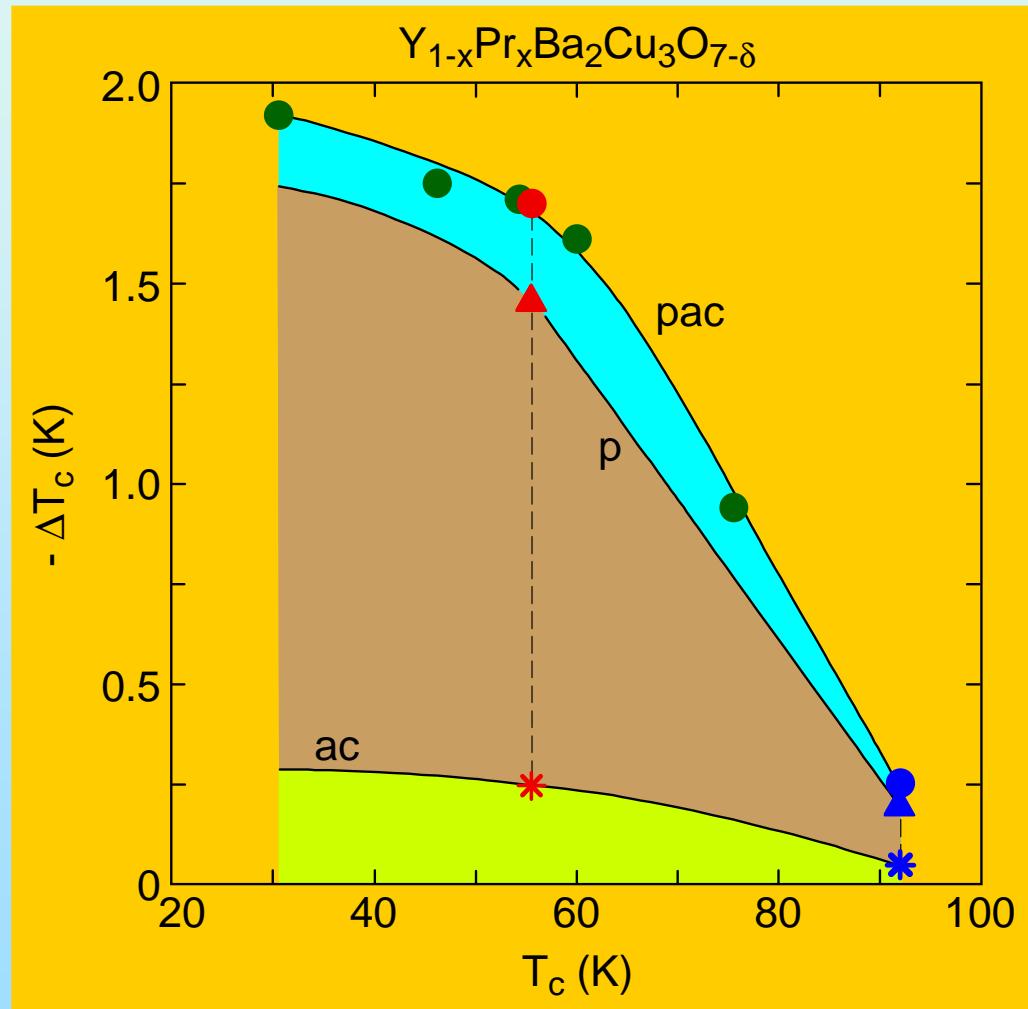


Site-selective oxygen isotope effect  
in optimally doped  $\text{YBa}_2\text{Cu}_3\text{O}_{6+\chi}$

⇒ planar oxygen atoms mainly (> 80 %)  
contribute to the total OIS

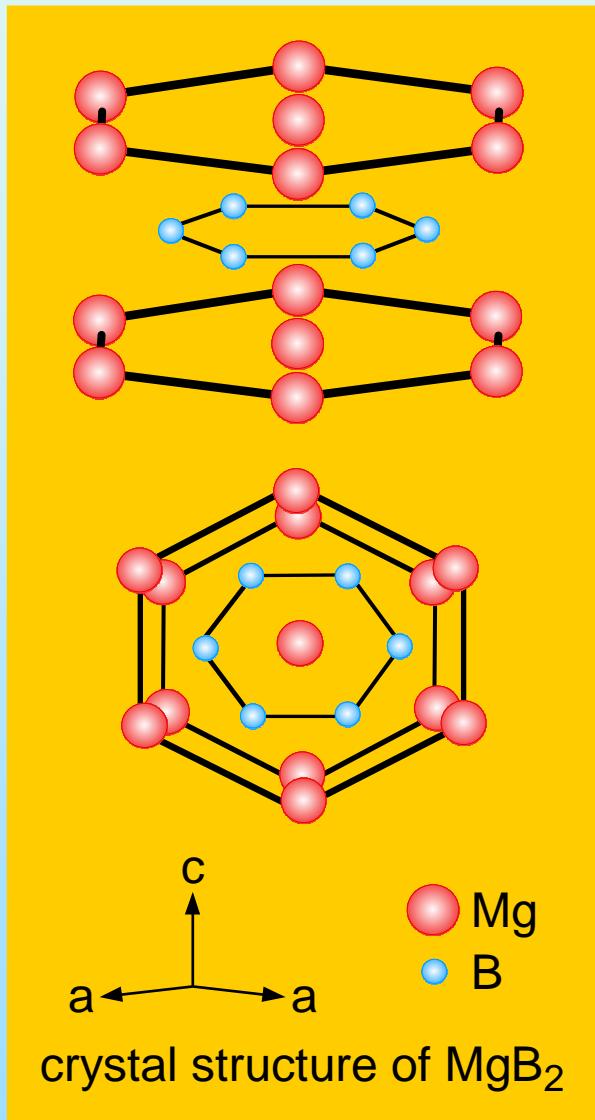
Zech *et al.*, Nature 371, 681 (1994)

## Oxygen-Isotope Effect on $T_c$

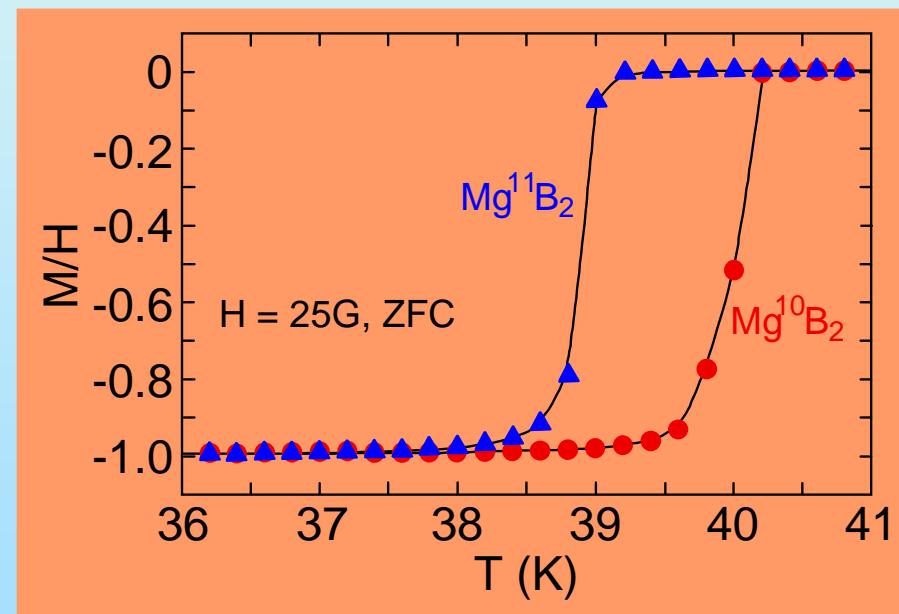


- ac : apical and chain oxygen
  - p : plane oxygen
  - pac : plane, apical and chain oxygen
- Franck *et al.*, Phys.Rev. B **44**, 5318 (1991)
- ▲ \* Zech *et al.*, Nature **371**, 681 (1994)
- ▲ \* Zhao *et al.*, Phys.Rev. B **54**, 14982 (1996)

# Boron isotope effect in superconducting MgB<sub>2</sub>

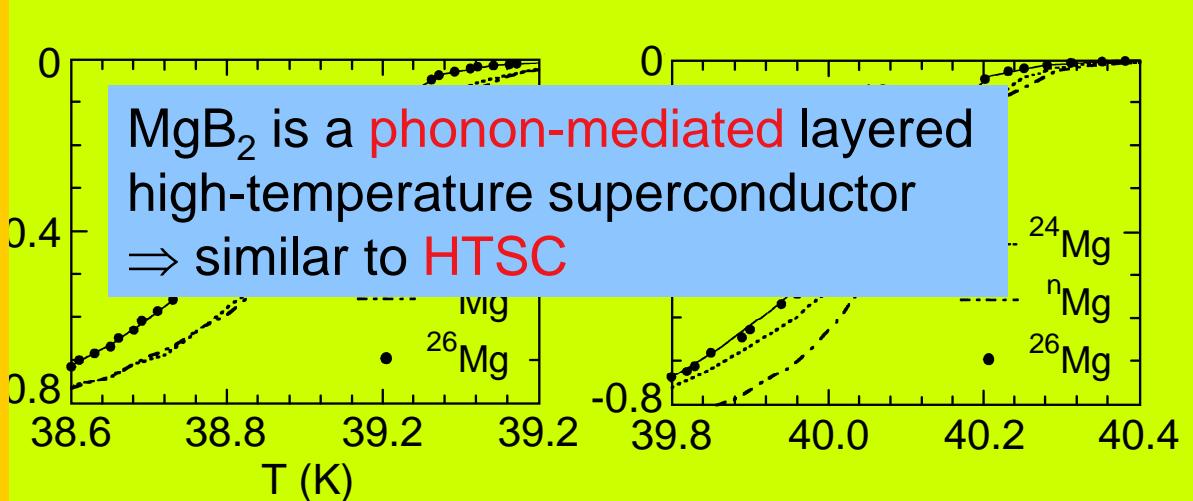
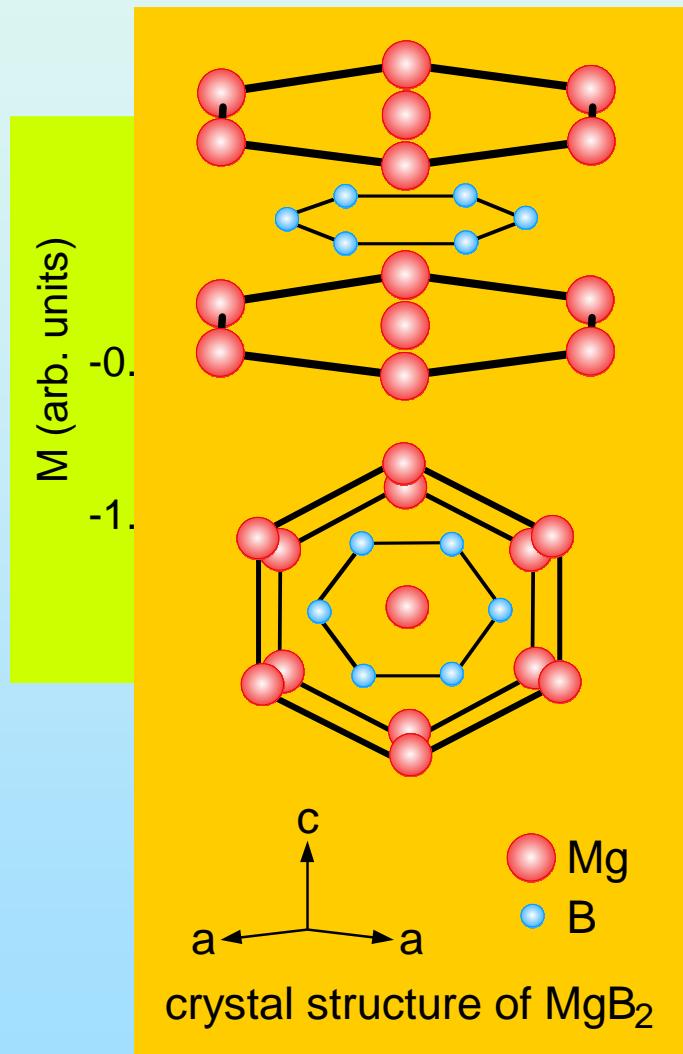


MgB<sub>2</sub> is a **phonon-mediated** layered high-temperature superconductor



$$\alpha_B = 0.26(3)$$

# Mg and B isotope effect in superconducting MgB<sub>2</sub>



$$\alpha_B = 0.30(1)$$
$$\alpha_{\text{Mg}} = 0.02(1)$$

## Question 1

What is the isotope effect in superconductors ?  
How isotope exponent is defined ?

## Question 2

Why by heating the sample in  $^{18}\text{O}_2$  atmosphere  
isotope exchange can be made ?

## Question 3

How oxygen isotope effect exponent depends  
on doping in cuprate high- $T_c$  superconductors ?