

*The Caucasian-German School and
Workshop on Hadron Physics 2004*

**Spin dependence in pd reactions
at intermediate energies**

**Pia Thörngren, Uppsala University
For the PINTEX collaboration**

Outline

□ Objective – Probing the spin dependence of the three-nucleon force (3NF)

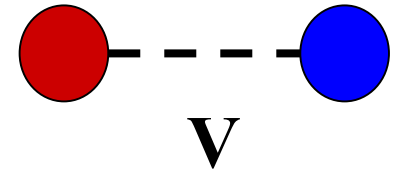
- PINTEX results from pd elastic scattering

□ The PINTEX dp breakup experiment

- Experimental set-up
- Analysis tools – The sampling method
- Recent results and present status

□ Outlook

3NF - What is it ?



□ IUCF Workshop Sep 1998 - Working Session II:

- *Question: What do we mean by 3NF, and where is the best place to look for experimental evidence?*

□ H. Witala (working session notes):

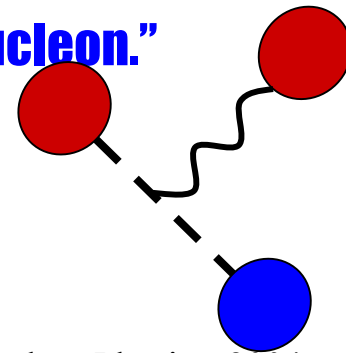
- "In a pragmatic view, with nucleon DOF only

$$H = T + \sum V_{ij} + V_{1,2,3}$$

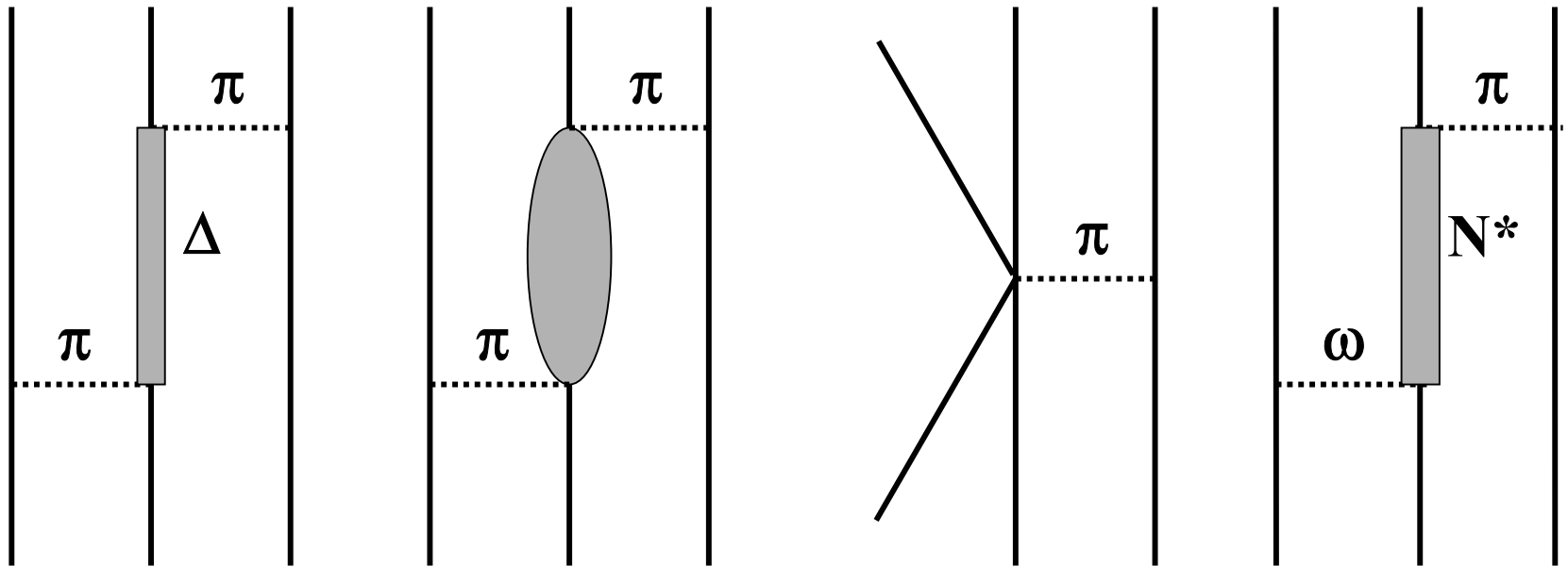
where the second term is all pairwise i.a. summed over the 3N. The rest is 3NF and takes into account any distortion of NN potential energy caused by the presence of the third nucleon."

Size of the 3NF interaction:

$$\Delta V \approx V^2/Mc^2 \rightarrow 0.5 - 1 \text{ MeV}$$



Three-Nucleon Interactions



2 π -Xchange force

incl. short range i.a.

Models for 3NF

□ Tucson –Melbourne (TM)

S. Coon and W. Glöckle,
PRC 23, 1790 (1981)

- **2π exchange process, full off-shell πN scattering amplitude**

□ TM modified (TM')

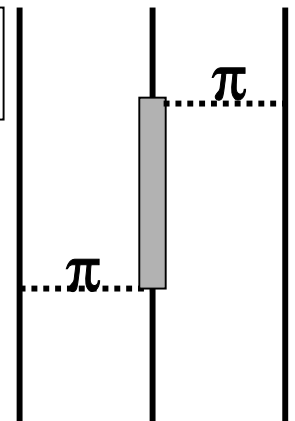
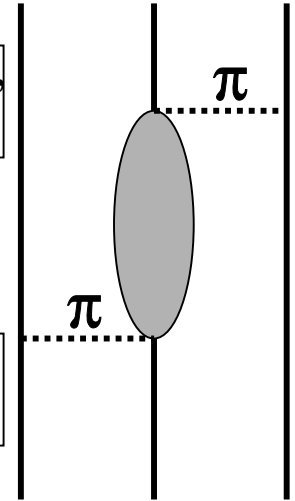
D. Hüber et al., Few-
Body Syst. 30, 95 (2001)

- **Drop one term and modify another to comply with chiral symmetry**

□ Urbana IX force

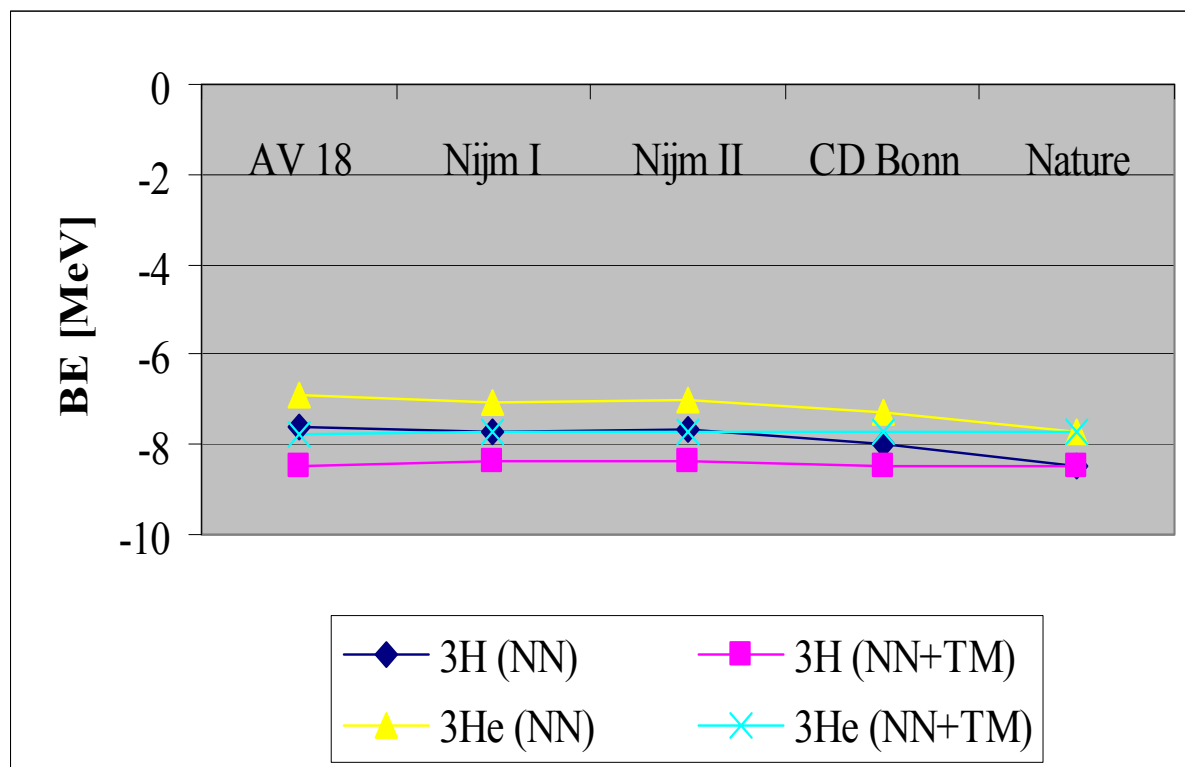
J. Carlson et al., Nucl.
Phys. A401, 59 (1983)

- **FM approach + phenomenological spin and isospin independent short-range part**



Binding Energy of ${}^3\text{He}$ and ${}^3\text{H}$

NN-potential	BE [MeV]			
	${}^3\text{H}(\text{NN})$	${}^3\text{H}(\text{+TM})$	${}^3\text{He}(\text{NN})$	${}^3\text{He}(\text{+TM})$
AV 18	-7.62	-8.48	-6.92	-7.76
Nijm I	-7.74	-8.39	-7.08	-7.72
Nijm II	-7.66	-8.39	-7.01	-7.72
CD Bonn	-8.01	-8.48	-7.27	-7.72
Nature	-8.48	-8.48	-7.72	-7.72



...so all is well....?

3NF in the continuum?

a) 3

b) 65

c) 135 MeV

d) 190 MeV



NN forces



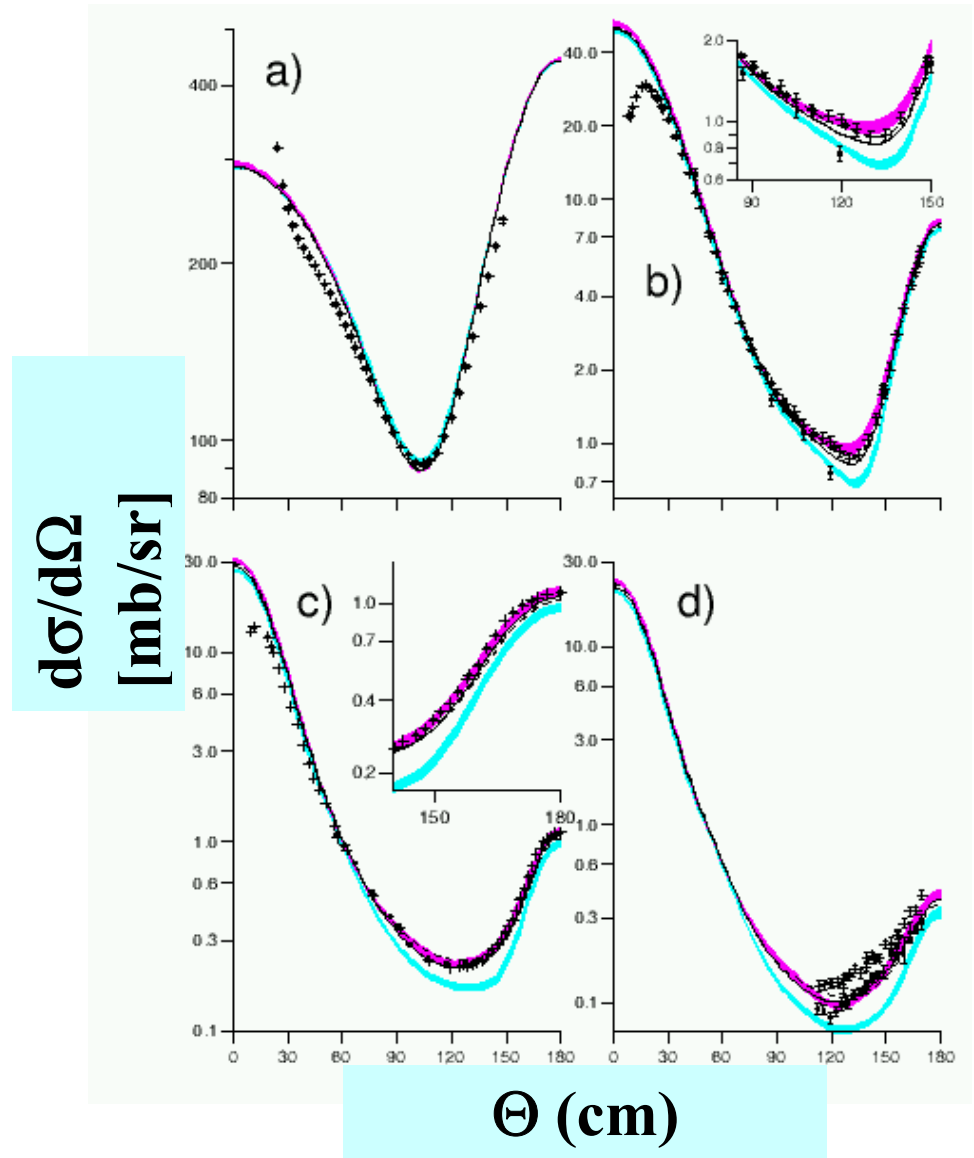
NN+TM3NF



AV18+UIX



CDBonn+TM'

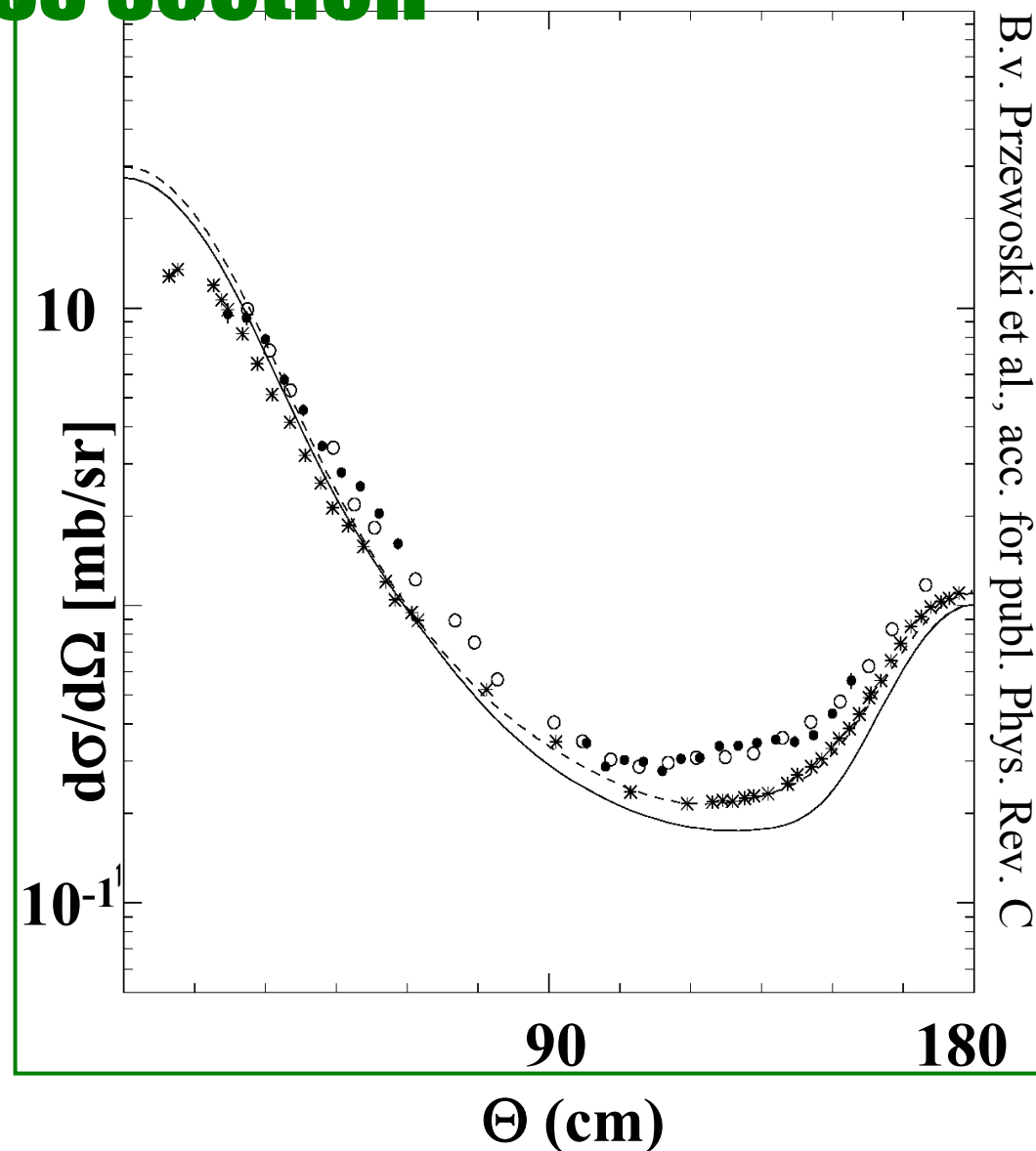


Differential cross section

p+d elastic scattering

at 135 MeV

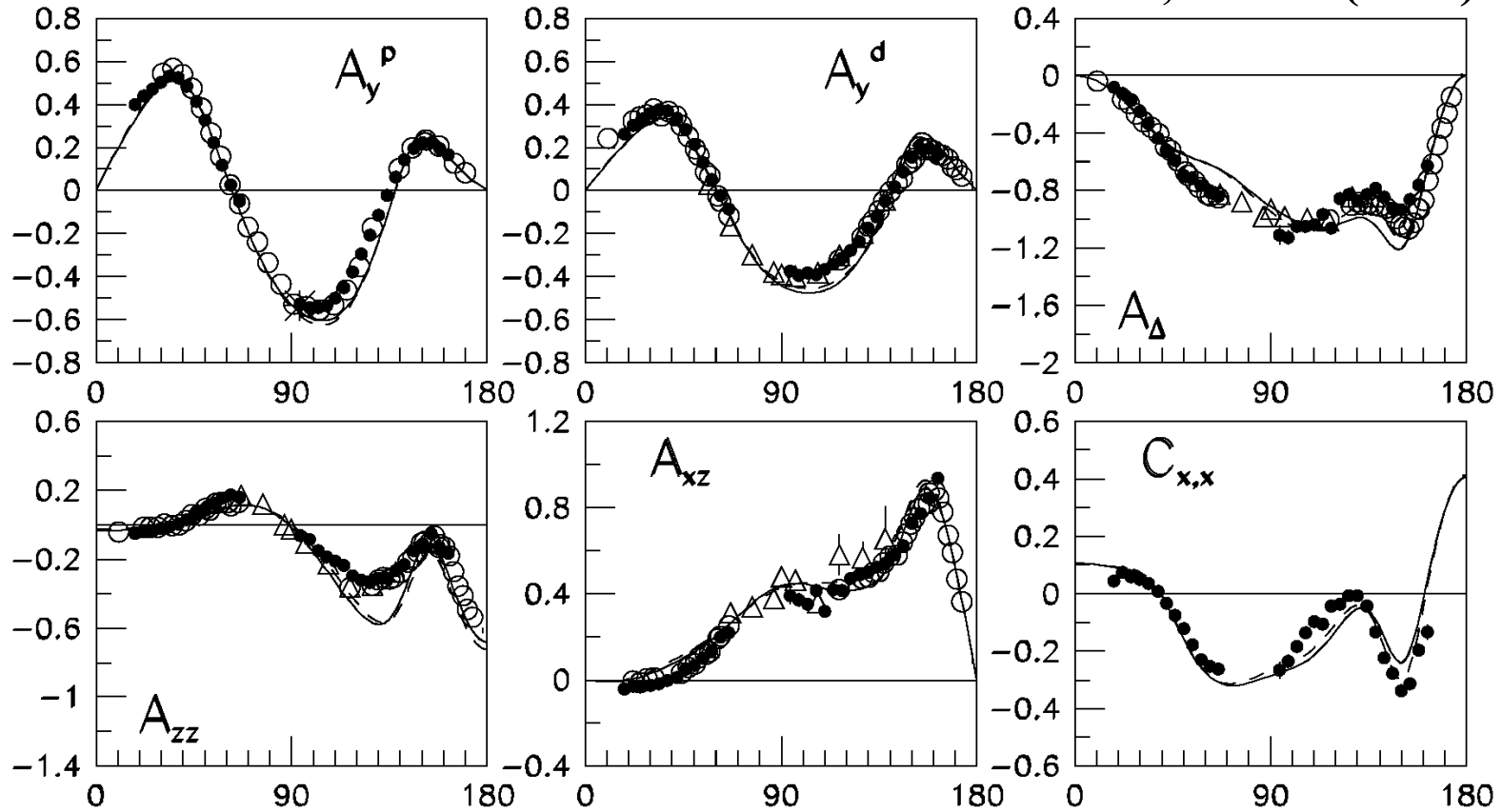
- K. Ermisch et al., arXiv:nucl-ex/0308012, PhD thesis, KVI Groningen, ISBN:90-9016528-2
- PINTEX-IUCF present data (normalized to Ermisch et al.)
- * K. Sekiguchi et al., Phys. Rev. C65 (2002) 034003
- CD Bonn, R. Machleidt, PRC63, 024001 (2001)
- CDBonn + TM 3NF



Spin observables for pd elastic scattering

135 MeV

- This experiment
- △ Previous meas.
- CDBonn NN
- AV18 NN, Wiringa et al., PRC51(1995)

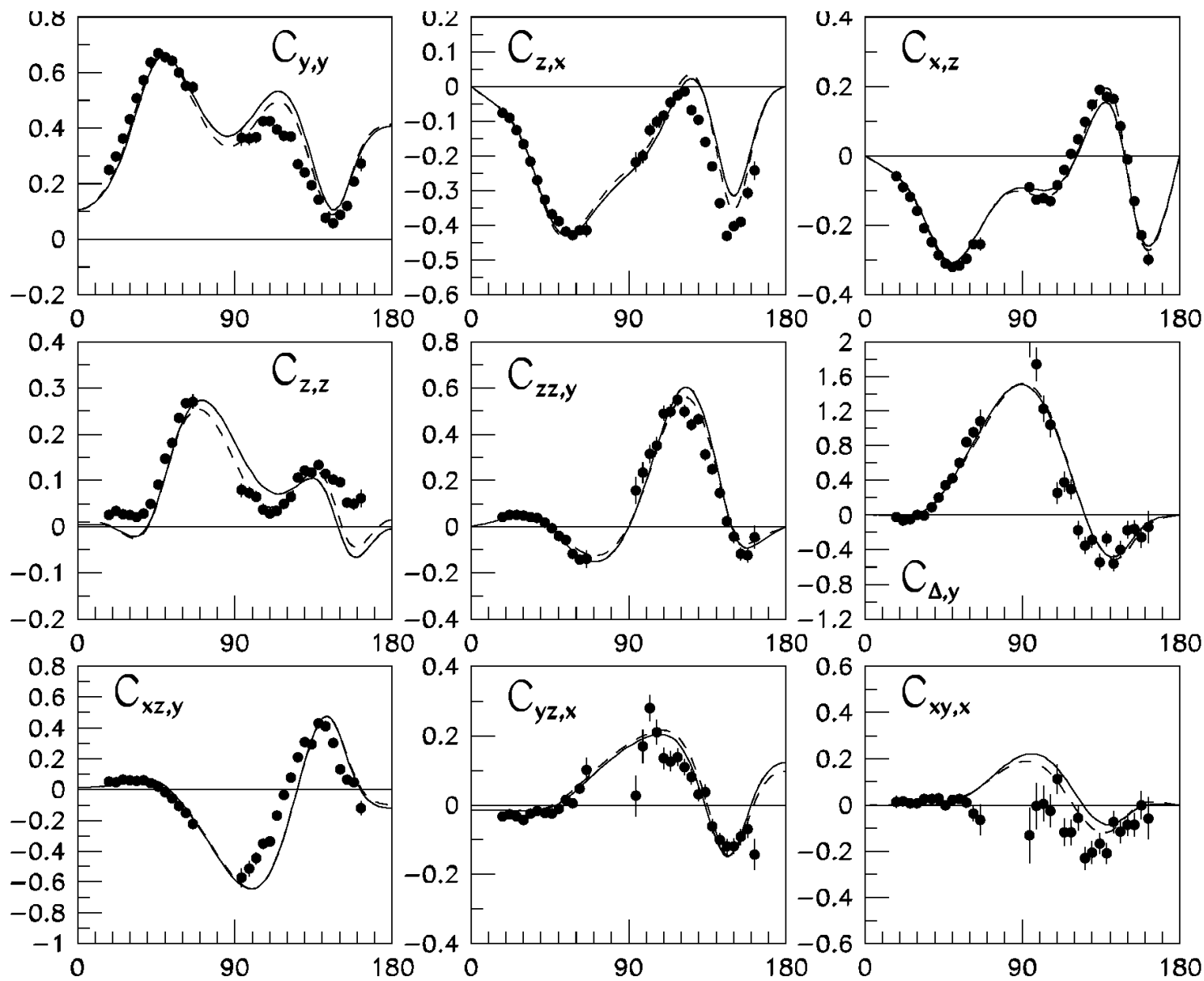


B.v. Przewoski et al., PRC, acc. July 04

Ermisch et al., PRL 86, 5862 (2001)
 Adelberger & Brown, PRD5, 2139 (1972)
 Wells et al., NIM A325, 205 (1993)

Θ_{cm} [deg]

Stephenson PRC60, 061001 (1991) Bieber
 PRL 84, 606 (2000) Sakamoto PLB367,
 60 (1996) Sakai PRL 84, 5288 (2000)
 Sekiguchi PRC65, 034003 (2002)



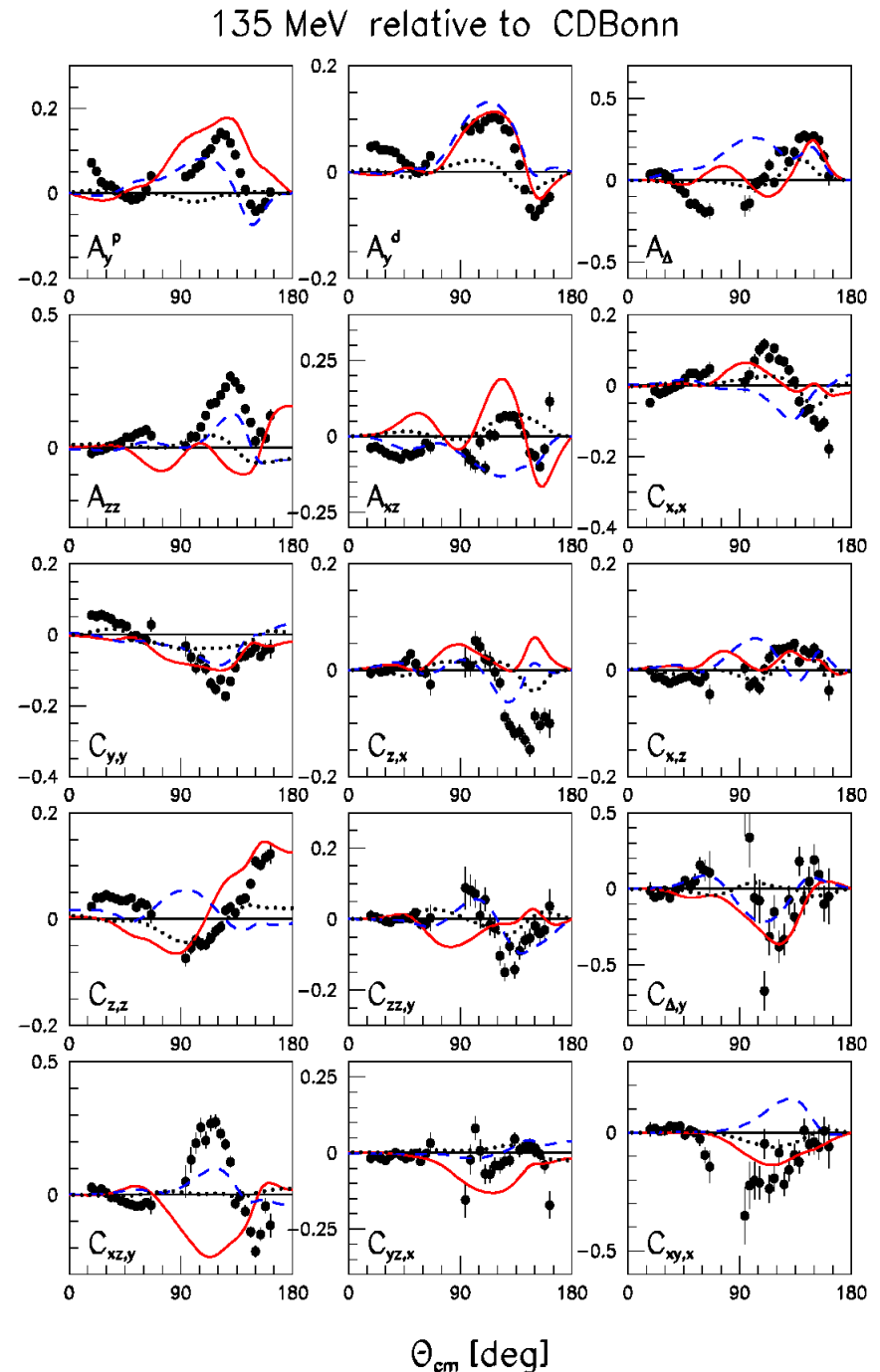
θ_{cm} [deg]

Witala et al., PRC 63, 024007 (2001)

Data – CDBonn

Spin observables for p+d elastic scattering at Tp=135 MeV

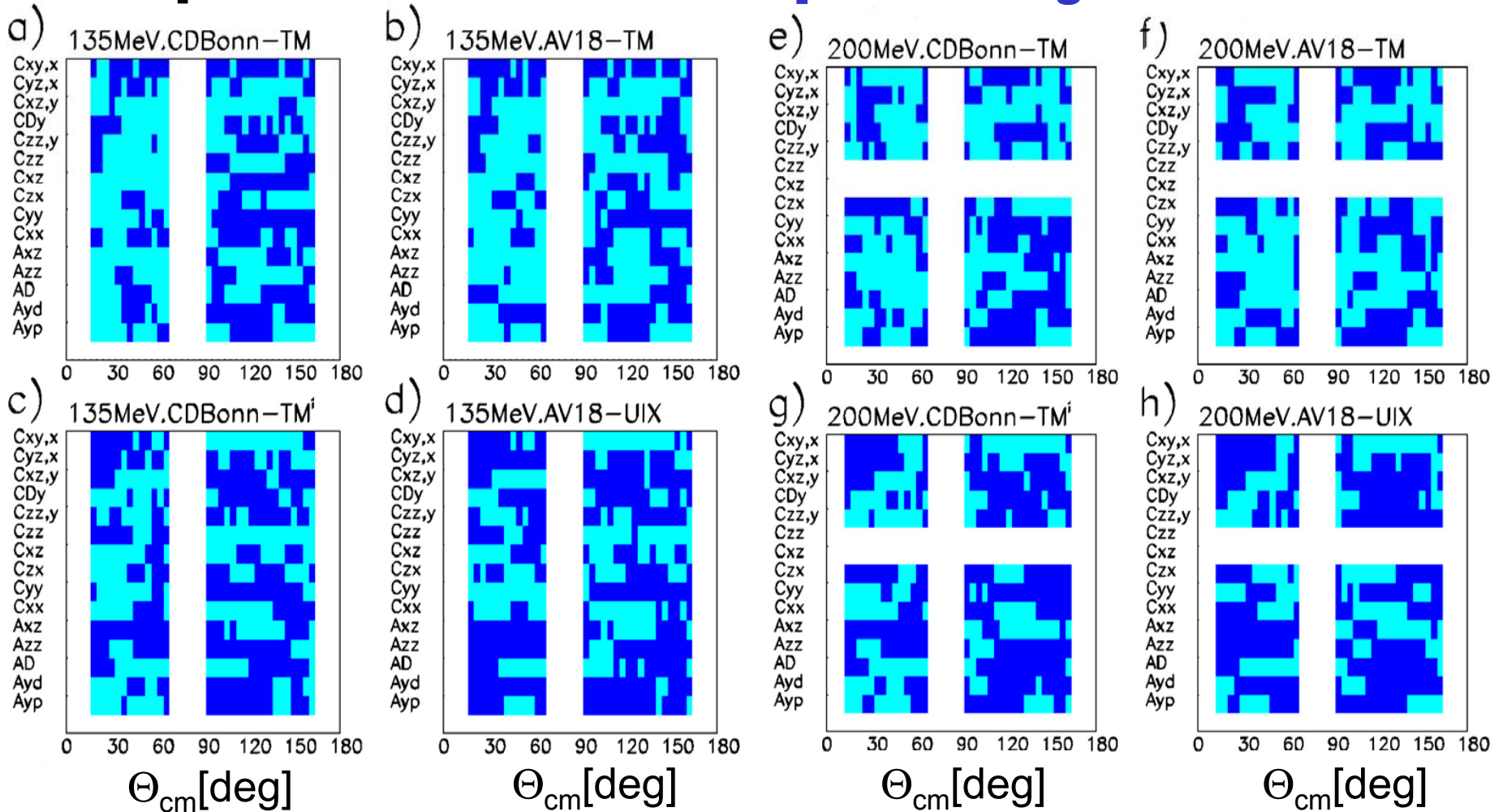
- **Data-CDBonn NN**
 - Including TM 3NF**
 - - - Including TM' 3NF**
 - ... AV18-CDBonn NN**
- Statistical errors*



Systematics of different 3NFs

Each pixel corresponds to one of the 868 data points

A pixel is colored blue if 3NF improves the agreement



Analyzing Powers & Spin Correlation in pd elastic at 135 and 200 MeV

- All analyzing powers, and 10 of 12 possible spin correlation coefficients in **p+d elastic scattering** were measured at 135 and 200 MeV beam energy. A discrepancy was resolved between two recent measurements of the differential cross section
- The Faddeev predictions based on modern NN potentials agree 'fairly' well with the data, the largest disagreements at backward angles
- Input of 3NF into the calculations did not improve the agreement with the data in any consistent way.

Spin dependence of dp breakup

□ The PINTEX dp breakup experiment

➤ Motivation

➤ Experimental set-up

➤ Analysis tools – The grid method

➤ Recent results and present status

□ Axial observables

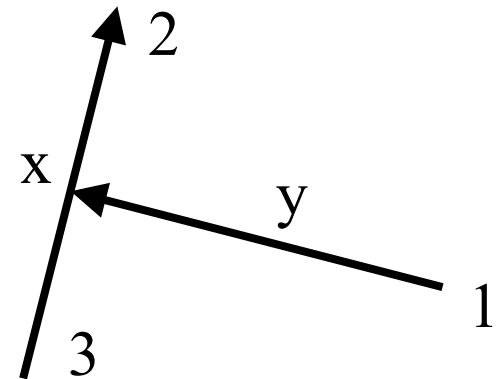
□ Tensor analyzing powers

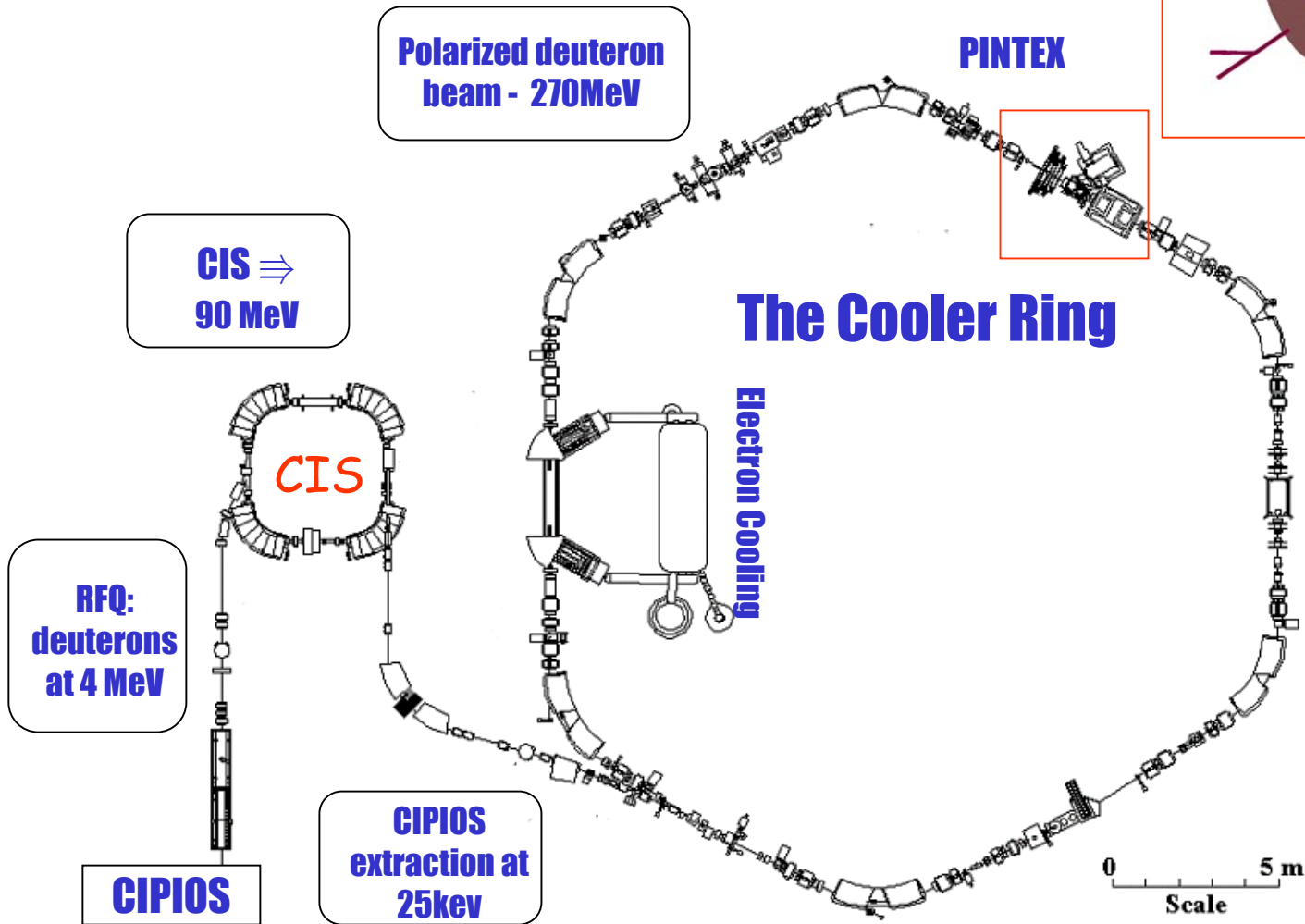
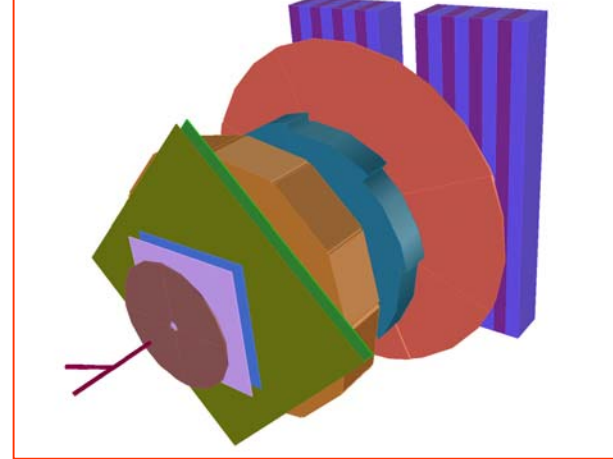
Axial observables in dp breakup

- Axial observables are required to be zero for coplanar events due to parity conservation. BUT - This is not the case in a breakup reaction.
- Axial observables: A_{zp} , $C_{y,x}-C_{x,y}$, $C_{zz,z}$, A_{zd} , $C_{xz,x}-C_{yz,y}$
- There are operators that are unique to axial observables that would vanish if there were no 3NFs. It is suggested that the axial operators might enhance the Axial observables.

$$\begin{aligned} O(2\pi - 3N) &= (\sigma_2 \cdot x)(\sigma_3 \cdot y) - (\sigma_2 \cdot y)(\sigma_3 \cdot x) \\ &= (\sigma_2 \times \sigma_3) \cdot (x \times y) \end{aligned}$$

L.D. Knutson PRL 73 (1994) 3062





Polarized deuteron beam

Beam state	Sextu pole 1	MFT	Sextu pole 2	WFT	SFT	Hyper fine s.	$\sim Q_\zeta$	$\sim Q_{\zeta\zeta}$
1	1,2,3	3→4	1,2		2→6	1,6	+0.8	+0.7
2	1,2,3	1→4	2,3	2→4		3,4	-0.6	+0.7
3	1,2,3	1→4	2,3		2→6	3,6		+0.8
4	1,2,3	1→4	2,3		3→5	2,5		-1.6

One beam state was unpolarized

Target storage cell

□ Front view

25 cm long, \varnothing 12 mm
0.025 mm aluminum
Teflon coated

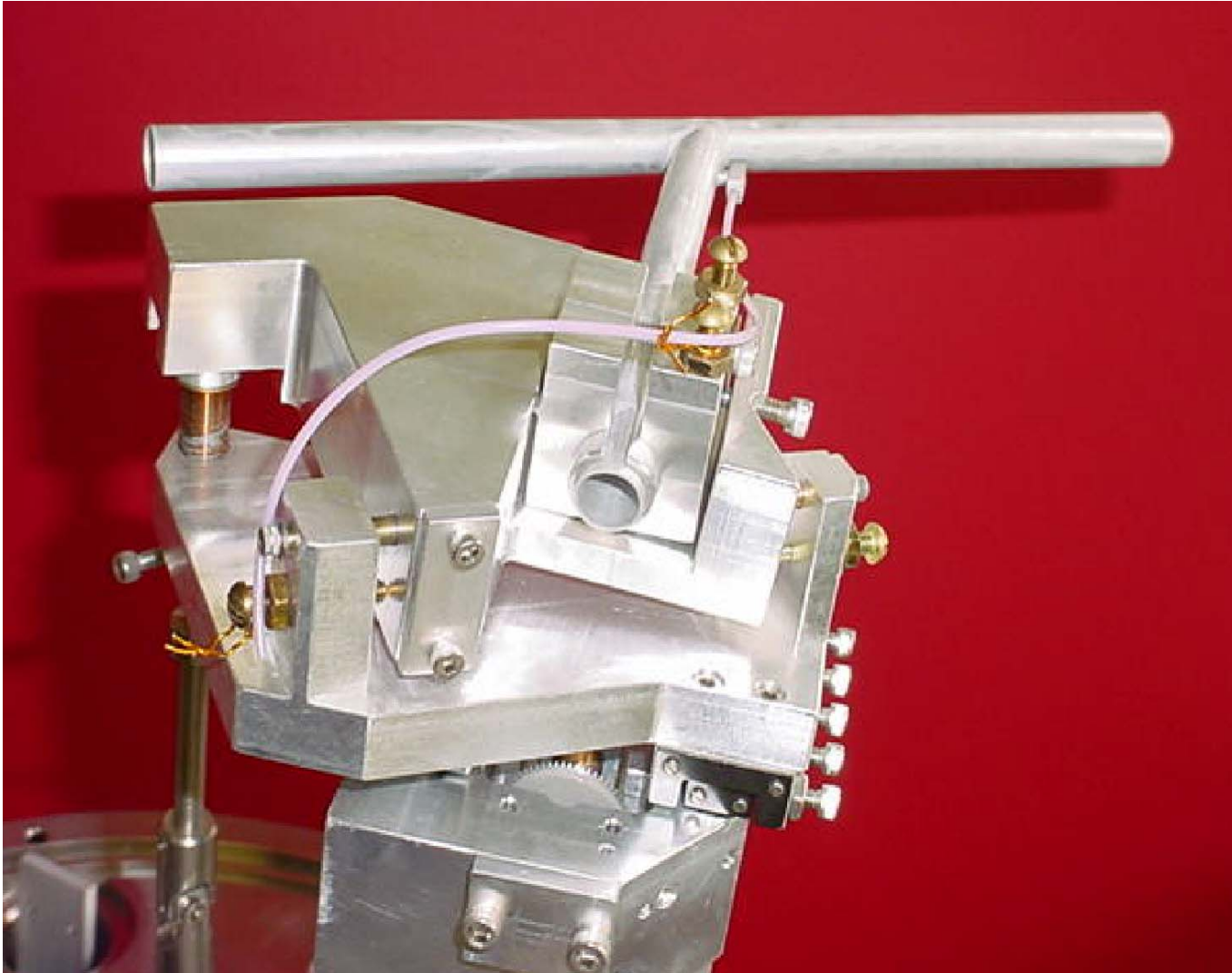
Target thickness
 $\sim 10^{13}$ atoms/cm²

Polarization ~ 0.6

$\pm x, \pm y, \pm z$ directions

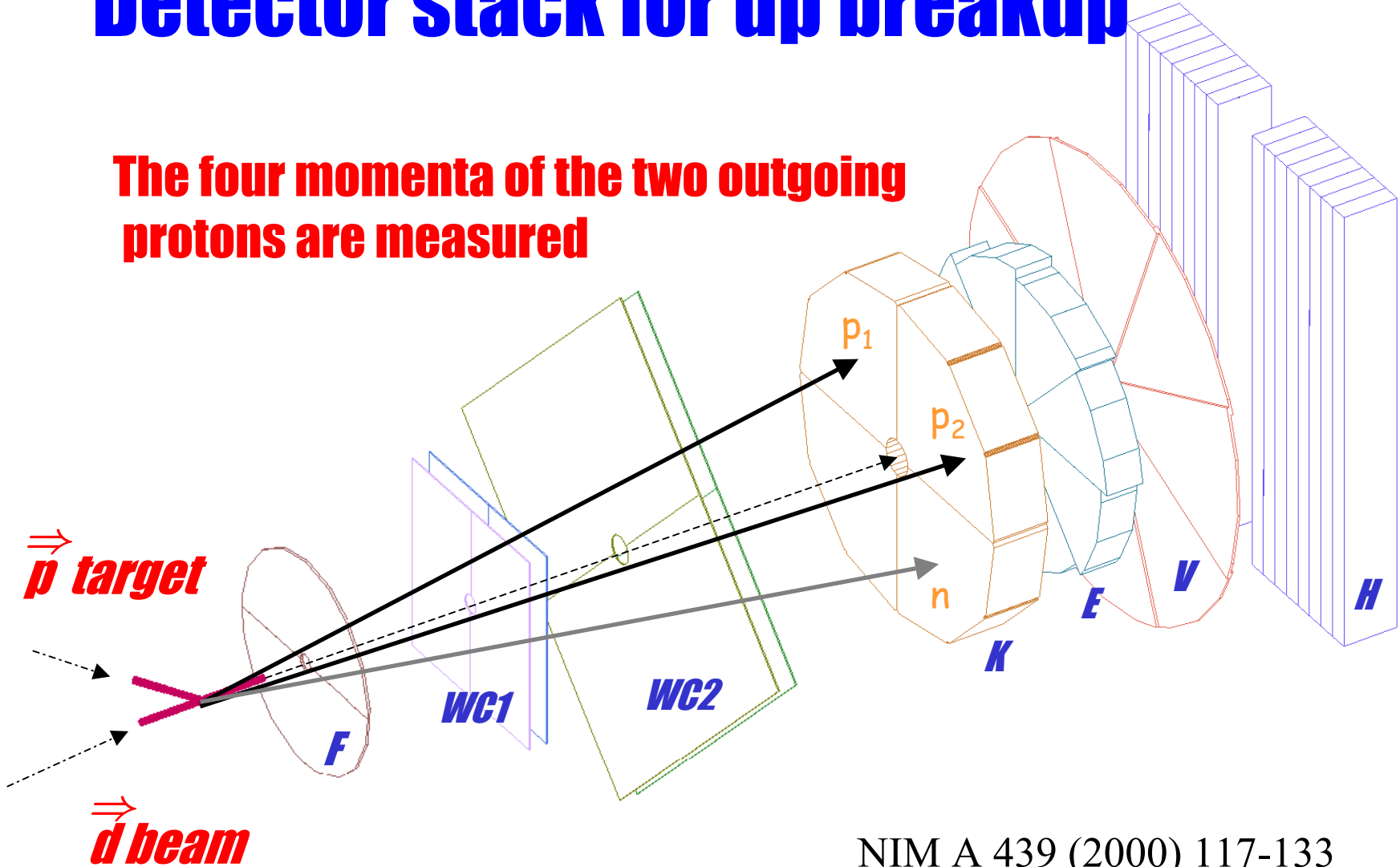


Target storage cell – side view



Detector stack for dp breakup

The four momenta of the two outgoing protons are measured



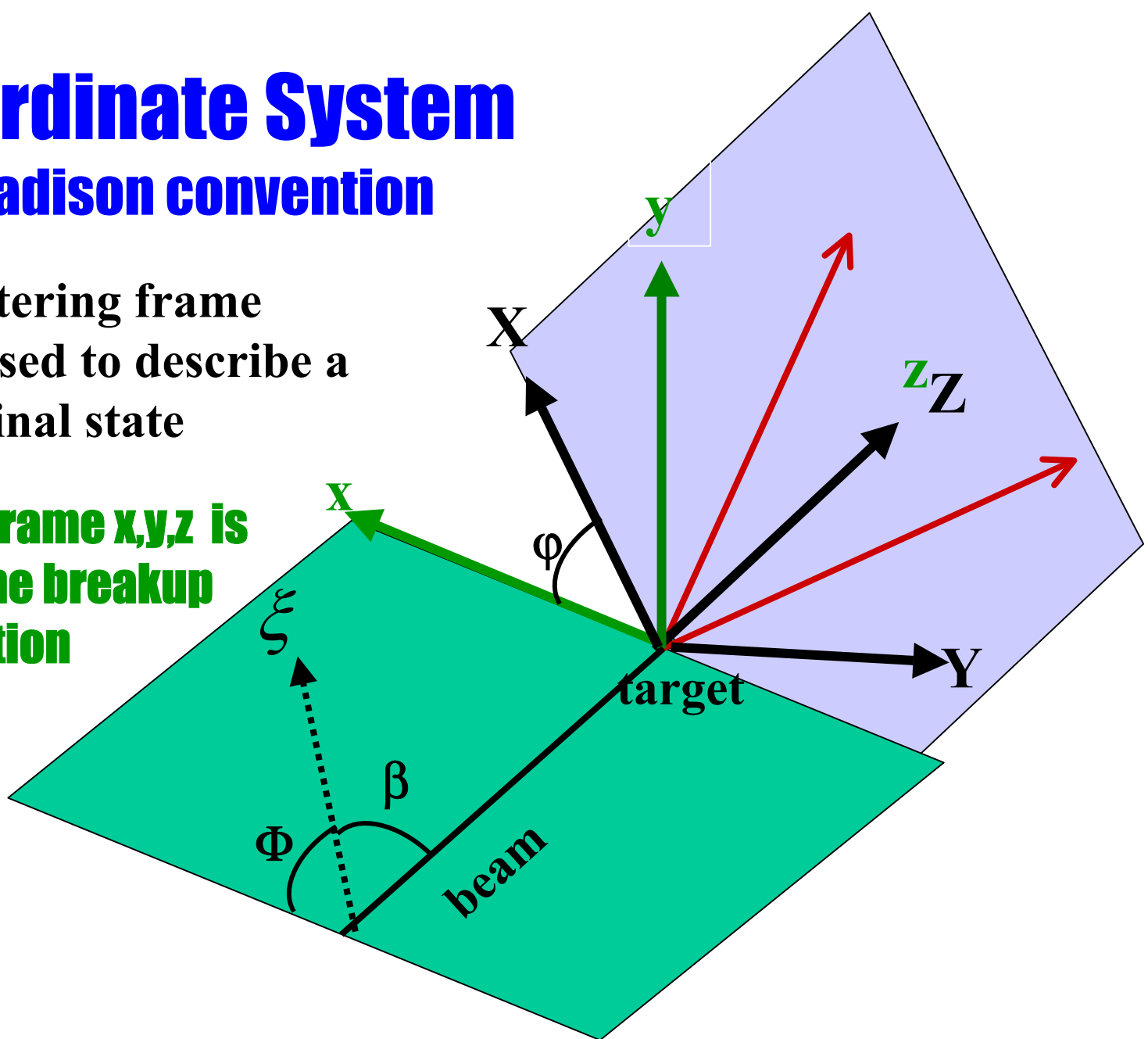
NIM A 439 (2000) 117-133

Coordinate System

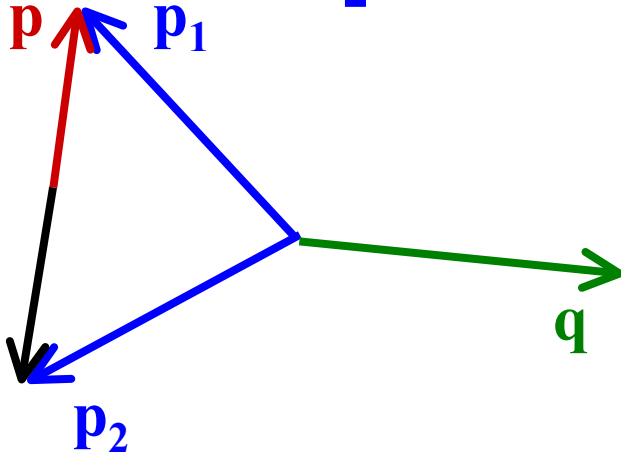
Madison convention

The scattering frame
 X, Y, Z used to describe a
2-body final state

The fixed frame x, y, z is
used for the breakup
configuration



Comparison of theory and experiment for 3N final states



Jacobi momenta

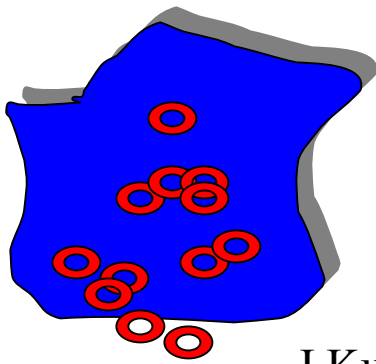
$$\mathbf{p} = \frac{1}{2} (\mathbf{p}_1 - \mathbf{p}_2)$$

$$\mathbf{q} = -(\mathbf{p}_1 + \mathbf{p}_2)$$

$$\Delta\varphi = \varphi(\mathbf{p}) - \varphi(\mathbf{q})$$

□ **Problem: How do we compare data to theory in a consistent way?**

- **True experimental acceptance/efficiency?**
- **Which is the most interesting observable and which independent variable to plot against, which to integrate over?**



The Sampling Method

J.Kuros-Zolnierczuk, P.Thörnngren, H.O. Meyer et al., FBS 34, 259 (2004)

- **For any 3b final state known with complete kinematics – ‘sample’ the theoretical value for each event in $\gamma =$ (detected) region of phase space**

$$O_{th}(\gamma) = \frac{\int \sigma_0(x) \varepsilon(x) O_{th}(x) dx}{\int \sigma_0(x) \varepsilon(x) dx} = \frac{\sum_x N(x_i) O_{th}(x_i)}{\sum_x N(x_i)}$$

The Sampling Method Using a Grid

Few Body Syst. 34, 259 (2004)

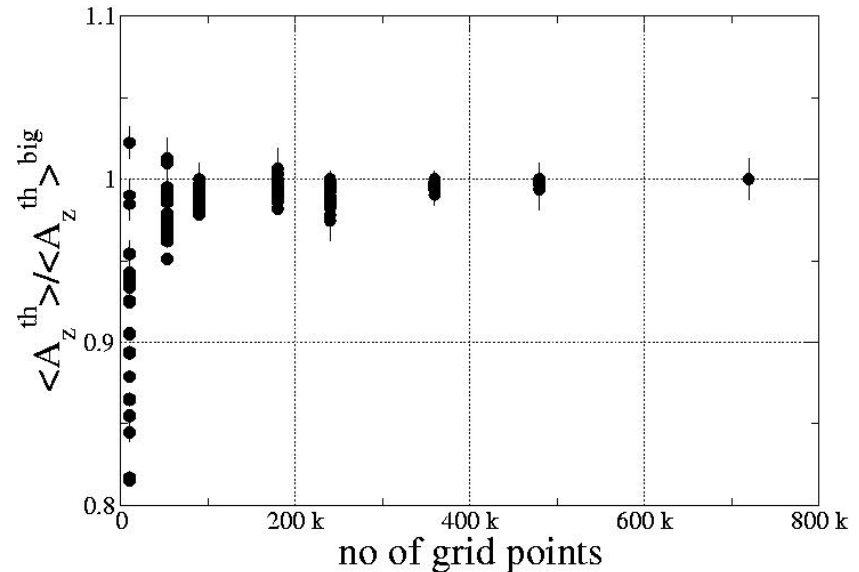
□ Requirement:

- Calculate a theoretical value for each event

Drawback: X time consuming

□ Solution:

- Construct a grid covering phase space
- Use multidimensional interpolation



Four-dimensional

$2^4=16$ corners / grid cell

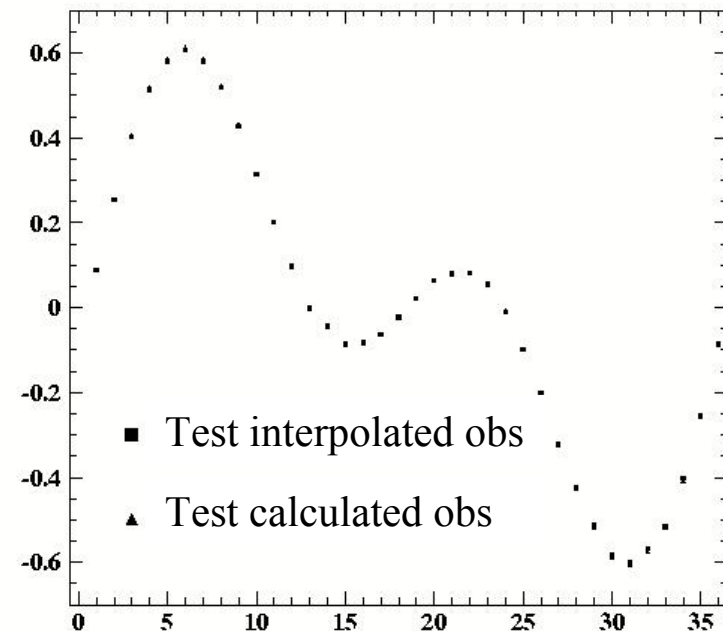
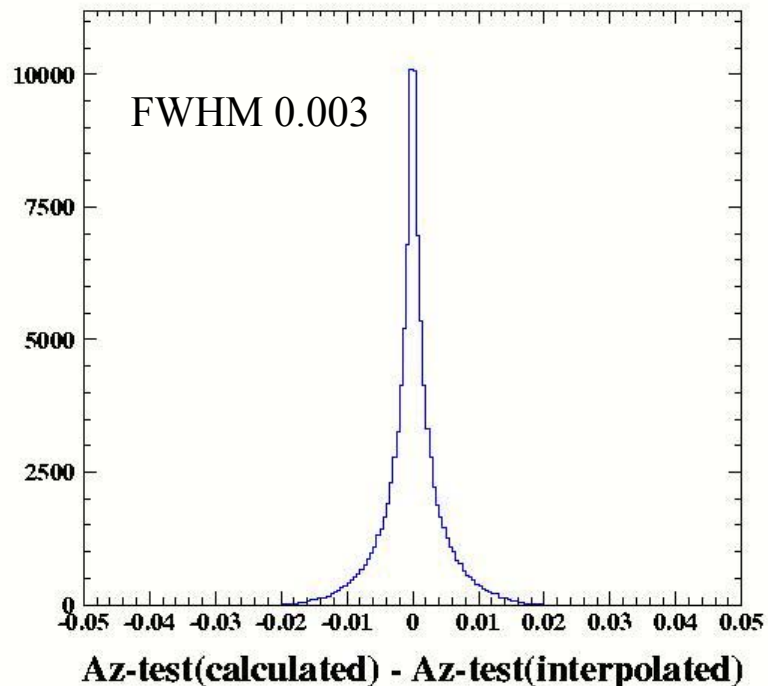
Five-dimensional:

$2^5=32$ corners / grid cell

Grid behaviour

Few Body Syst. 34, 259 (2004)

□ **Test: Construct a 'fake' observable with similar angular dependencies**



The Sampling Method Using a Grid

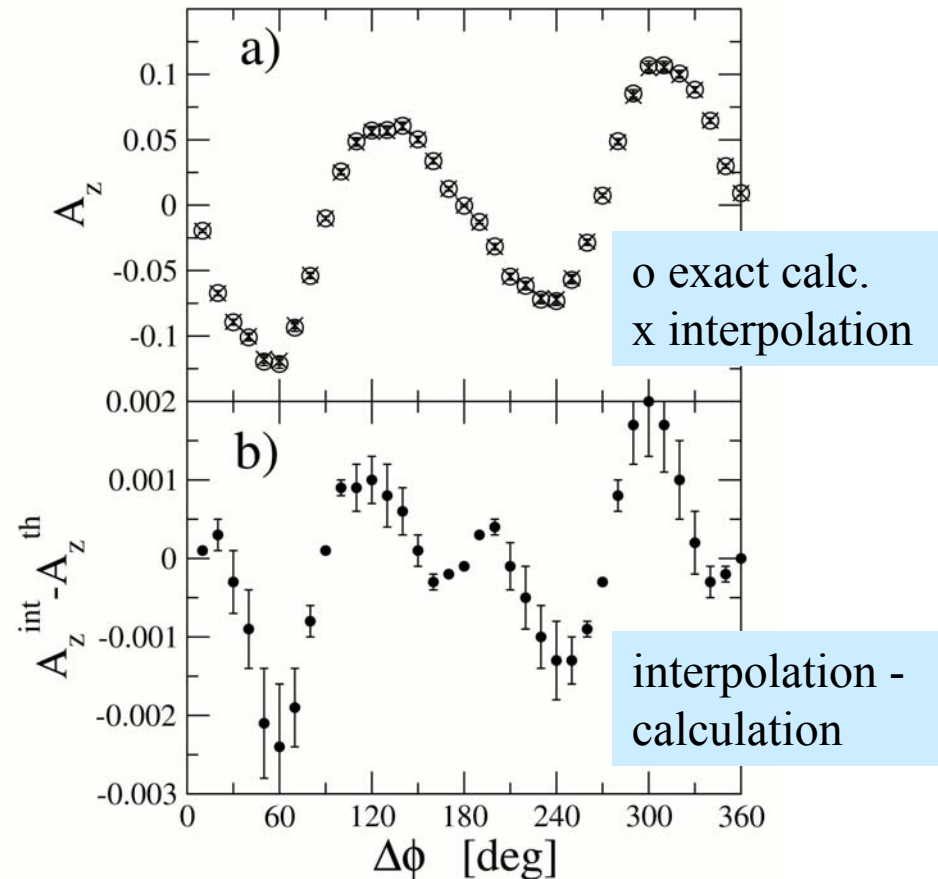
Few Body Syst. 34, 259 (2004)

□ Test of accuracy:

- Compare single-shot exact calculation and interpolation

□ Conclusion

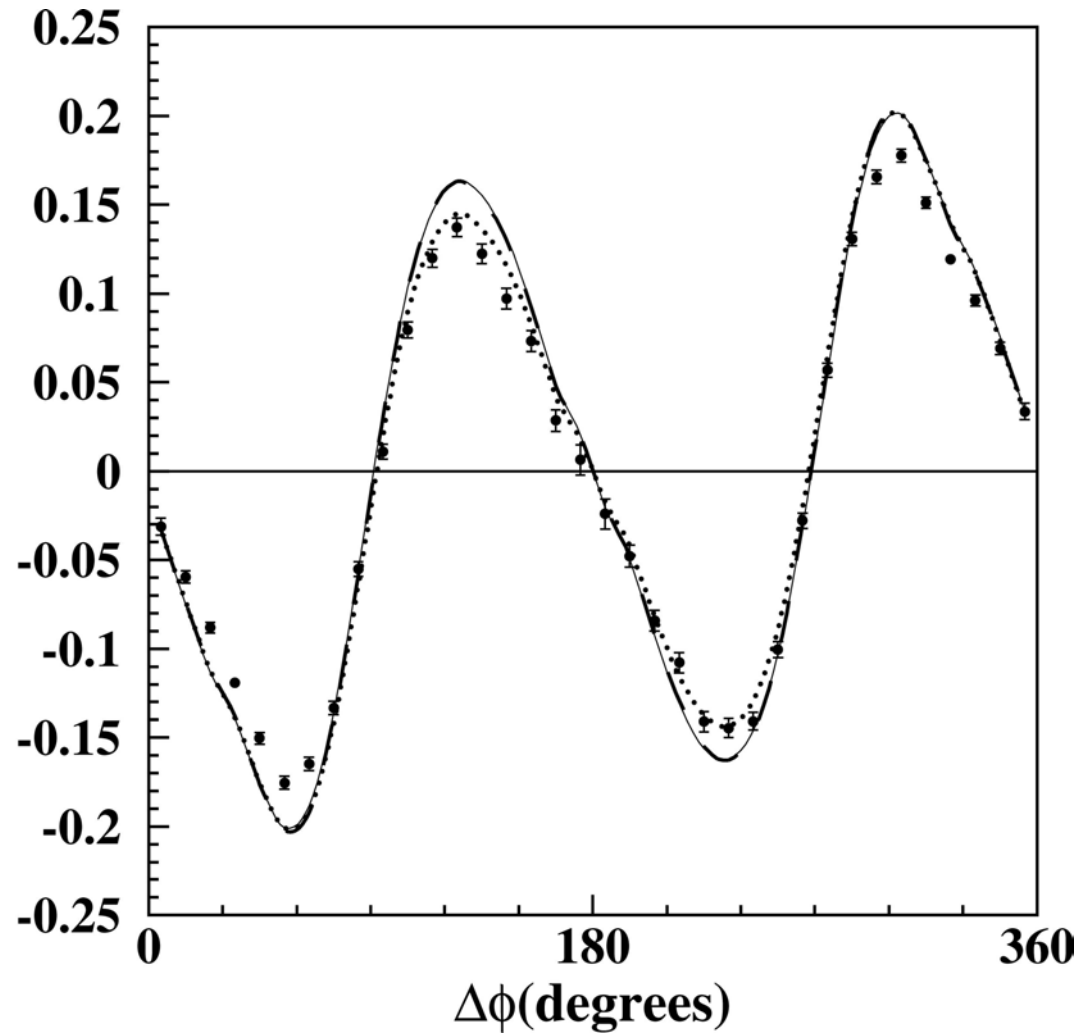
- The sampling method eliminates the necessity of monte carlo simulations and reflects the true detector acceptance and efficiency. Using a theoretical grid and interpolation reduces the computing time.



A_z VS $\Delta\phi$

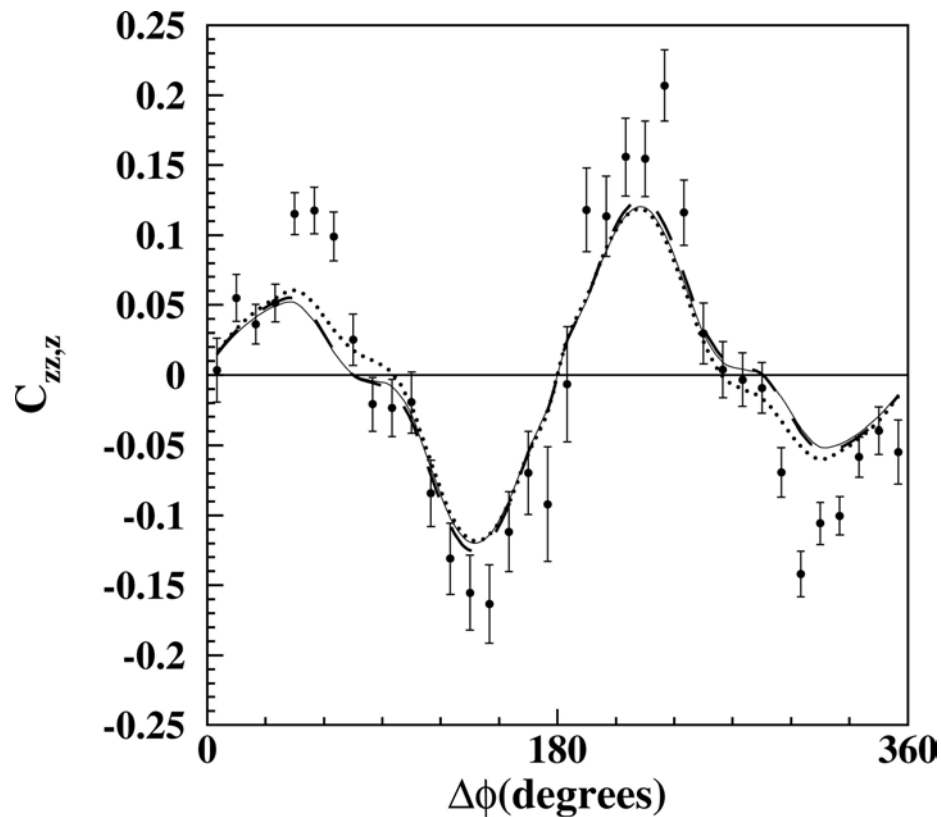
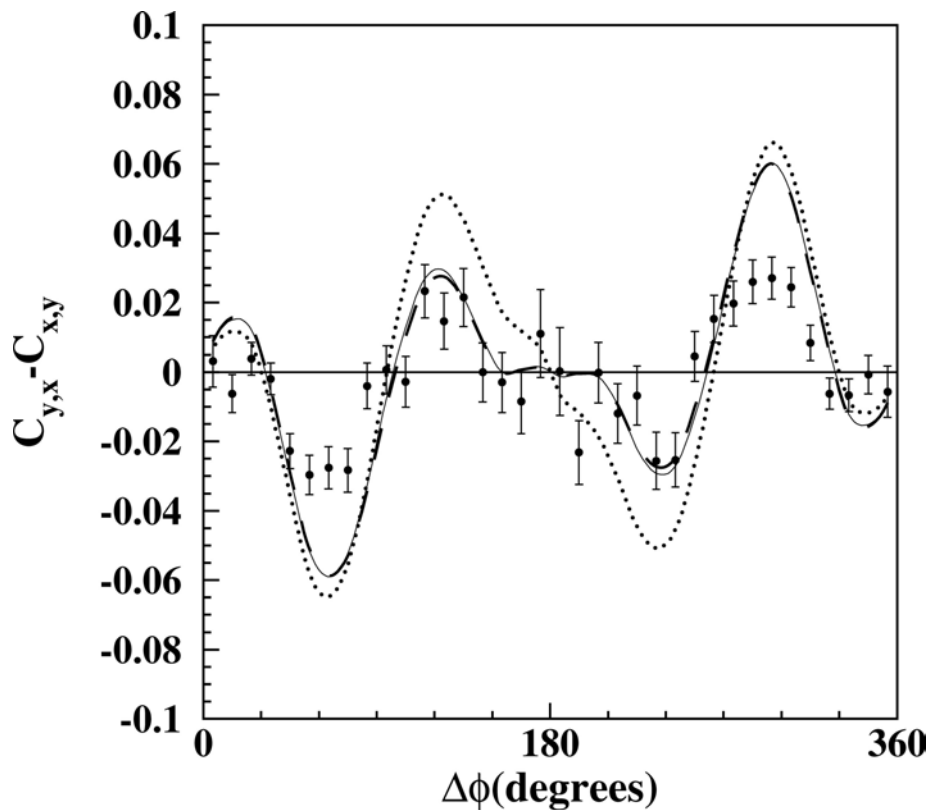
*Data using all five
beam states and
 $\pm z$ target*

solid line: CD-Bonn
dashed: AV18
dotted: CD-Bonn+TM'



solid line: CD-Bonn
dashed: AV18
dotted: CD-Bonn+TM'

$C_{y,x} - C_{x,y}$ and $C_{zz,z}$ as a function of $\Delta\phi$

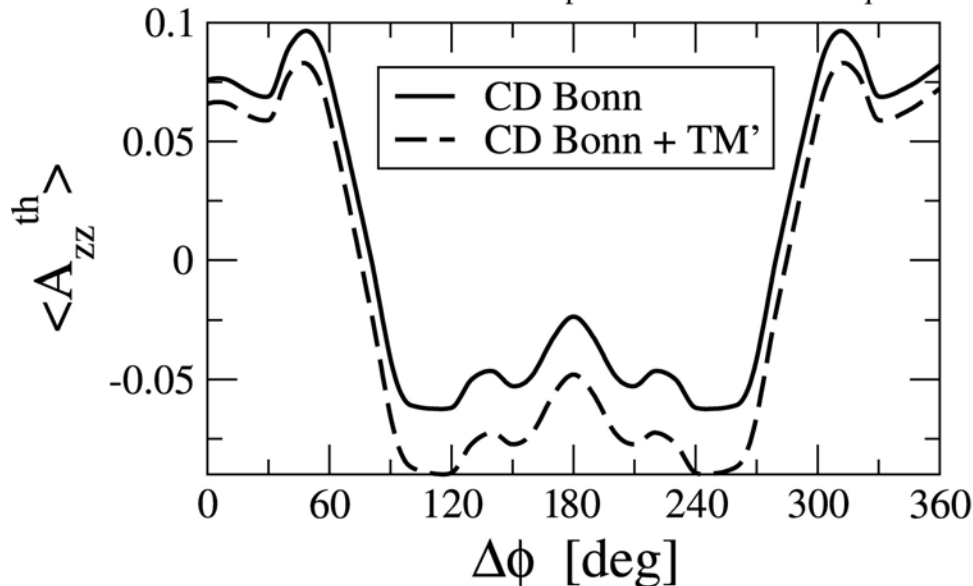


Tensor analyzing powers

- Using the tensor polarized beam states and summing over all target polarization: σ (tensor) =

$$\sigma_0 \left(1 - \frac{1}{4} Q Q \cos(2\phi) (A_{xx} - A_{yy}) - \frac{1}{4} Q Q A_{zz} \right)$$

$0.05 \leq p \leq 1.45$, $5^\circ \leq \theta_p \leq 90^\circ$, $100^\circ \leq \theta_q \leq 180^\circ$

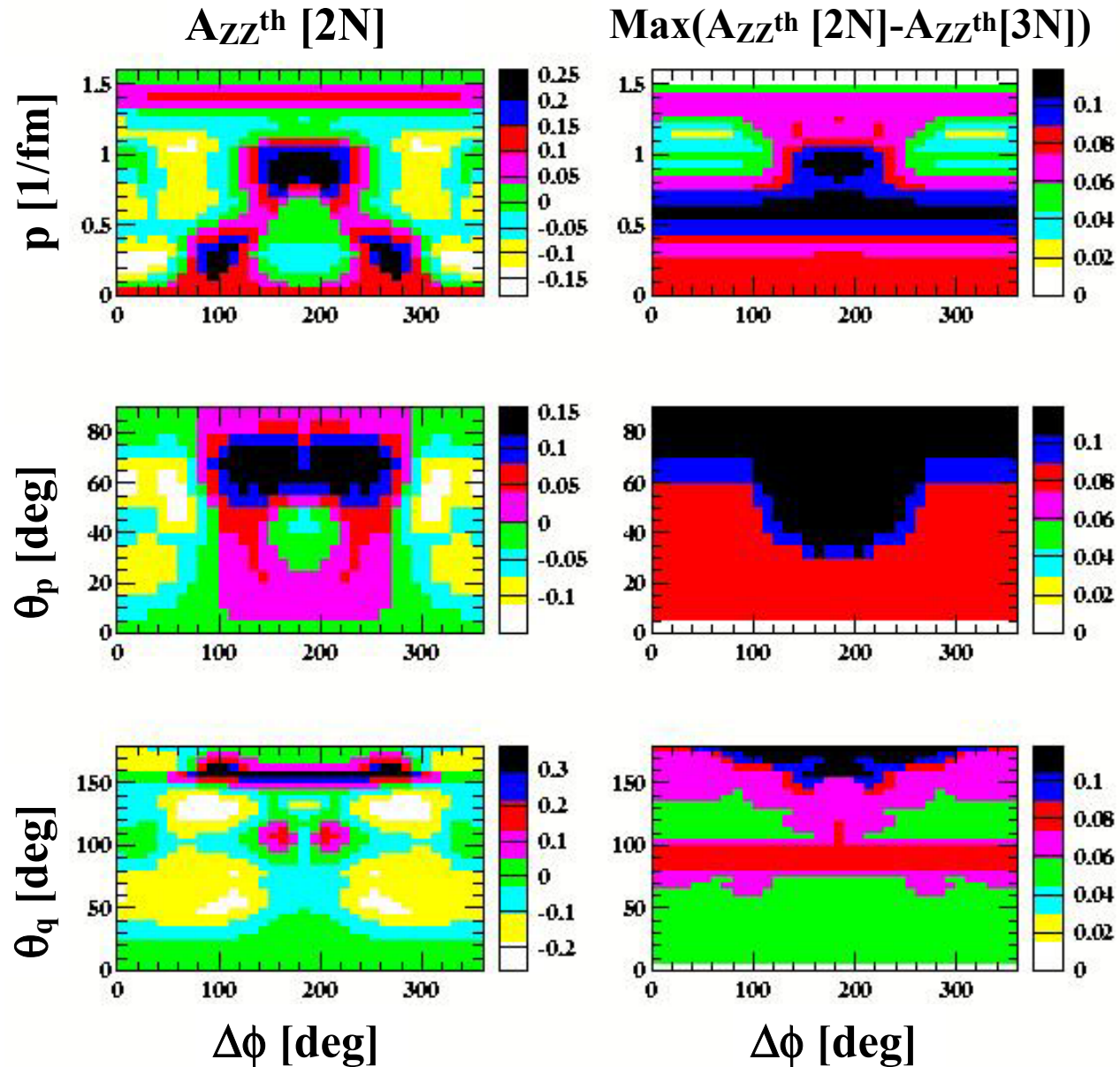


Using the grid -

To investigate theoretical predictions -

Joanna Kuros-Zolnierczuk

Krakow-Bochum group



Observables measured in dp breakup

□ **d+p breakup at $T_d=270\text{MeV}$**

□ **Measured in this experiment:**

(deuteron spin alignment +y)

➤ **Analyzing powers:** A_y^p , A_z^p , A_y^d , A_{zz} , $(A_{xx} - A_{yy})$

➤ **Vector-vector correlation coefficients:**

$(C_{x,x} - C_{y,y})$ $(C_{x,x} + C_{y,y})$ $C_{x,z}$ $(C_{y,x} - C_{x,y})$

➤ **Tensor-vector correlation coefficients**

$(C_{xx,y} - C_{yy,y})$ $C_{xy,x}$ $C_{xy,z}$ $C_{zz,y}$ $C_{zz,z}$

Summary and outlook

□ **A new method has been developed for the analysis of dp breakup reactions. It allows for quick searches for places in phase space that are sensitive for 3NF**

□ **A_Z , $(C_{y,x} - C_{x,y})$, $C_{ZZ,Z}$ measured for the first time – they do not show enhanced sensitivity to TM 3NF**

Analysis of other observables is in progress, 3NF effects are predicted to be large in tensor analyzing powers

□ **The breakup data will together with the 15 measured spin observables in p+d elastic scattering, constrain any future 3NF model**

➤ **Compare with predictions for 3N from chiral effective field theory**

The tools are in place!

Acknowledgements

□ The PINTEX collaboration:

**H.O. Meyer, J. Kuros-Zolnierscuk,
B.v.Przewoski, P.Thörngren Engblom, T.J.
Whitaker, J.T.Balewski, J.Doskow,
W.W.Daehnick, W.Haeberli, R.Ibald,
B.Lorentz, P.Pancella, F. Rathmann, Swapan
K. Saha, A.Wellinghausen**

Cross section for spin 1 on spin 1/2

□ The most general case:

$$\begin{aligned}
 \sigma = \sigma_0 & \left(1 + p_y A_{yp} + p_z A_{zp} + \frac{3}{2} q_y A_{yd} + \frac{3}{2} q_z A_{zd} + \frac{1}{6} (q_{xx} - q_{yy}) (A_{xx} - A_{yy}) + \frac{1}{2} q_{zz} A_{zz} + \frac{2}{3} q_{xz} A_{xz} \right. \\
 & + \frac{3}{4} (q_x p_x + q_y p_y) (C_{x_x} + C_{y_y}) + \frac{3}{4} (q_x p_x - q_y p_y) (C_{x_x} - C_{y_y}) + \frac{3}{4} (q_y p_x - q_x p_y) (C_{y_x} - C_{x_y}) \\
 & + \frac{3}{2} q_x p_z C_{x_z} + \frac{3}{2} q_z p_x C_{z_x} + \frac{3}{2} q_z p_z C_{z_z} + \frac{1}{6} (q_{xx} - q_{yy}) p_y (C_{xx_y} - C_{yy_y}) + \frac{1}{2} q_{zz} p_z C_{zz_z} + \frac{1}{2} q_{zz} p_y C_{zz_y} \\
 & + \frac{2}{3} q_{xy} p_x C_{xy_x} + \frac{2}{3} q_{xz} p_y C_{xz_y} + \frac{2}{3} q_{yz} p_x C_{yz_x} + \frac{2}{3} q_{xy} p_z C_{xy_z} + \frac{2}{3} q_{yz} p_z C_{yz_z} \\
 & \left. + \frac{1}{3} (q_{xz} p_x + q_{yz} p_y) (C_{xz_x} + C_{yz_y}) \right)
 \end{aligned}$$