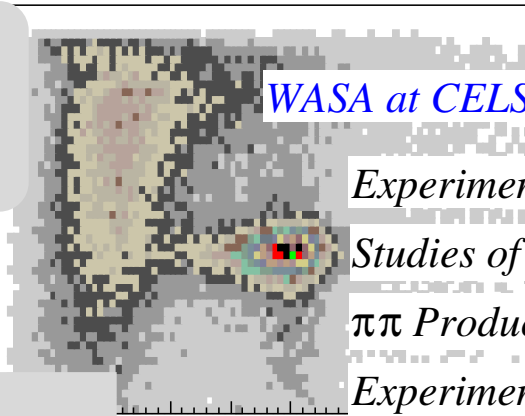


# WASA at *CELSIUS* and $\eta'$ Decays with WASA@COSY

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Institut für Kernphysik  
Forschungszentrum Jülich



WASA at *CELSIUS*

Experimental Technique

Studies of  $\eta$  Decays

$\pi\pi$  Production

Experimental Programme

## $\eta'$ Decays with WASA at COSY

Charge Symmetry  
and Light Quark Masses

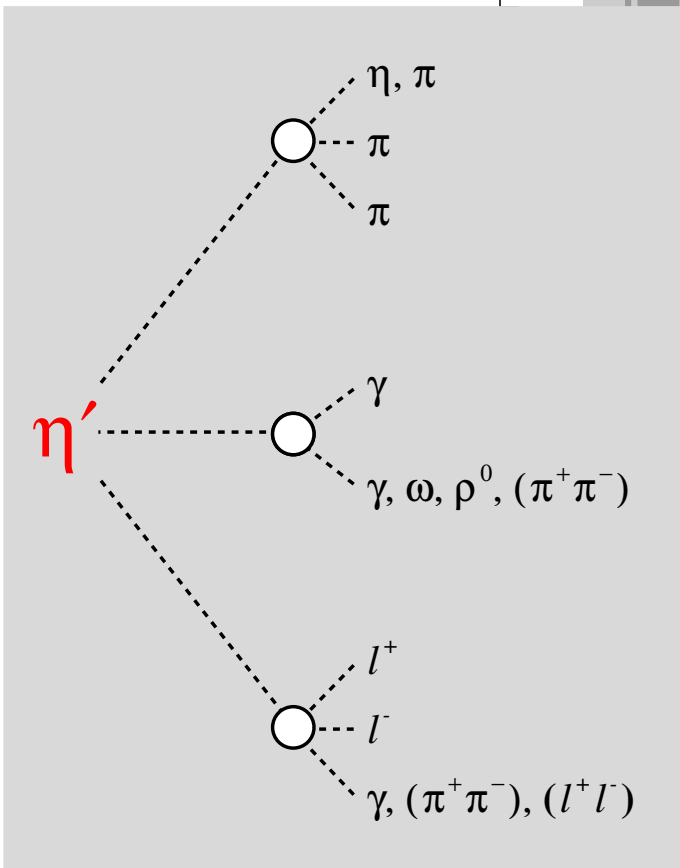
Scalar Couplings

Pseudoscalar  
Singlet-Octet Mixing

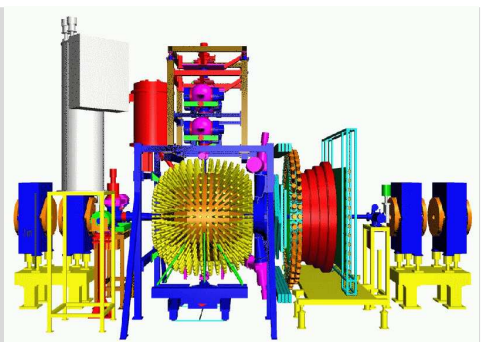
QCD Anomalies

Glue Content

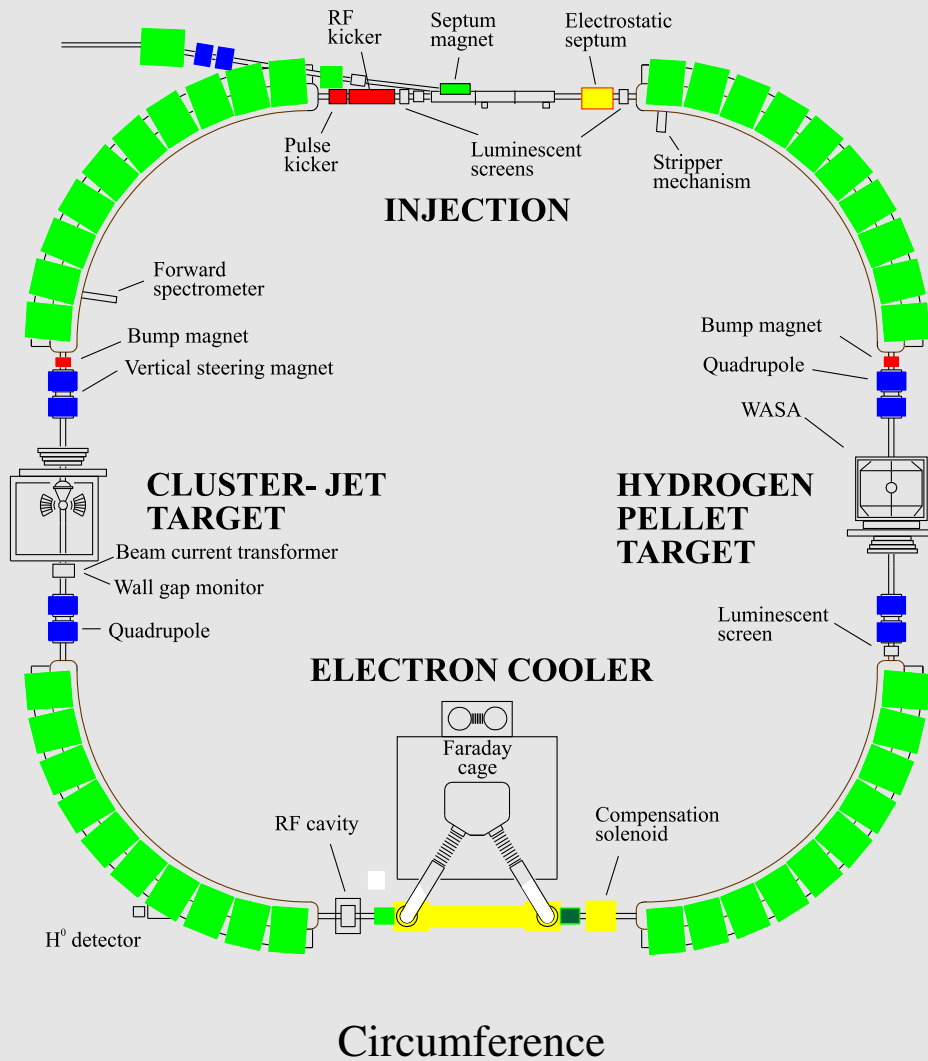
Transition Form Factor



Caucasian-German  
School and Workshop on  
Hadron Physics  
Tbilisi, Aug 30 - Sep 4, 2004



# The CELSIUS Cooler Ring



81.8m

Maximum proton energy

1450MeV

Number of stored protons

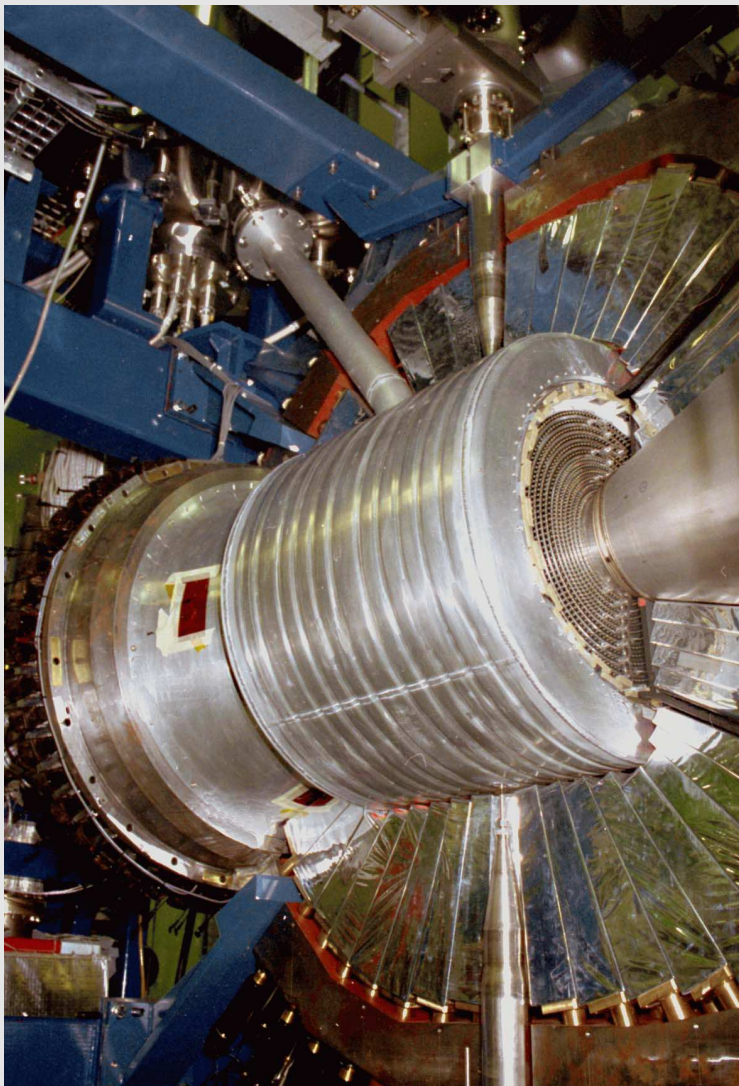
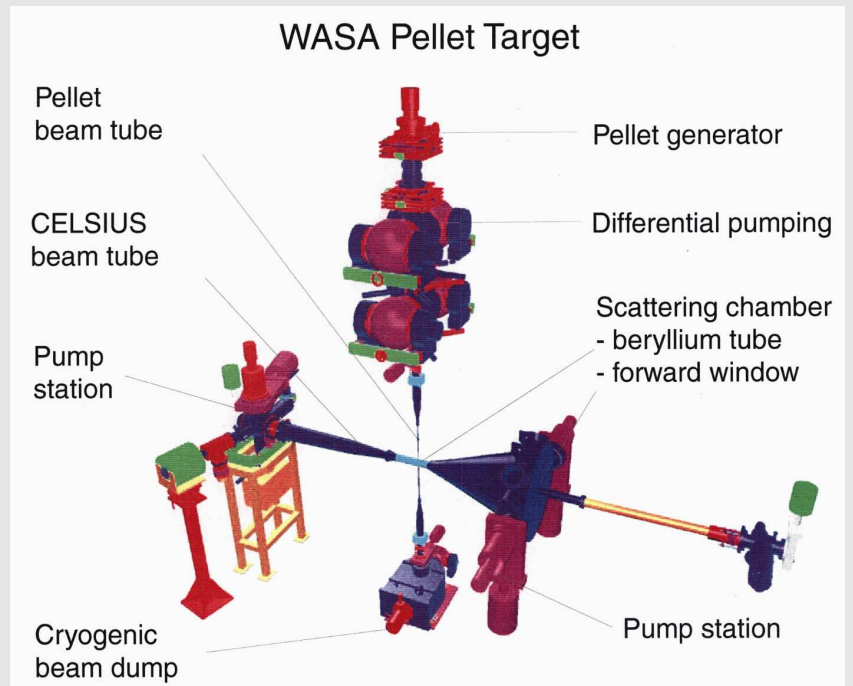
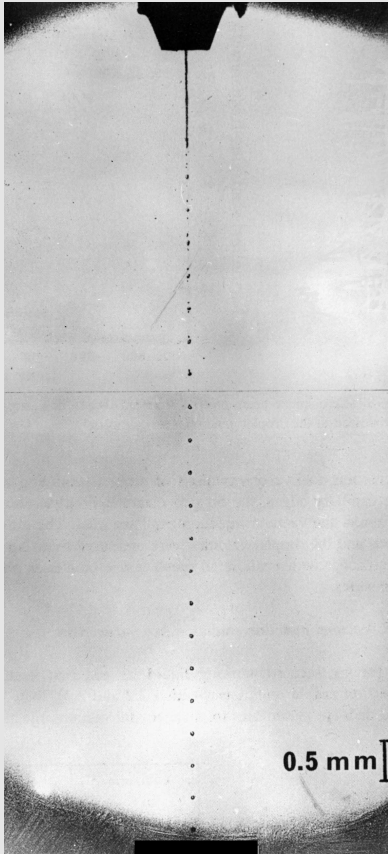
$5 \cdot 10^{10}$

Relative momentum spread  $\Delta p/p$

$1 \cdot 10^{-3}$

Beam dimensions at target (h/v)

5/2.5mm



Pellet diameter

25 - 35  $\mu\text{m}$

---

Pellet frequency

5 - 12 kHz

---

Pellet-pellet distance

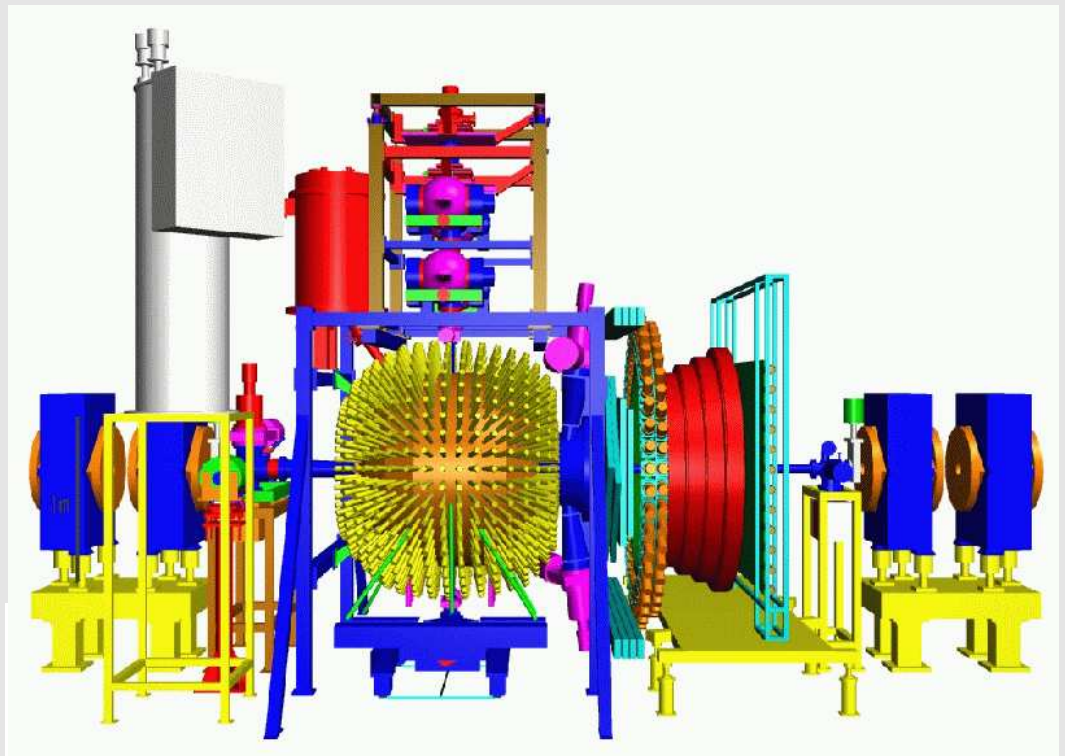
9 - 20 mm

---

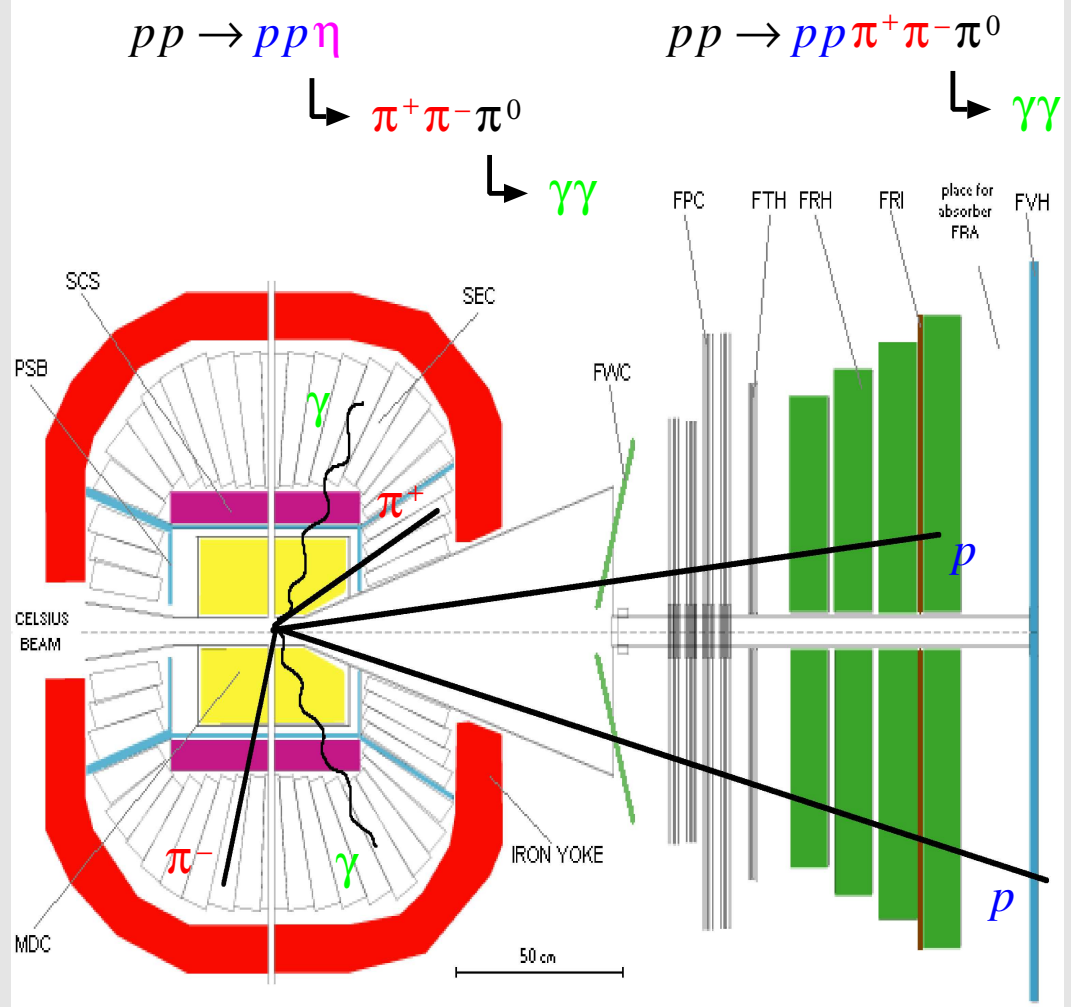
Effective target thickness

$> 10^{15}$  atoms/cm<sup>2</sup>

# WASA detector



# Event identification



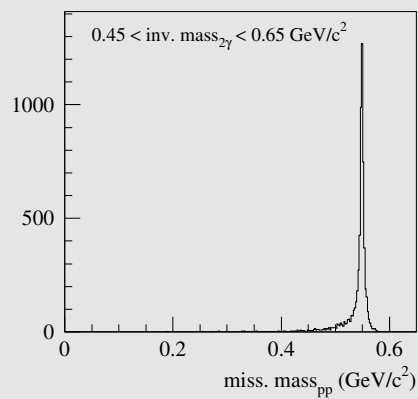
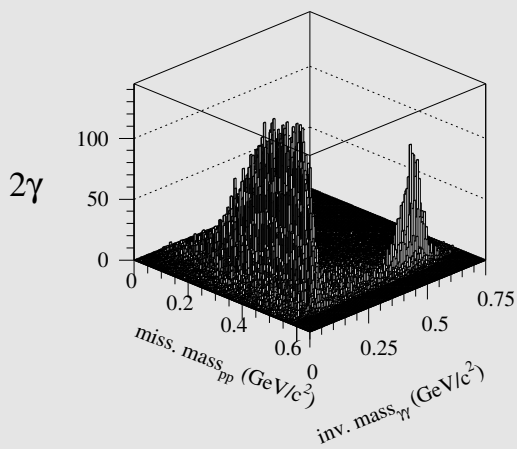
$$pp \rightarrow pp + \gamma_s$$

$$T_p = 1360 \text{ MeV}$$

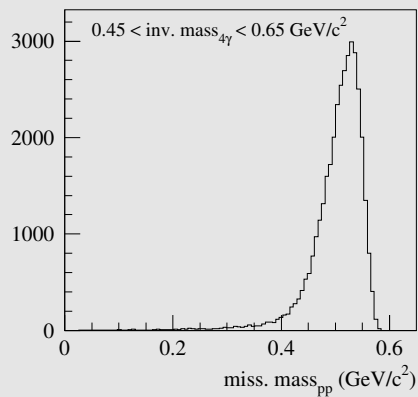
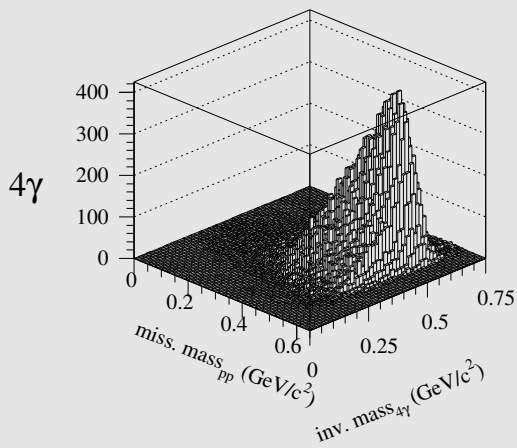
$\gamma_s$  invariant mass  
vs  
 $pp$  missing mass

$pp$  missing mass

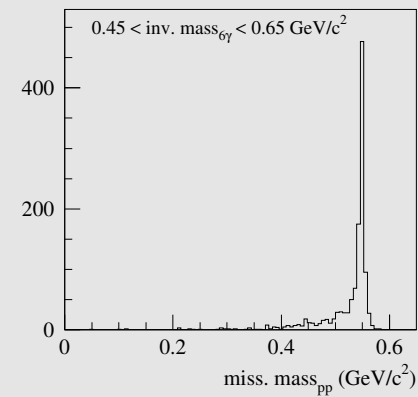
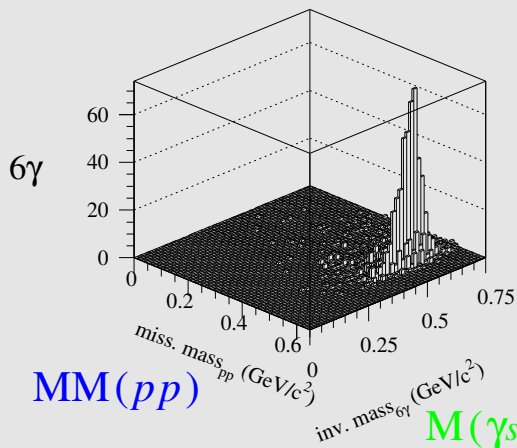
main contribution  
at  
high  $M(\gamma_s)$



$$pp \rightarrow pp\eta (\rightarrow 2\gamma)$$



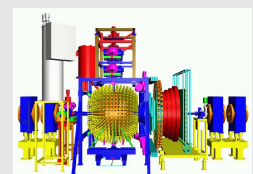
$$pp \rightarrow pp2\pi^0 (\rightarrow 4\gamma)$$



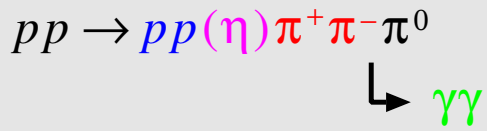
$$pp \rightarrow pp\eta (\rightarrow 3\pi^0 \rightarrow 6\gamma)$$

$MM(pp)$   $M(\gamma_s)$

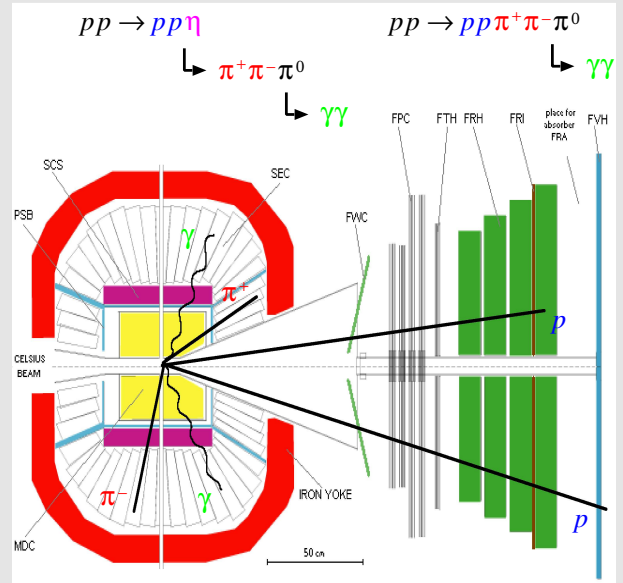
$MM(pp)$



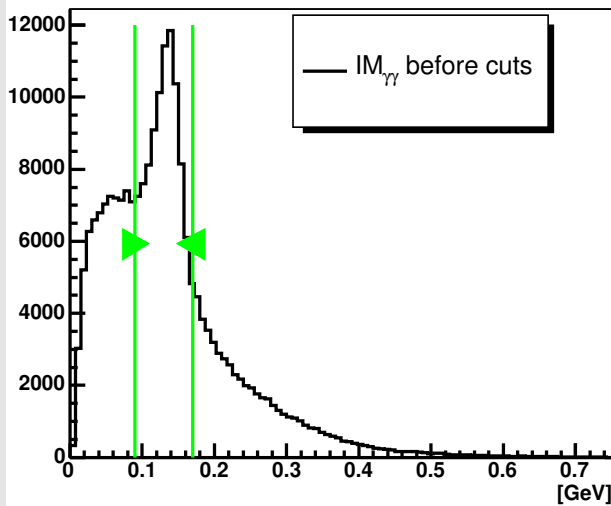
# Event identification



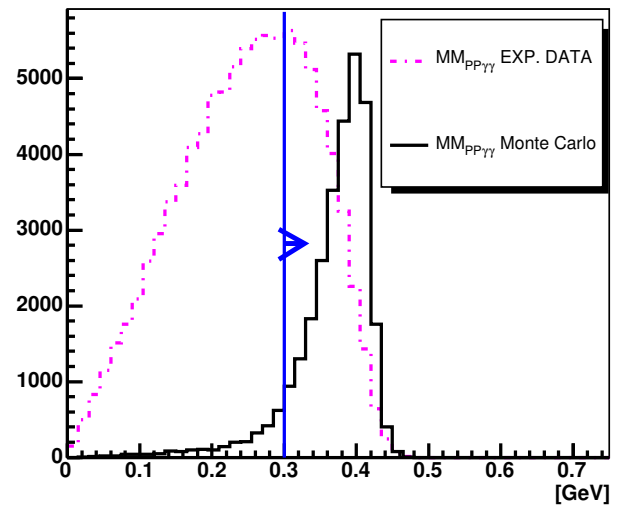
*M. Jacewicz,  
PhD thesis, 2004*



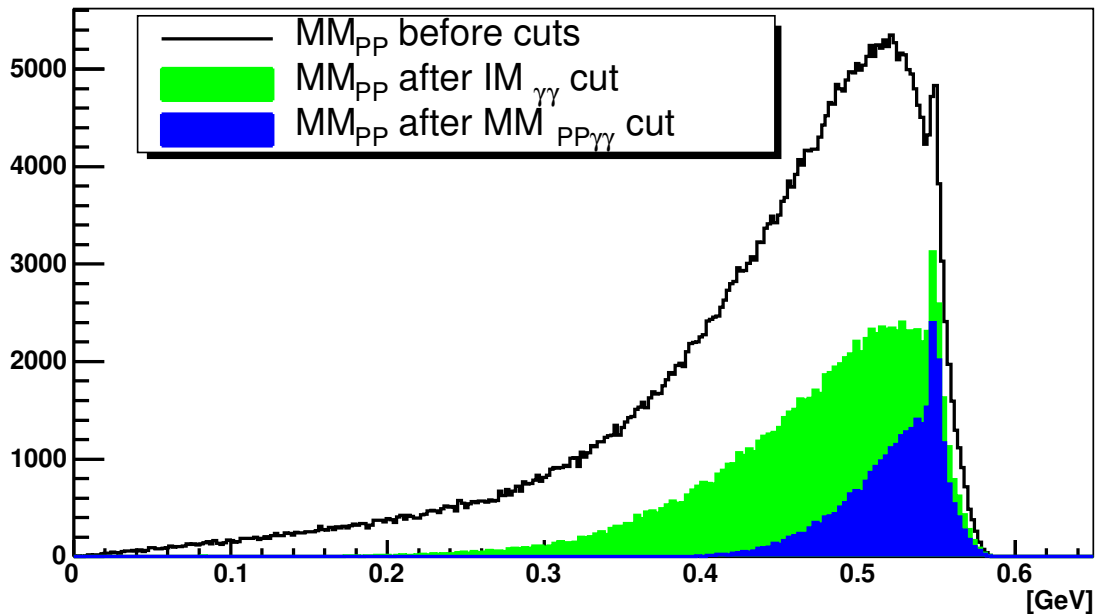
**$\gamma\gamma$  Invariant Mass**



**(PP $\gamma\gamma$ ) Missing Mass**



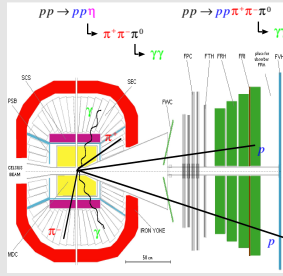
**PP Missing Mass**



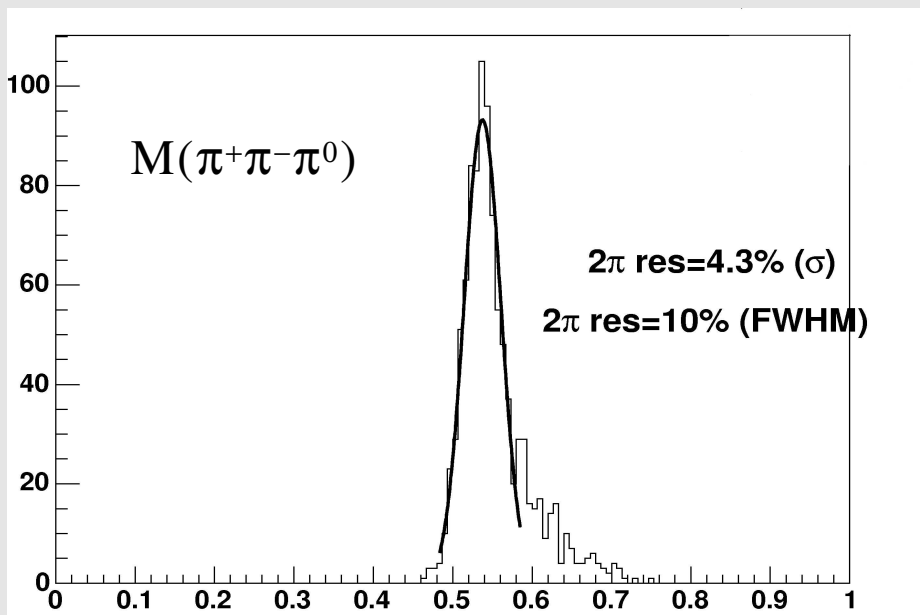
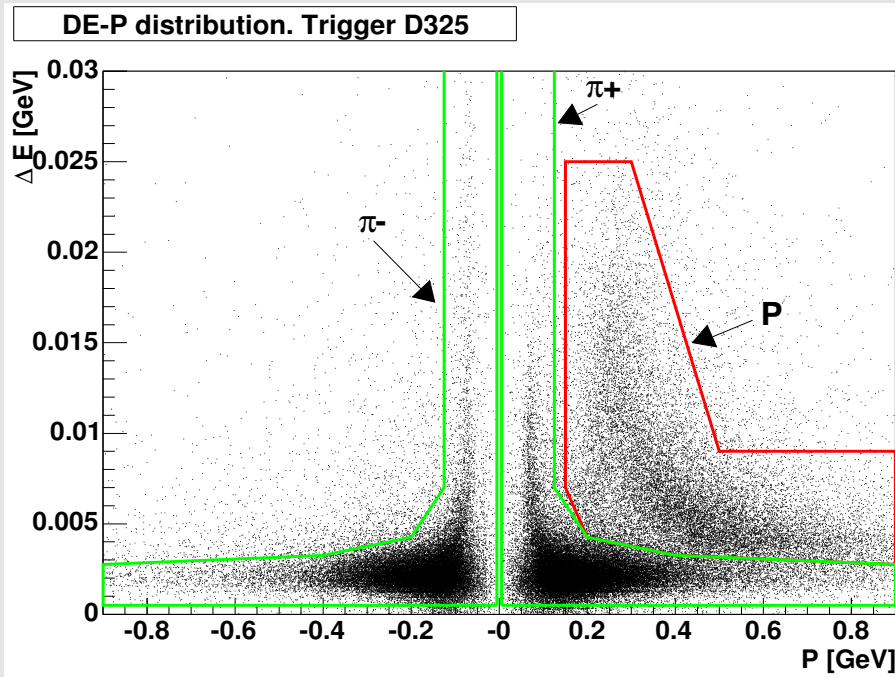
## Event identification

$$pp \rightarrow pp(\eta)\pi^+\pi^-\pi^0 \rightarrow \gamma\gamma$$

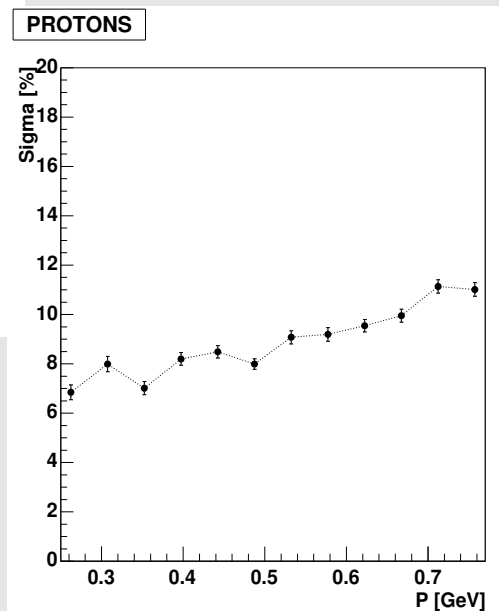
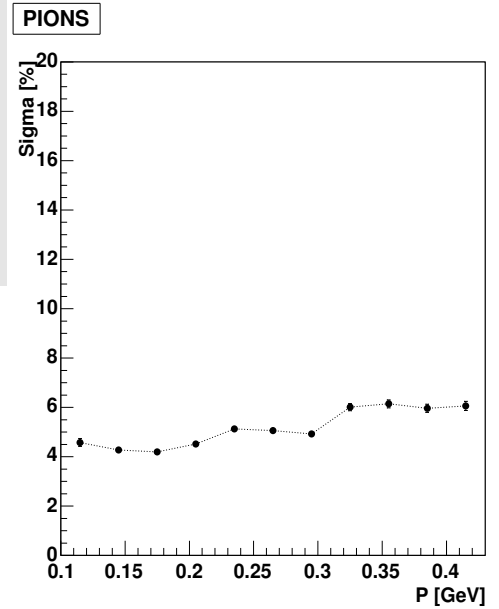
M. Jacewicz,  
PhD thesis, 2004



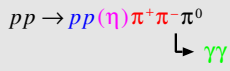
## $\pi^+\pi^-$ identification



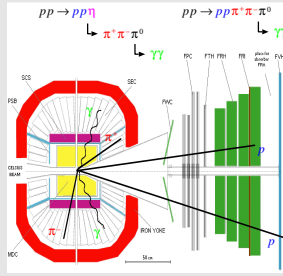
## momentum resolution



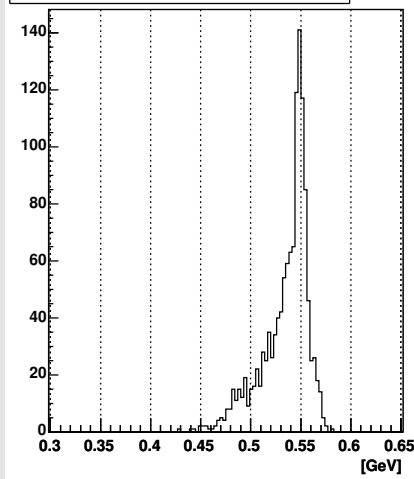
## Event identification



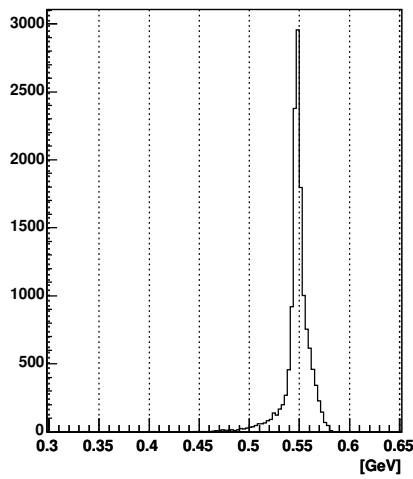
M. Jacewicz,  
PhD thesis, 2004



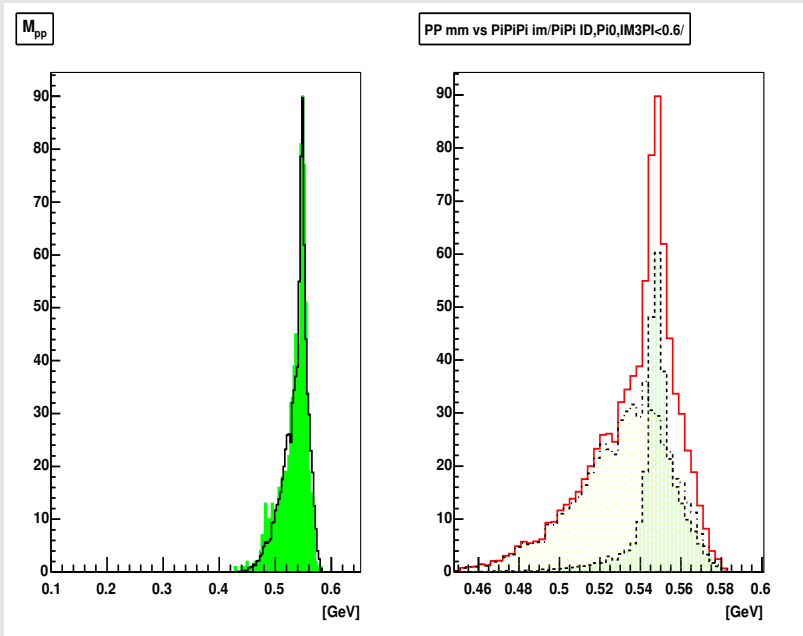
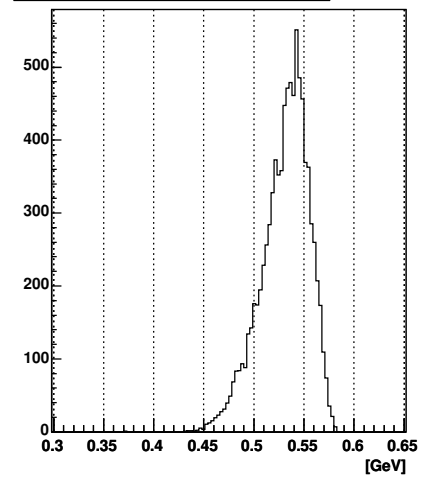
MM<sub>pp</sub> - EXP. DATA after full event recon.



MM<sub>pp</sub> - Monte Carlo  $\eta \rightarrow \pi^+\pi^-\pi^0$



MM<sub>pp</sub> - Monte Carlo  $pp \rightarrow pp\pi^+\pi^-\pi^0$



$$\sigma(pp \rightarrow pp\pi^+\pi^-\pi^0) = 4.6 \pm 1.2^{+0.7}_{-0.9} \mu\text{b}$$

$$\sigma(pp \rightarrow pp\pi^+\pi^-\pi^0) / \sigma(pp \rightarrow pp\eta \rightarrow pp\pi^+\pi^-\pi^0) \approx 4$$

$$\sigma(pp \rightarrow pp\pi^+\pi^-\pi^0) / \sigma(pp \rightarrow pp\pi^0\pi^0\pi^0) \approx 3 \neq 8$$

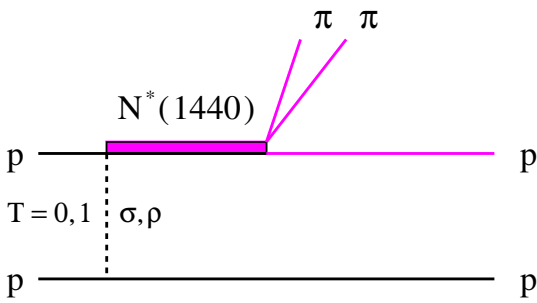
statistical model prediction,  
J. Bartke, Herceg-Novi (1970)



# Two Pion Production in Nucleon-Nucleon Collisions

(L. Alvarez-Ruso, E. Oset, E. Hernández,  
Nucl.Phys.A 633 (1998) 519)

## Reaction Mechanism Near Threshold

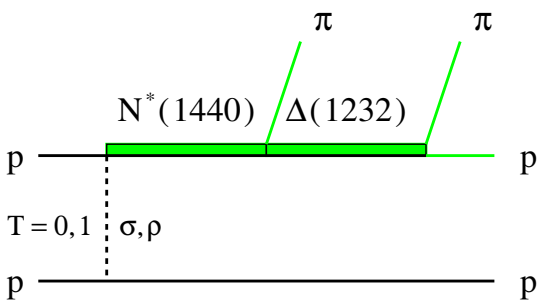


$N^*(1440) P_{11}$  s-wave decay  
5-10% decay directly to  $2\pi$

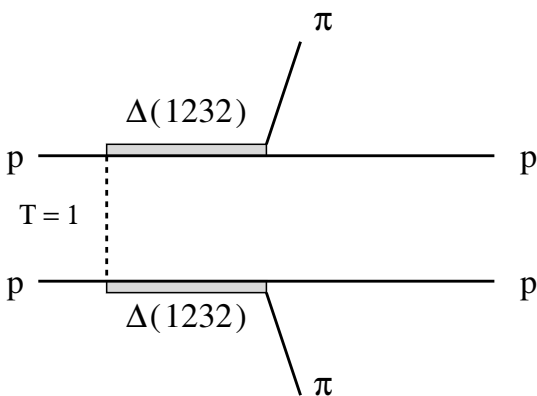
$N^*$  decay amplitude

$$A_{N^*} \approx 1 + c [\mathbf{k}_1 \cdot \mathbf{k}_2 (3D_{\Delta^{++}} + D_{\Delta^0}) + i\mathbf{s} \cdot (\mathbf{k}_1 \times \mathbf{k}_2) (3D_{\Delta^{++}} - D_{\Delta^0})]$$

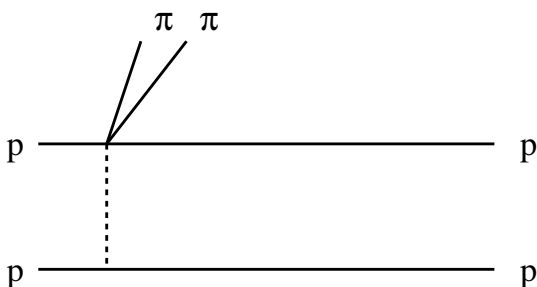
$\mathbf{k}_i = \pi$  momenta (cms),  $D_{\Delta} = \Delta$  propagators,  $\mathbf{s} =$  nucleon spin



$N^*(1440) P_{11}$  s-wave decay  
20-30% decay to  $\Delta\pi$   $\mathbf{k}_1 \cdot \mathbf{k}_2 \leftrightarrow M_{\pi\pi}, \delta_{\pi\pi} = \langle (\mathbf{k}_1, \mathbf{k}_2) \rangle$

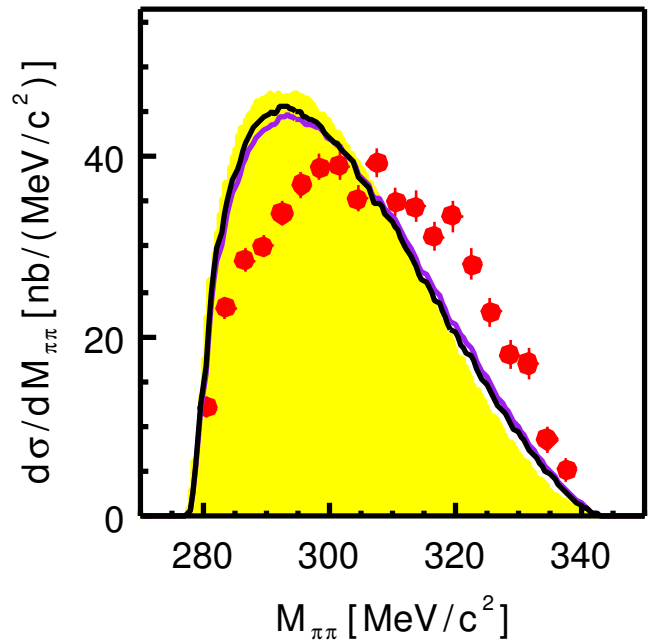
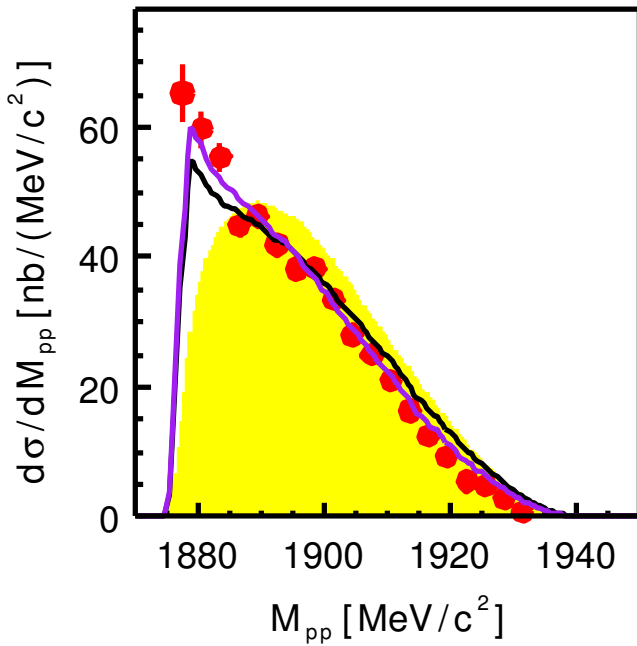


dominated by higher partial waves  
 $\sigma(\theta_{\pi}) \approx 1 + 3\cos^2\theta_{\pi}$



# $pp \rightarrow pp\pi^+\pi^-$ Invariant Mass Distributions

$Q = 64.4 \text{ MeV}$  ( $T_p = 750 \text{ MeV}$ )



● PROMICE/WASA  
(W. Brodowski et al., Phys. Rev. Lett. 88 (2002) 192301)

■ phase space

— phase space + pp FSI

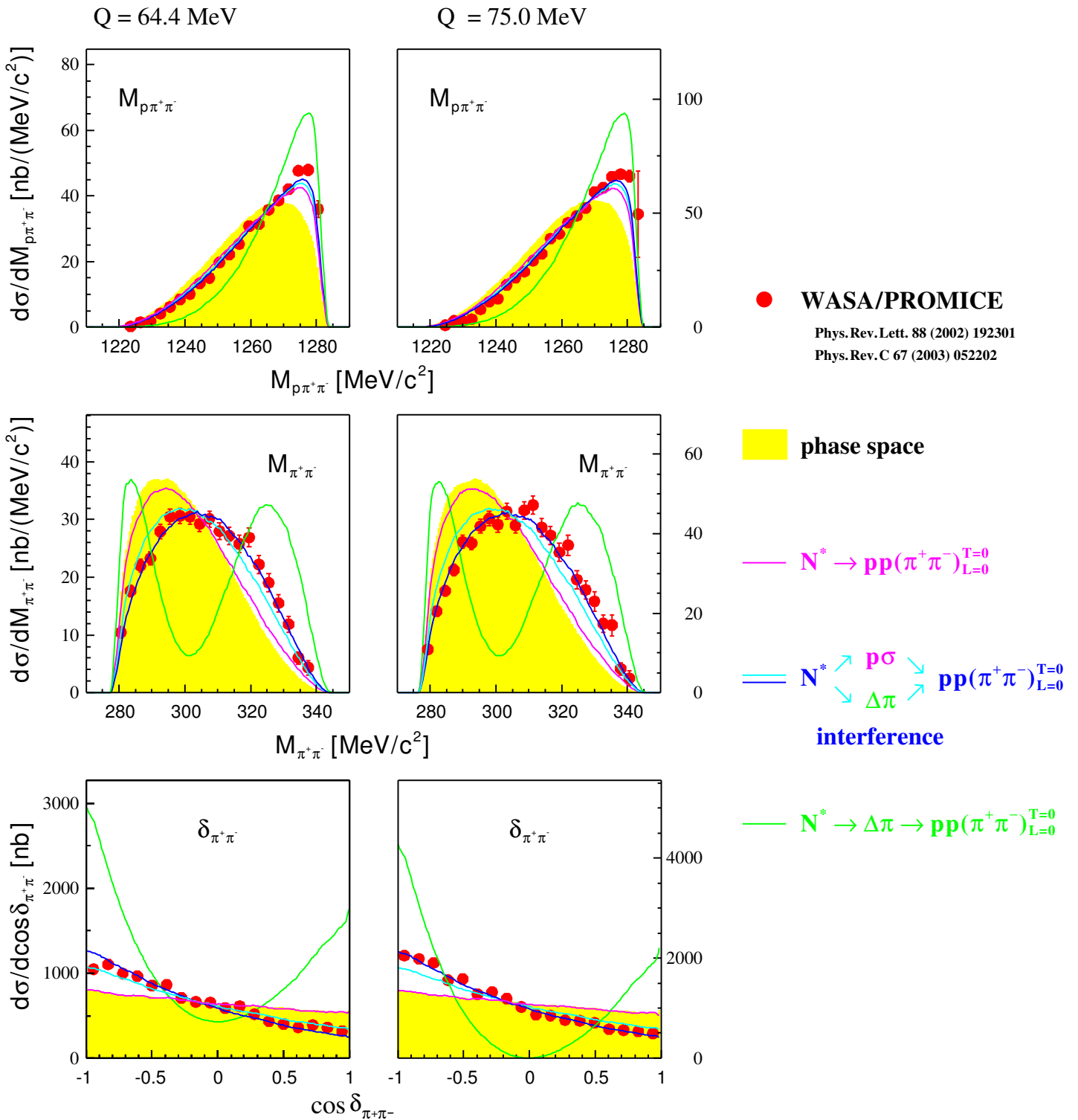
— phase space + pp FSI +  $\sigma$  exchange

phase space + pp FSI

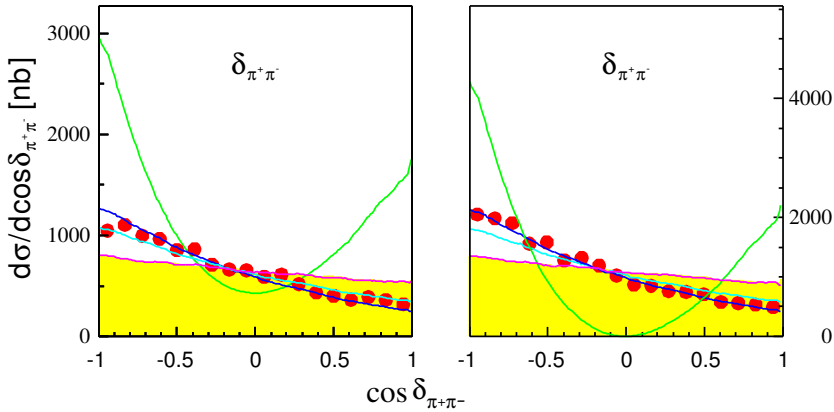
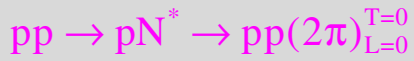
pp invariant mass is reproduced

additional dynamics of  $\pi\pi$  production

# Interference of $N^*$ Decay Routes



# $N^*(1440)$ Partial Decay Widths



$N^*(1440)$  decay amplitude

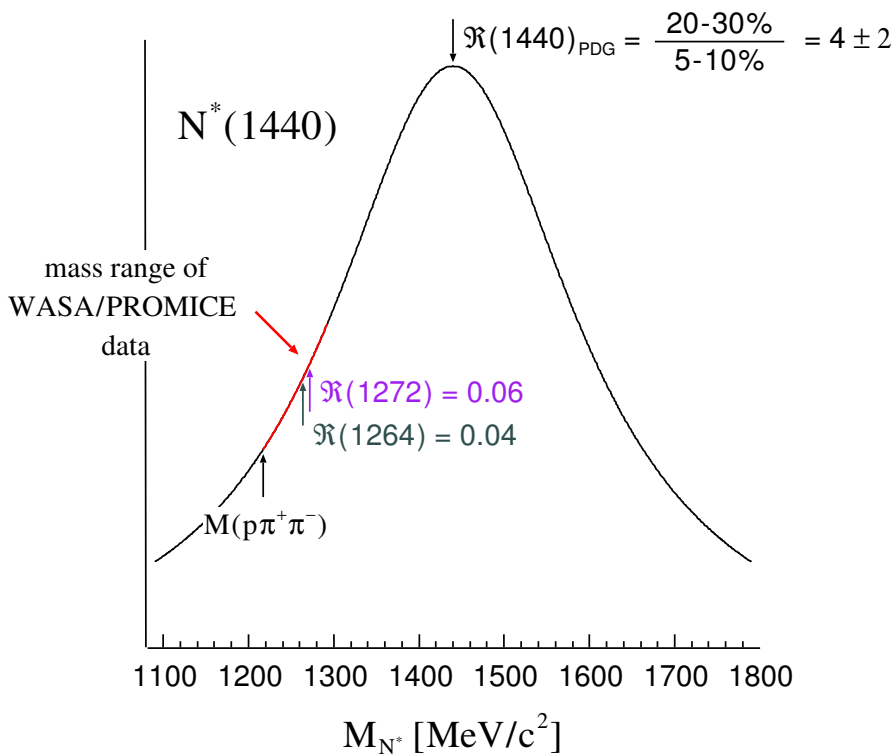
$$A_{N^*} \sim 1 + c \cdot [\mathbf{k}_1 \cdot \mathbf{k}_2 (3D_{\Delta^{++}} + D_{\Delta^0})]$$

$$= A_{N^* \rightarrow N\sigma} + c \cdot A_{N^* \rightarrow \Delta\pi}$$

$\mathbf{k}_i = \pi$  momenta (cms),  $D_{\Delta} = \Delta$  propagators

$$\sigma(\delta_{\pi\pi}) \sim \langle A_{N^*} \rangle^2$$

$$\mathfrak{R}(M_{N^*}) = \frac{\Gamma_{N^* \rightarrow \Delta\pi \rightarrow N\sigma}(M_{N^*})}{\Gamma_{N^* \rightarrow N\sigma}(M_{N^*})} \sim c^2 \cdot \frac{\int |A_{N^* \rightarrow \Delta\pi}|^2 dM_{p\pi^+}^2 dM_{\pi^+\pi^-}^2}{\int |A_{N^* \rightarrow N\sigma}|^2 dM_{p\pi^+}^2 dM_{\pi^+\pi^-}^2}$$

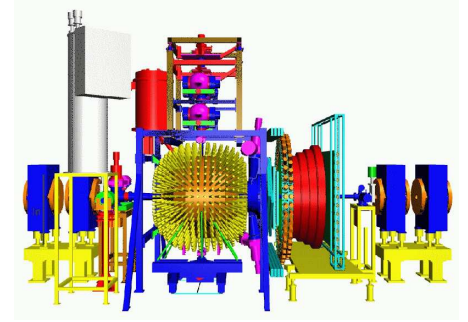
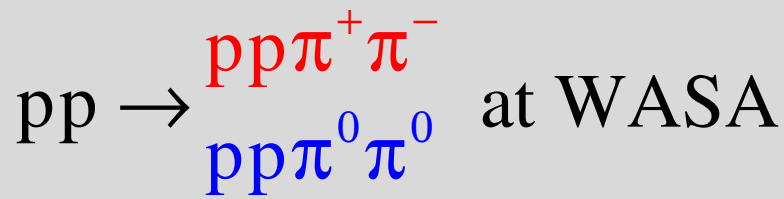


**Extrapolation  
(model dependent!)**

$$\mathfrak{R}(1440) = 3.4 \pm 0.3$$

**Experimental  
programme**

**Energy Dependence**



preliminary results

phase space

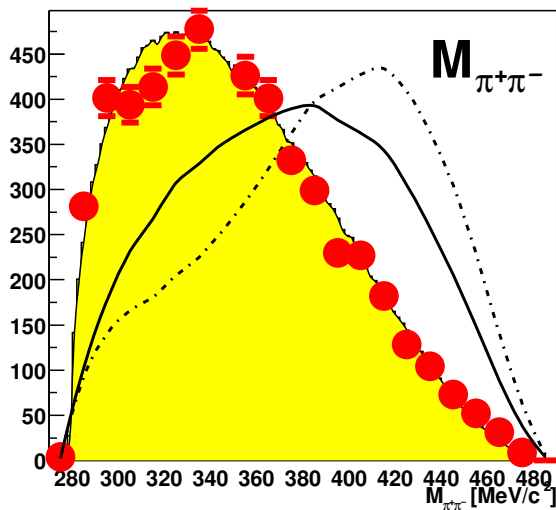
$\Re(1440) = 3$

$\Re(1440) = 1$

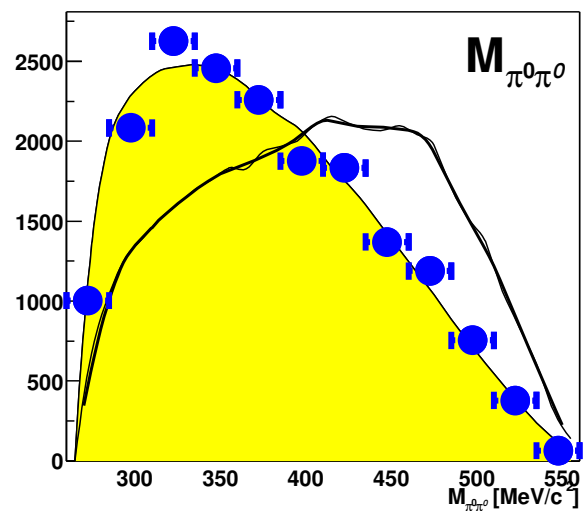
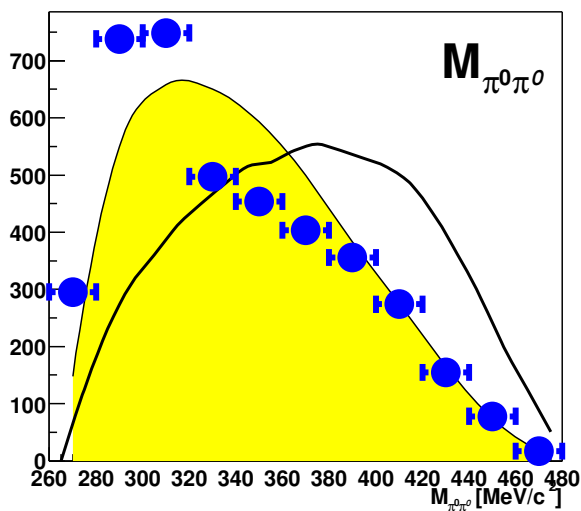
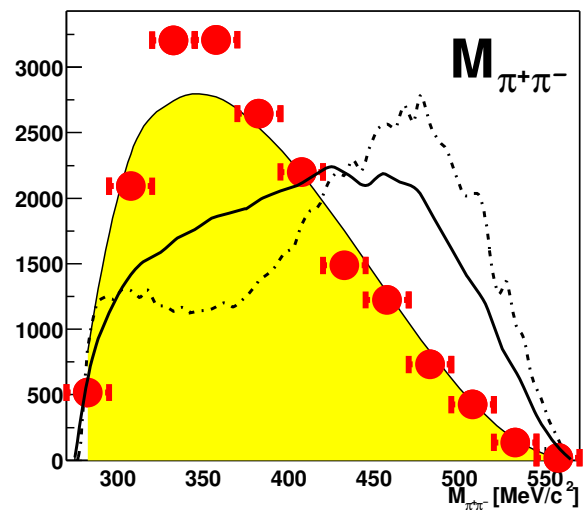
CELSIUS WASA preliminary  $pp \rightarrow pp\pi^+\pi^-$

CELSIUS WASA preliminary  $pp \rightarrow pp\pi^0\pi^0$

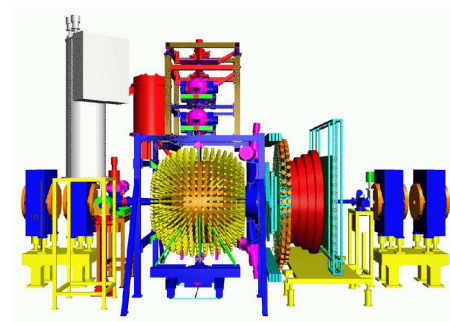
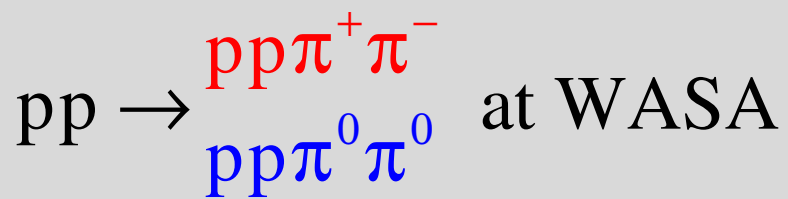
$T_p = 1100 \text{ MeV}$  ( $Q = 208 \text{ MeV}$ )



$T_p = 1300 \text{ MeV}$  ( $Q = 286 \text{ MeV}$ )





Analysis: M. Bashkanov, H. Clement, T. Skorodko,  
University of Tübingen




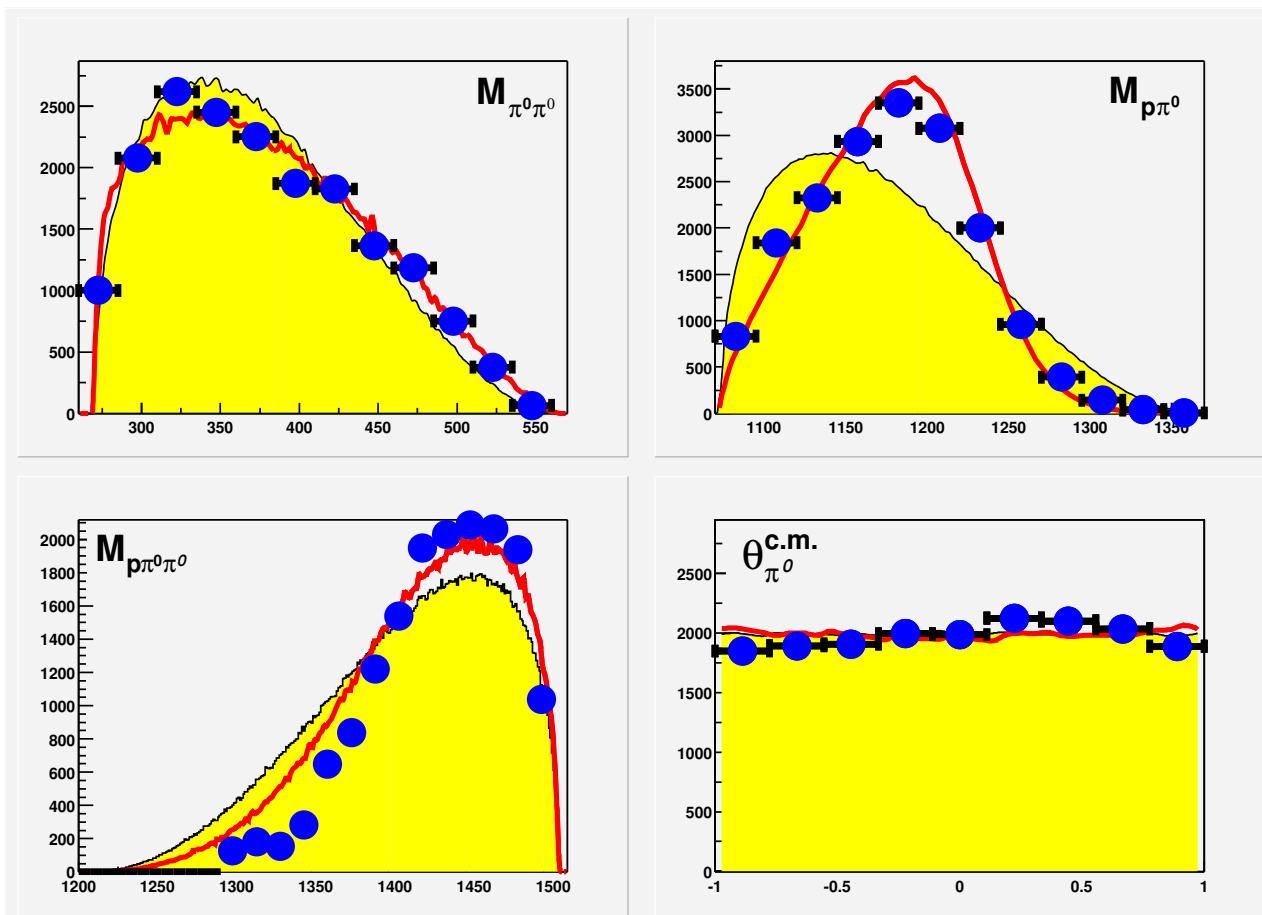
preliminary results

$T_p = 1300 \text{ MeV}$  ( $Q = 286 \text{ MeV}$ )

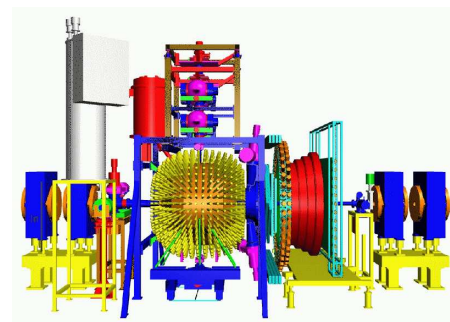
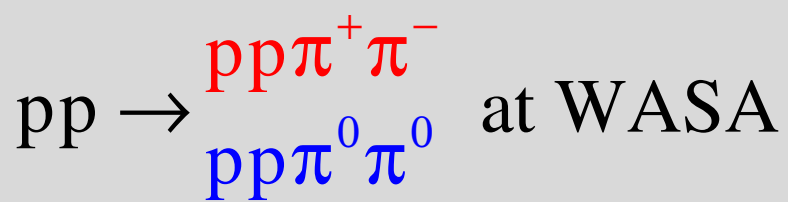
 phase space

 CELSIUS WASA preliminary  $pp \rightarrow pp\pi^0\pi^0$

  $pp \rightarrow (\Delta\Delta)_{J(P)=0(+)} \rightarrow pp\pi^0\pi^0$



Analysis: M. Bashkanov, H. Clement, T. Skorodko,  
University of Tübingen

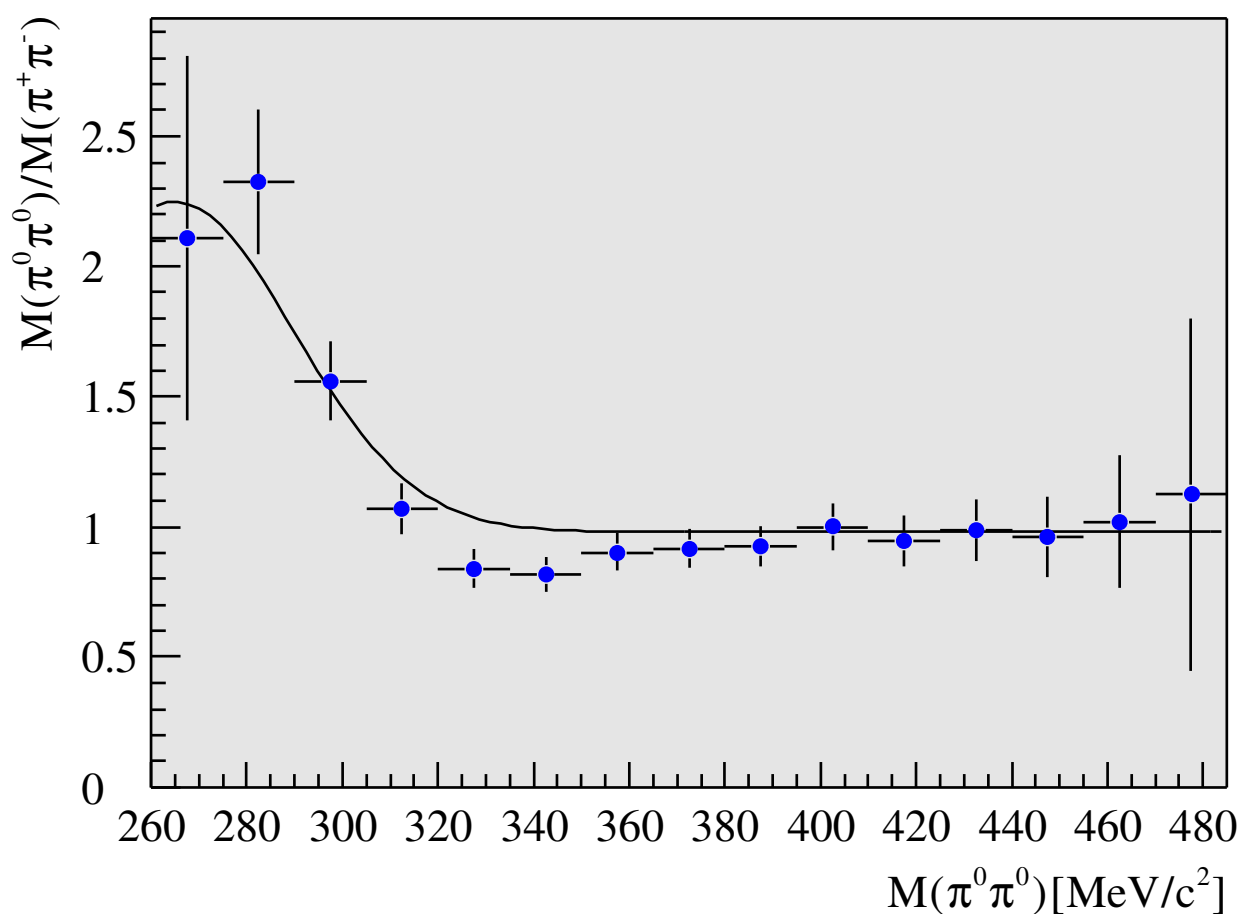


preliminary results

$T_p = 1100 \text{ MeV}$  ( $Q = 208 \text{ MeV}$ )

— fit normalized at large  $M(\pi\pi)$

● CELSIUS WASA preliminary  $pp \rightarrow pp\pi^0\pi^0$  correlation function  $M(\pi^0\pi^0)/M(\pi^+\pi^-)$

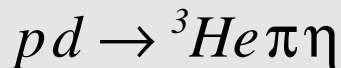
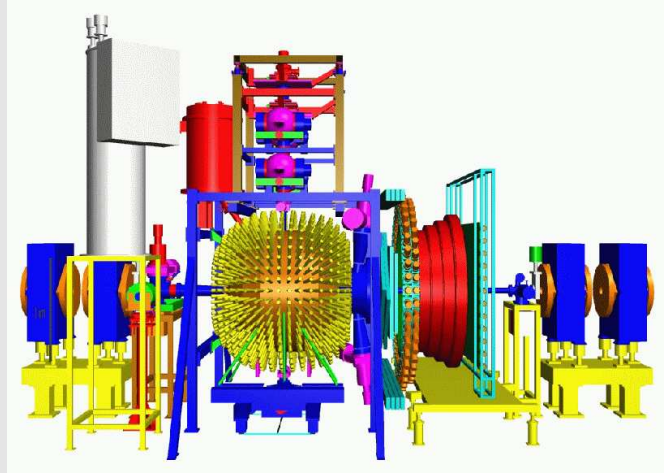


Analysis: M. Bashkanov, H. Clement, T. Skorodko,  
University of Tübingen

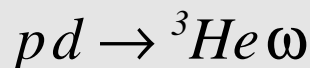
# CELSIUS/WASA Experimental Programme

*until middle of 2005*

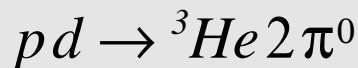
## Production Experiments



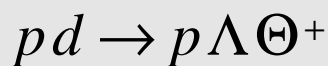
$\pi$ - $\eta$  interaction



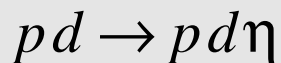
$\omega$  production dynamics



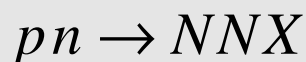
$\pi$ - $\pi$  dynamics



pentaquark search/dynamics



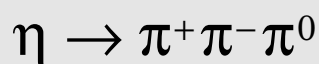
$\eta$ - $d$  interaction,  
 $\eta$  production dynamics



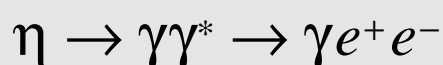
quasifree production

## Not so rare $\eta$ Decays

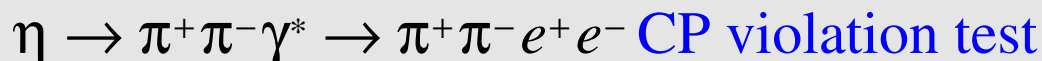
tagging:  $pd \rightarrow {}^3\text{He}\eta$



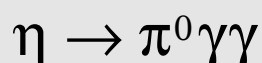
isospin violation



$\eta$  transition form factor



CP violation test

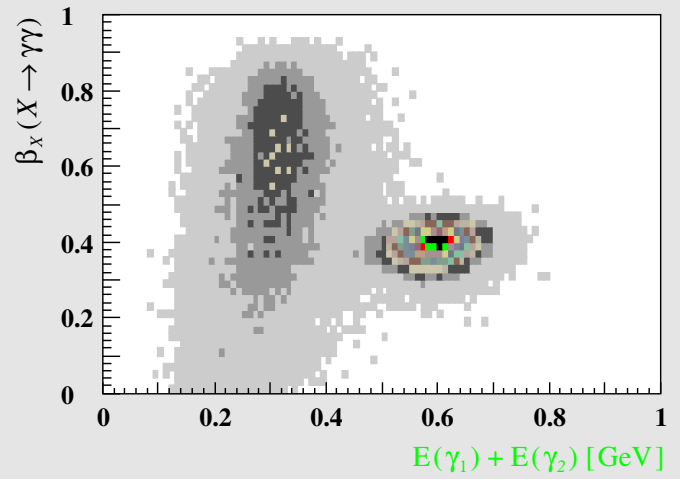
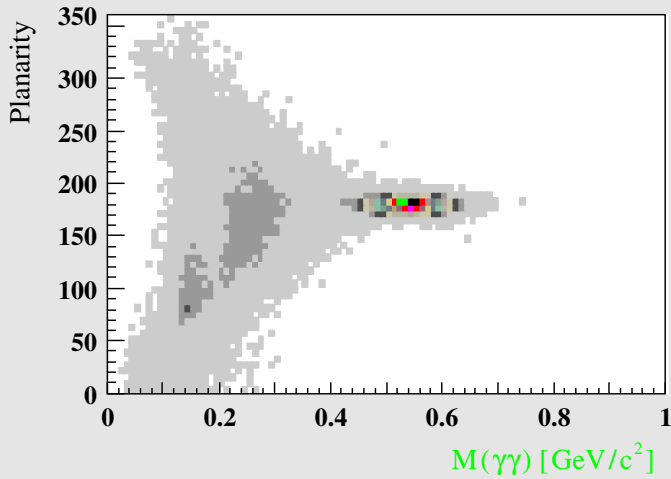


higher order ChPT terms



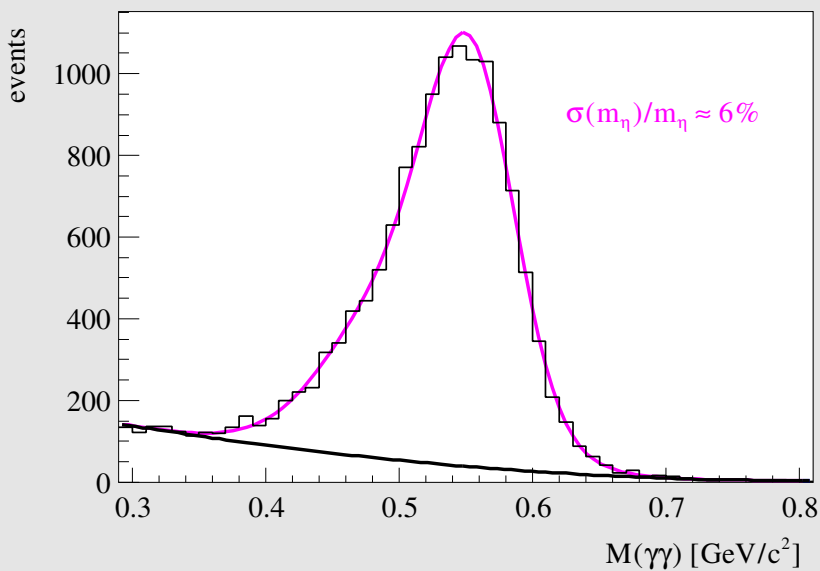
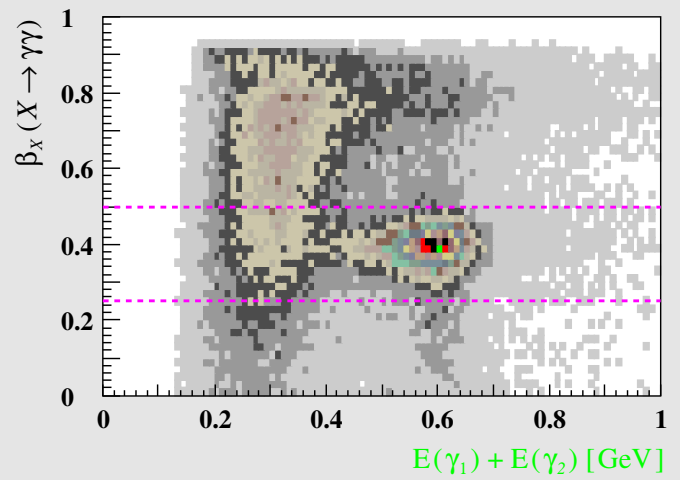
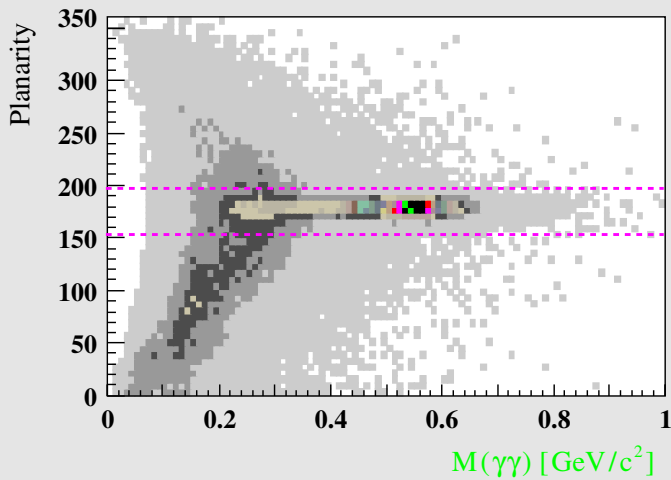
# $\eta$ Tagging in $pd \rightarrow {}^3\text{He}X$

Monte Carlo



preliminary

Data March/June 2004



$\eta$  rate on tape:  
1/s

# Charge Symmetry Breaking

*- Difference between  $u$ - and  $d$ -Quarks -*

## Origin:

- Mass Difference  $m_d - m_u$
- Electromagnetic Energy Differences (charge, magnetic moments)

## Approaches:

- Meson Masses (mass formulae, Coulomb estimates)
- Meson Production
- Meson Decay

# $\pi$ - $\eta$ Mixing In Hadronic $\eta'$ Decays

*H. Machner, A. Magiera,*

*Workshop FEMC04, Jülich, 26-29 Jan 2004*

## Charge Symmetry Breaking

### $(m_d - m_u)$ and $\pi$ - $\eta$ Mixing

*SU(3) singlet and octet representations*

$$|\eta_0\rangle = \frac{1}{\sqrt{3}} (u\bar{u} + d\bar{d} + s\bar{s})$$

$$|\eta_8\rangle = \frac{1}{\sqrt{6}} (u\bar{u} + d\bar{d} - 2s\bar{s})$$

*bare states without CSB*

$$|\tilde{\pi}^0\rangle = \frac{1}{\sqrt{2}} (u\bar{u} - d\bar{d})$$

$$|\tilde{\eta}\rangle = \cos\theta_{PS} |\eta_8\rangle - \sin\theta_{PS} |\eta_0\rangle$$

$$|\tilde{\eta}'\rangle = \sin\theta_{PS} |\eta_8\rangle - \cos\theta_{PS} |\eta_0\rangle$$

*octet-singlet mixing angle  $\theta_{PS} = -20^\circ$  (PDG,  $P \rightarrow \gamma\gamma$ )*

$$\begin{aligned} \langle \tilde{\pi}^0 | H_m | \tilde{\eta} \rangle &= \left\langle \frac{1}{\sqrt{2}} (u\bar{u} - d\bar{d}) \left| m_d d\bar{d} + m_u u\bar{u} + m_s s\bar{s} \right| \frac{1}{\sqrt{3}} (u\bar{u} + d\bar{d} - s\bar{s}) \right\rangle \\ &= \frac{1}{\sqrt{6}} (m_u - m_d) \end{aligned}$$

$\Rightarrow \pi^0, \eta$  mixtures of isospin eigenstates

## Charge Symmetry Breaking

### $(m_d - m_u)$ , $\pi$ - $\eta$ Mixing and $\eta'$ Decays

$\pi^0, \eta$  mixtures of isospin eigenstates

$$|\pi^0\rangle = \cos\theta_{\pi\eta} |\tilde{\pi}^0\rangle + \sin\theta_{\pi\eta} |\tilde{\eta}\rangle$$

$$|\eta\rangle = -\sin\theta_{\pi\eta} |\tilde{\pi}^0\rangle + \cos\theta_{\pi\eta} |\tilde{\eta}\rangle$$

*D.J.Gross, S.B.Treiman, F.Wilczek,  
Phys. Rev. D19 (1979) 2188*

$$\sin\theta_{\pi\eta} = \frac{\sqrt{3}(m_d - m_u)}{4(m_s - \hat{m})}$$

$$\hat{m} = (m_u + m_d) / 2$$

$\eta' \rightarrow \pi\pi\pi$  forbidden

$\eta' \rightarrow \eta\pi\pi$  allowed

by isospin invariance

$$R_1 = \frac{\Gamma(\eta' \rightarrow \pi^0\pi^0\pi^0)}{\Gamma(\eta' \rightarrow \eta\pi^0\pi^0)}$$

$$R_2 = \frac{\Gamma(\eta' \rightarrow \pi^0\pi^+\pi^-)}{\Gamma(\eta' \rightarrow \eta\pi^+\pi^-)}$$

*D.J.Gross, S.B.Treiman, F.Wilczek,  
Phys. Rev. D19 (1979) 2188*

*G.Ecker, G.Müller, H.Neufeld, A.Pich,  
Phys. Lett. B477 (2000) 88*

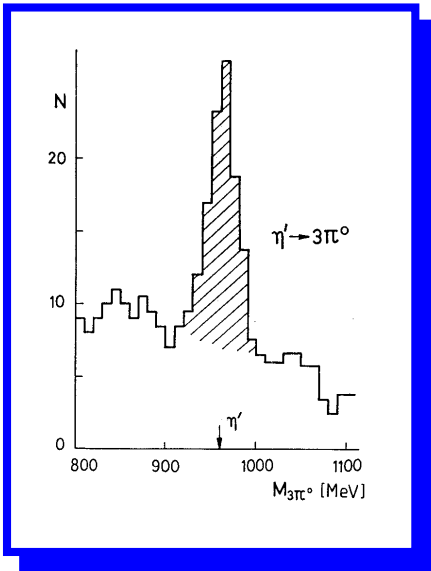
$$R_i = P_i \sin^2\theta_{\pi\eta}$$

$P_i$  = Ratios of Phase Space Volumes

$$P_1 = 14.0, P_2 = 15.2$$

## Charge Symmetry Breaking

### Existing Data $\pi$ - $\eta$ Mixing from $\eta'$ Decays



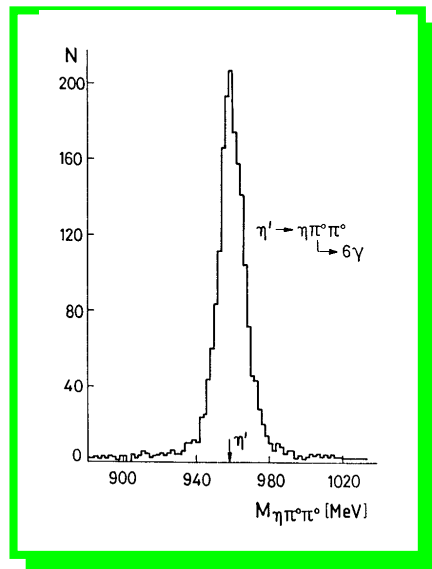
GAMS-2000

D. Alde et al.,  
Z. Phys. C 36 (1987) 603  
F. Binon et al.,  
Phys. Lett. B 140 (1984) 264

$$\eta' \rightarrow \pi^0 \pi^0 \pi^0$$

$$R_2 = \frac{\Gamma(\eta' \rightarrow \pi^0 \pi^0 \pi^0)}{\Gamma(\eta' \rightarrow \eta \pi^0 \pi^0)} = (7.4 \pm 1.2) \times 10^{-3}$$

$$\sin \Theta_{\pi\eta} = 0.023 \pm 0.002$$



$$\eta' \rightarrow \pi^0 \pi^+ \pi^-$$

$$R_1 = \frac{\Gamma(\eta' \rightarrow \pi^0 \pi^+ \pi^-)}{\Gamma(\eta' \rightarrow \eta \pi^+ \pi^-)} < 0.11$$

## $\pi$ - $\eta$ Mixing

### In Hadronic $\eta'$ Decays with WASA@COSY

H. Machner, A. Magiera,  
Workshop FEMC04,  
Jülich, 26-29 Jan 2004

$\sin\theta_{\pi\eta}$  Literature:

$0.023 \pm 0.002$	$\eta' \rightarrow 3\pi^0 / \eta 2\pi^0$	F. Binon et al. (GAMS-2000), PL B 140 (1984) 264
$\approx 0.010$	Meson Masses, Dashen's Theorem	A.J. Gross, S.B. Treiman, F. Wilczek, PR D 19 (1979) 2188
0.010	Meson and Baryon Masses, Dashen's Theorem	J. Gasser, H. Leutwyler, Phys. Rep. 87 (1982) 77
$0.034 \pm 0.013$	Radiative Decays, Anomalous Ward Identities	B. Bagchi, A. Lahiri, S. Niyogi, PR D 41 (1990) 2871

$\eta'$  Tagging:  $pp \rightarrow pp\eta'$

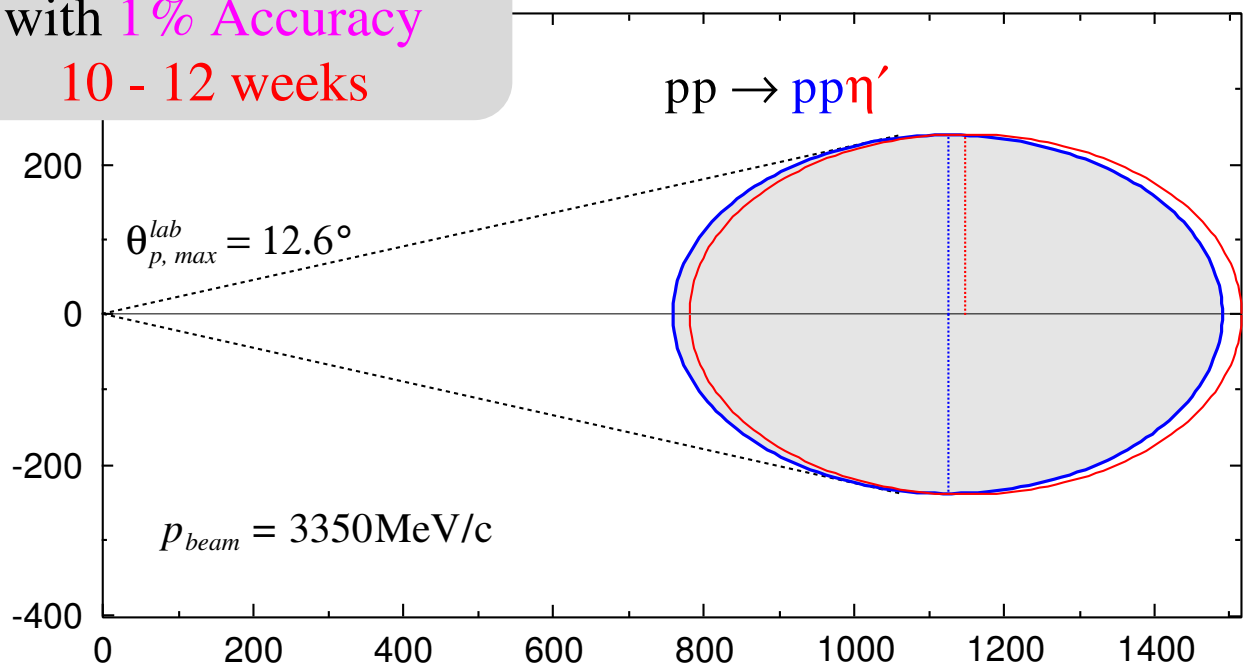
Beam Momentum: 3350 MeV/c

Cross Section: 300 nb

A. Khoukaz et al. (COSY-11),  
Eur. Phys. J. A 20 (2004) 345

Luminosity:  $10^{32} \text{ cm}^{-2} \text{ s}^{-1}$

Beam Time Estimate:  
Measurement of  $\sin\theta_{\pi\eta}$   
with 1% Accuracy  
10 - 12 weeks



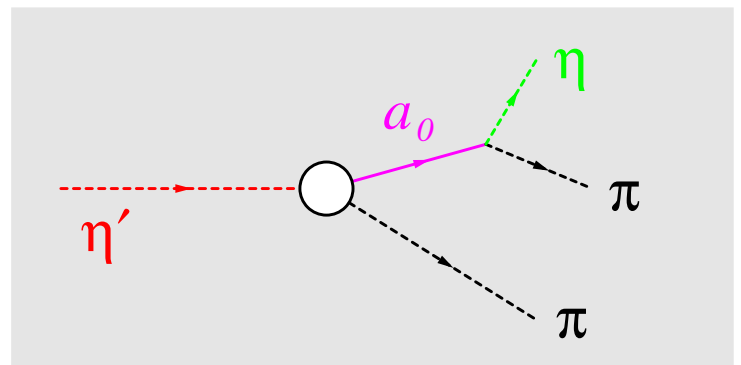
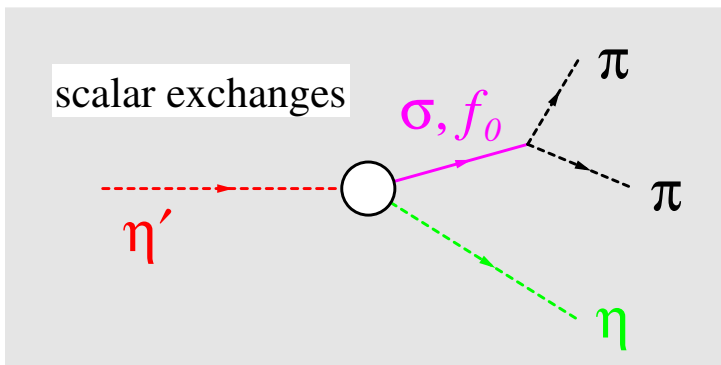
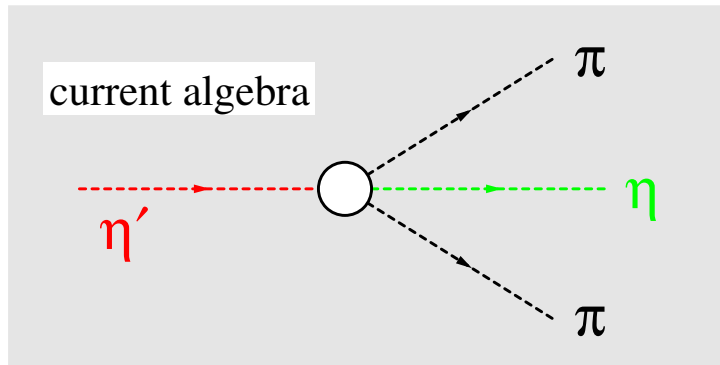
$$\eta' \rightarrow \eta \pi \pi$$

# A View on the Scalars I

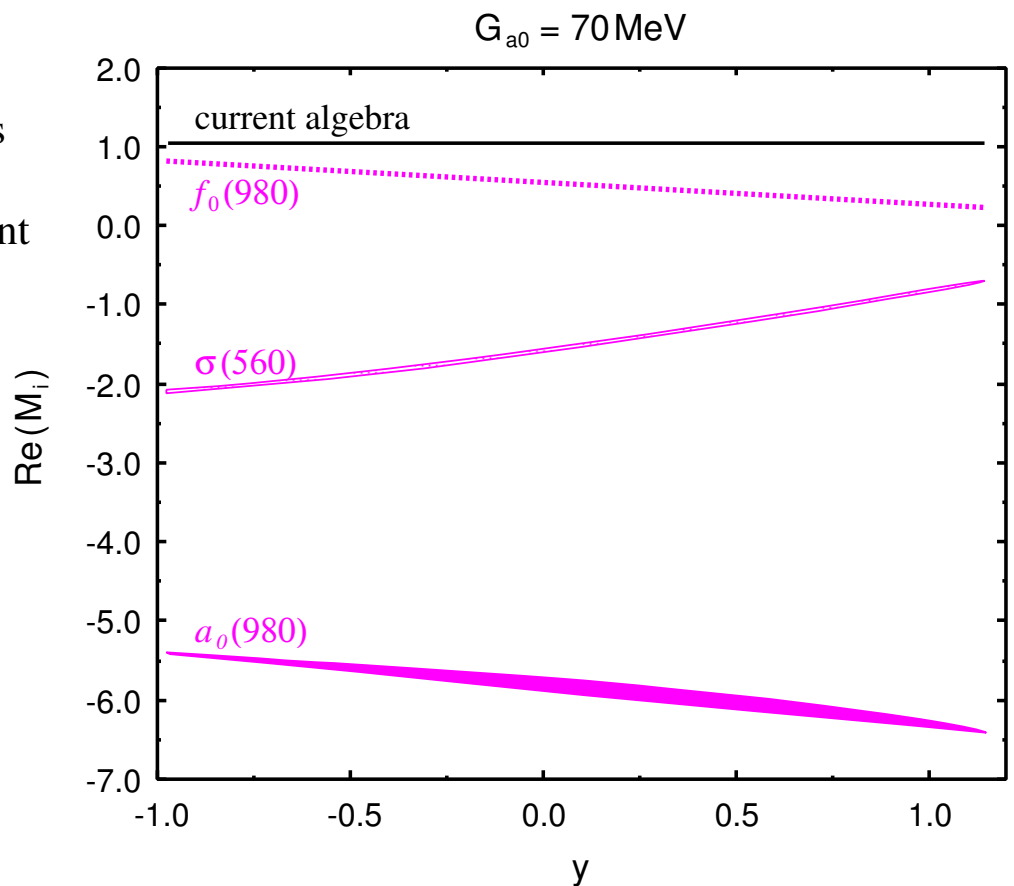
A. H. Fariborz, J. Schechter,  
*Phys. Rev. D* 60 (1999) 034002

effective chiral Lagrangian  
 including scalar nonet:  
 $\sigma(560), \kappa(900), f_0(980), a_0(980)$

scalar-pseudoscalar-pseudoscalar  
 interaction parameters:  
 $\pi\pi, \pi K$  scattering,  $\eta' \rightarrow \eta \pi \pi$



Scalar Contributions  
 in  
 Decay Matrix Element



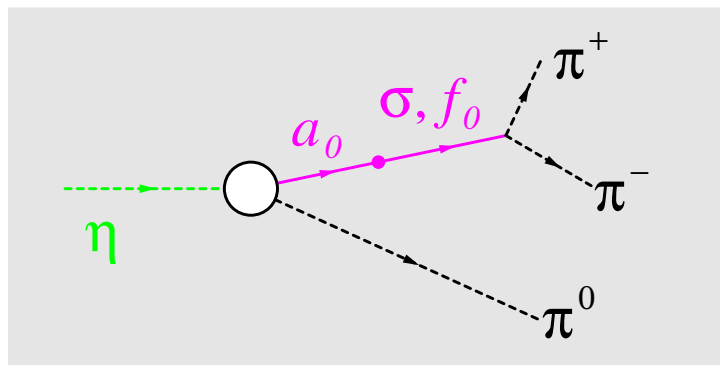
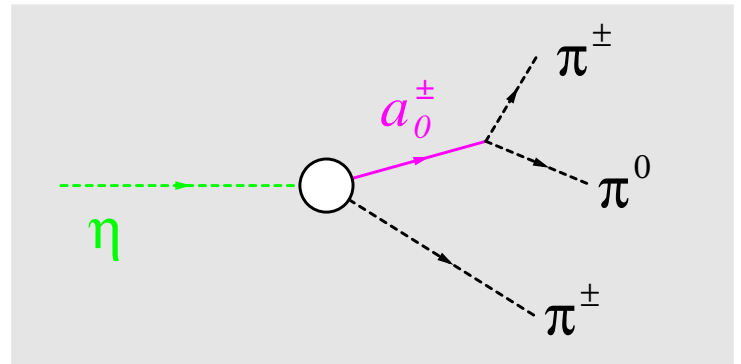
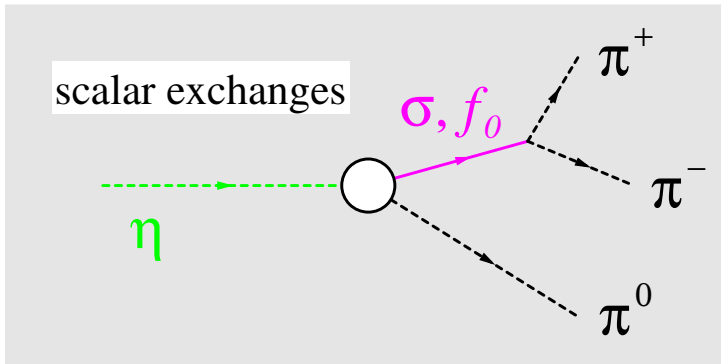
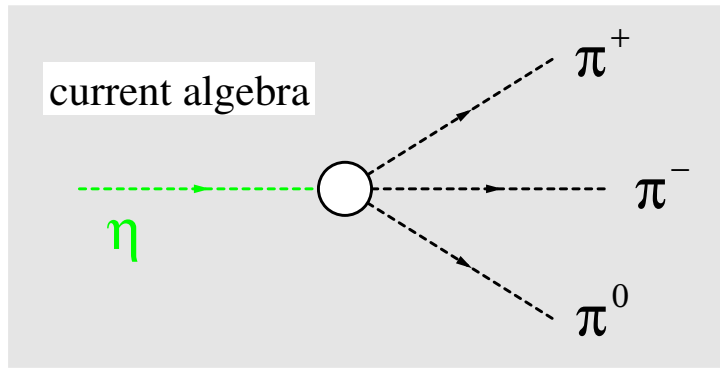
$$\eta \rightarrow \pi\pi\pi$$

## A View on the Scalars II

*A. Abdel-Rehim, D. Black,  
A. H. Fariborz, J. Schechter,  
Phys. Rev. D 67 (1003) 054001*

effective chiral Lagrangian  
including scalar nonet:

$\sigma(560), \kappa(900), f_0(980), a_0(980)$



Scalar Contributions  
in  
Decay Rate

$< 30\%$

for  $\eta'$ :  $a_0, f_0$  propagators closer to mass shell



## Hadronic Decays of the $\eta'$

	Branching Ratio	Existing Data	Count Rate Estimate WASA@COSY per day
$\pi^+ \pi^- \eta$	$44.3 \pm 1.5 \%$	388 / 8090	18000
$\pi^0 \pi^0 \eta$	$20.9 \pm 1.2 \%$	4 / 5400	14500
$3 \pi^0$	$5.56 \pm 0.26 \times 10^{-3}$	$\approx 70$	145
$\pi^+ \pi^- \pi^0$	$< 5 \%$		(2700)
$\rho^0 \pi^0$	$< 4 \%$		(2100)
$2 \pi^+ 2 \pi^-$	$< 1 \%$		(260)
$4 \pi^0$	$< 5 \times 10^{-4}$		(8)

### Experimental Conditions

Luminosity	$1 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$
Efficiency	present WASA setup including reconstruction efficiency
Tagging	$pp \rightarrow pp\eta'$ 3.350 GeV/c (Q = 45 MeV)
Cross Section	300 nb

## Radiative Decays

Bull. Frère, T, T, T  
PL 8365 (96) 36

$$|\chi'\rangle = |\chi_B\rangle \sin\theta + |\chi_0\rangle \cos\theta$$

Axial Current "Anomaly"

$$\partial_\mu A_B^\mu = \frac{2}{f_B} (m_u \bar{u} i \gamma_5 u + m_d \bar{d} i \gamma_5 d - 2 m_s \bar{s} i \gamma_5 s)$$

$$\begin{aligned} \partial_\mu A_0^\mu &= \frac{2}{f_0} (m_u \bar{u} i \gamma_5 u + m_d \bar{d} i \gamma_5 d + m_s \bar{s} i \gamma_5 s) \\ &\quad + \frac{1}{f_3} \frac{3}{4} \frac{m_s}{\pi} G_{\mu\nu}^A \tilde{G}^{\mu\nu} \end{aligned}$$

Couplings of  $\chi$  to  $\partial_\mu A^\mu$

$$\langle 0 | \partial_\mu A_B^\mu | \chi' \rangle = m_{\chi'}^2 f_B \sin\theta$$

$$\langle 0 | \partial_\mu A_0^\mu | \chi' \rangle = m_{\chi'}^2 f_0 \cos\theta$$

$m_u = m_d = 0 \Rightarrow$  matrix element of strong anomaly over vacuum

$$\langle 0 | \frac{3}{4} \frac{m_s}{\pi} G_{\mu\nu}^A \tilde{G}^{\mu\nu} | \chi' \rangle = \sqrt{\frac{3}{2}} m_{\chi'}^2 \left( \underline{f_B \sin\theta} + \sqrt{2} \underline{f_0 \cos\theta} \right)$$

$\Rightarrow$  fix  $f_B(\theta), f_0(\theta)$

$$\Gamma(\chi \rightarrow \gamma\gamma) = \frac{m_{\chi'}^2}{36\pi^2} \alpha^2 \left( \frac{\sin\theta}{f_B} + \frac{2\sqrt{2} \cos\theta}{f_0} \right)^2$$

$$\Gamma(\chi \rightarrow \gamma\gamma) = \frac{m_{\chi'}^2}{36\pi^2} \alpha^2 \left( \frac{\cos\theta}{f_B} - \frac{2\sqrt{2} \sin\theta}{f_0} \right)^2$$

still needed:  $\Gamma(P \rightarrow V\gamma) = \frac{\alpha}{8} g_{VP\gamma}^2 \left( \frac{m_P^2 - m_V^2}{m_P} \right)$

$$g_{\omega\eta\gamma} \propto \frac{\cos\theta}{4f_0} (\sqrt{2} \cos\theta_V - \sin\theta_V) - \frac{\sin\theta}{2\sqrt{2}f_0} \sin\theta_V$$

$$g_{\eta\eta'\gamma} \propto$$

## Radiative Decays of the $\eta'$

	Branching Ratio	Existing Data	Count Rate Estimate WASA@COSY per day
$\rho^0 \gamma$	$29.5 \pm 1.0 \%$	1300 + 7000	44000
$\omega \gamma$	$3.03 \pm 0.31 \%$	$\approx 160$	1200
$\gamma \gamma$	$2.12 \pm 0.14 \%$	2767	17100
$\pi^0 \gamma \gamma$	$< 8 \times 10^{-4}$		(250)

### Experimental Conditions

Luminosity	$1 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$
Efficiency	present WASA setup including reconstruction efficiency
Tagging	$pp \rightarrow pp\eta'$ 3.350 GeV/c (Q = 45 MeV)
Cross Section	300 nb

# Glue Content of the $\eta'$

*E. Kou,*

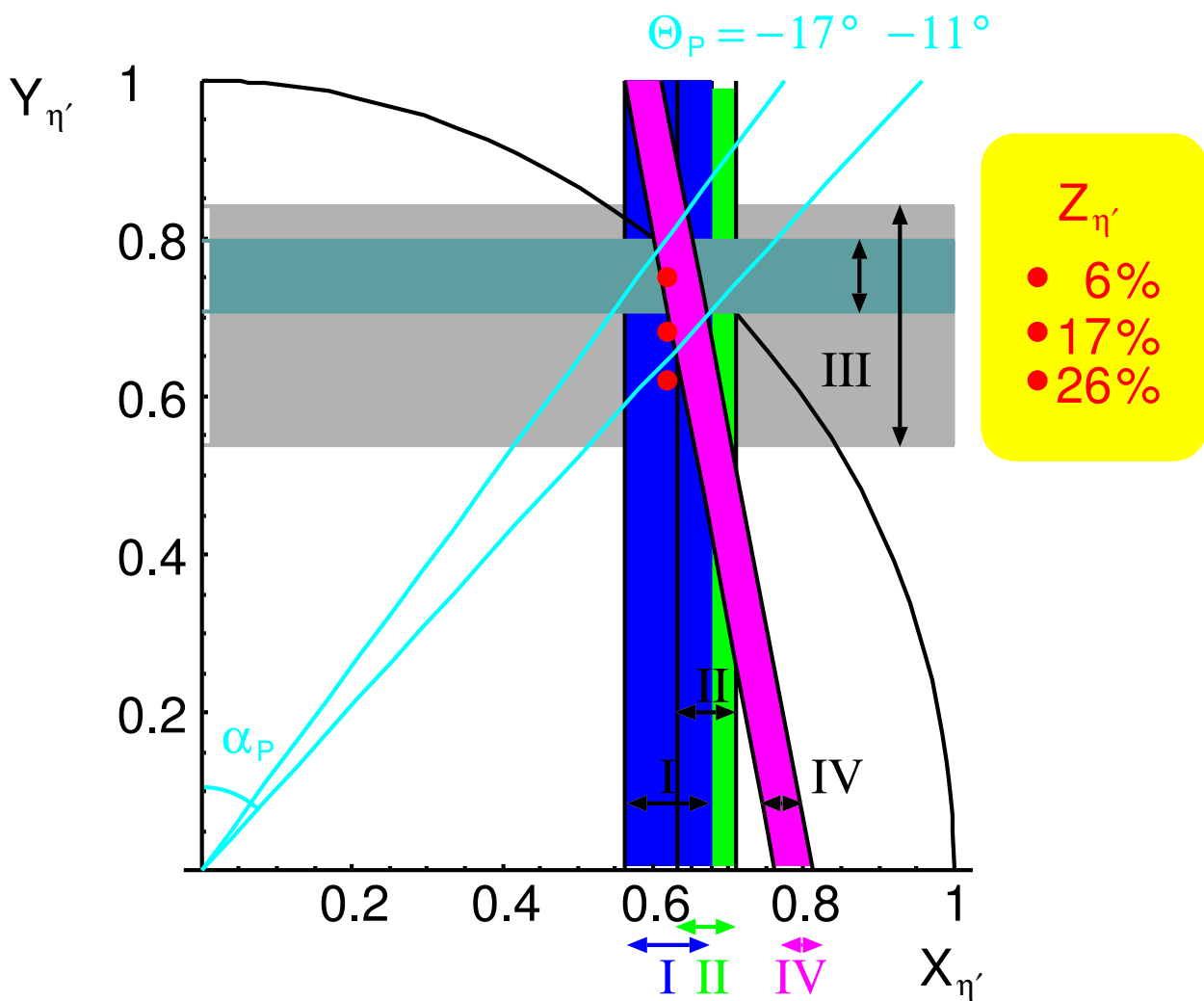
Phys. Rev. D63 (2001) 054027

*J. L. Rosner,*

Phys. Rev. D27 (1983) 1101

$$|\eta\rangle = X_\eta |u\bar{u} + d\bar{d}\rangle / \sqrt{2} + Y_\eta |s\bar{s}\rangle$$

$$|\eta'\rangle = X_{\eta'} |u\bar{u} + d\bar{d}\rangle / \sqrt{2} + Y_{\eta'} |s\bar{s}\rangle + Z_{\eta'} |\text{gluonium}\rangle$$



- |     |                                  |            |                                                    |
|-----|----------------------------------|------------|----------------------------------------------------|
| I   | $\eta' \rightarrow \omega\gamma$ | BR =       | $(3.0 \pm 0.3) \times 10^{-2}$                     |
| II  | $\eta' \rightarrow \rho\gamma$   | BR =       | $(3.0 \pm 0.13) \times 10^{-1}$                    |
| III | $\Phi \rightarrow \eta'\gamma$   | BR =       | $(8.2_{-1.9}^{+2.1} \pm 1.1) \times 10^{-5}$ CMD-2 |
|     | $\Phi \rightarrow \eta'\gamma$   | BR =       | $(8.2_{-1.9}^{+2.1} \pm 1.1) \times 10^{-5}$ KLOE  |
| IV  | $\eta' \rightarrow \gamma\gamma$ | $\Gamma =$ | $(0.20 \pm 0.016) \text{ MeV}$                     |

# Anomalies in QCD : Triangle and Box

starting point: Wess-Zumino Lagrangian

Gess, Zumino  
Phys Lett B 37 (1971) 95

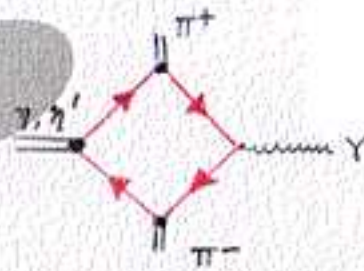
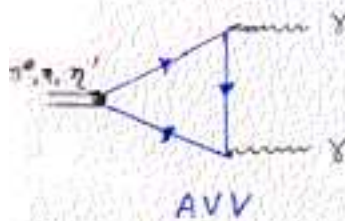
classical triangle anomaly

Adler, PR 117 (1969) 2426

Bell, Jackiw NC 60 (1969) 47

higher order anomalies

box anomaly



Amplitudes

$$M(X \rightarrow \gamma\gamma) =$$

$$B_X(k_1, k_2) \epsilon_{\mu\nu\alpha\beta} k_1^\alpha k_2^\beta \epsilon^\mu(\gamma_1) \epsilon^\nu(\gamma_2)$$

$$M(X \rightarrow \pi^+\pi^-\gamma) =$$

$$E_X(p, k, p-k) \epsilon_{\mu\nu\alpha\beta} \epsilon^\alpha(\gamma) k^\beta p_\nu^+ p_\mu^-$$

Chauowitz Equations

Low Energies

M.S. Chauowitz,  
Phys Rev Lett 35 (1975) 947

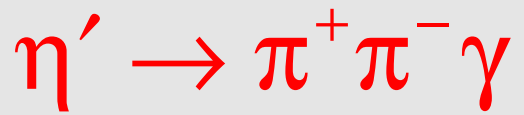
$$B_\eta(0) = -\frac{\alpha_{em}}{\pi\sqrt{3}} \left[ \cos\theta_{ps}/f_0 - 2\sqrt{2} \xi \sin\theta_{ps}/f_0 \right]$$

$$B_{\eta'}(0) = -\frac{\alpha_{em}}{\pi\sqrt{3}} \left[ \sin\theta_{ps}/f_0 + 2\sqrt{2} \xi \cos\theta_{ps}/f_0 \right]$$

$$E_\eta(0) = -\frac{e}{4\pi^2\sqrt{3}} \frac{1}{f_\pi^2} \left[ \cos\theta_{ps}/f_0 - \sqrt{2} \frac{\sin\theta_{ps}}{f_0} \right]$$

$$E_{\eta'}(0) = -\frac{e}{6\pi^2\sqrt{3}} \frac{1}{f_\pi^2} \left[ \sin\theta_{ps}/f_0 + \sqrt{2} \frac{\cos\theta_{ps}}{f_0} \right]$$

$$\Gamma(X \rightarrow \gamma\gamma) = \frac{m_X^2}{32\pi} |B_X(0)|^2$$

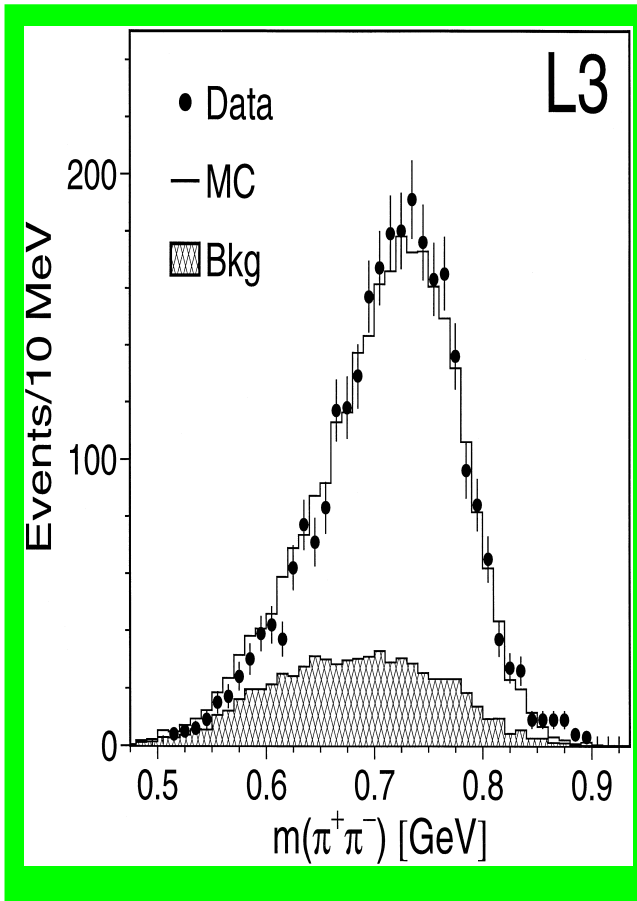


Evidence for  
Box Anomaly?

⇐ *M. Acciarri et al. (L3),*  
Phys. Lett. B 418 (1998) 399

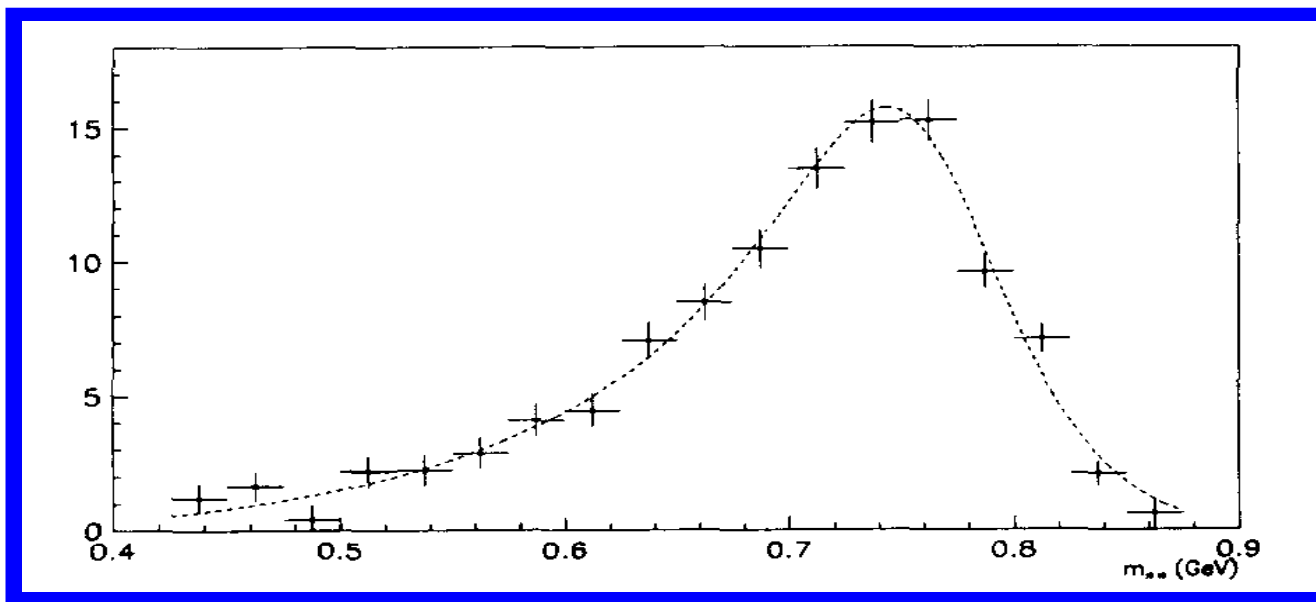
$$\xi = 0 \quad (\text{CL} = 37\%)$$

$$(\xi = 0.4, \phi = 3.14 \Rightarrow \text{CL} = 3\%)$$



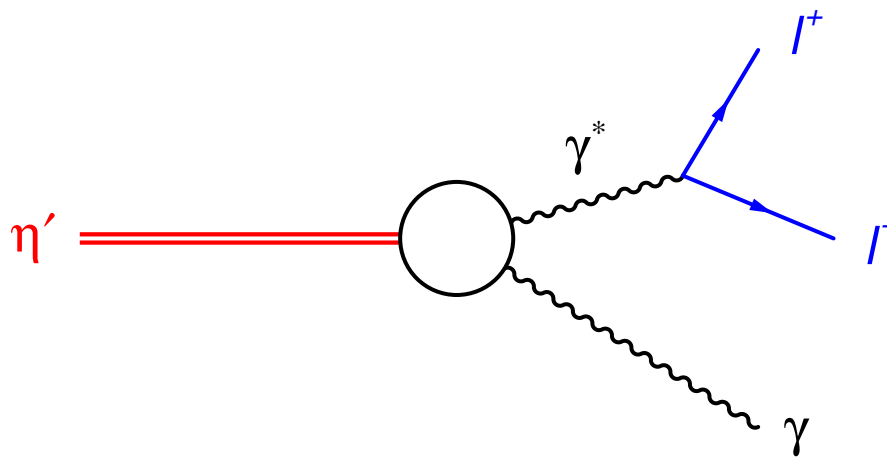
$$\text{BW}(\rho) = \frac{1}{(m_{12}^2 - m_\rho^2) - i m_{12} \Gamma_\rho} + \frac{\xi}{m_{\eta'}^2} \exp(i\phi)$$

⇓ *A. Abele et al. (Crystal Barrel),*  $\xi = 0.4, \phi = 3.14$   
Phys. Lett. B 402 (1997) 195



# $\eta'$ Transition Form Factor

# Conversion Decays



*probe  
spatial distribution  
of meson matter*

observable:  $l^+l^-$  mass distribution

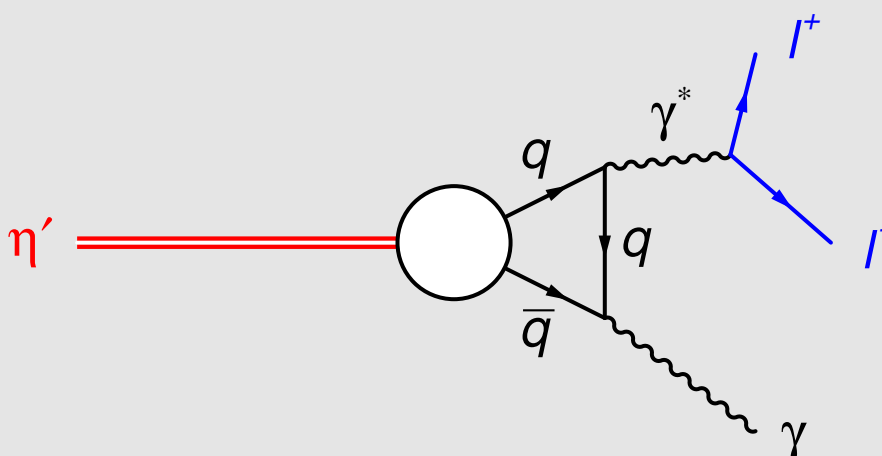
for  $\eta$ : J. Stepaniak et al.,  
Phys. Scripta T99 (2002) 133

Calculations:

VMD

Quark  
Triangle Loop

ChPT

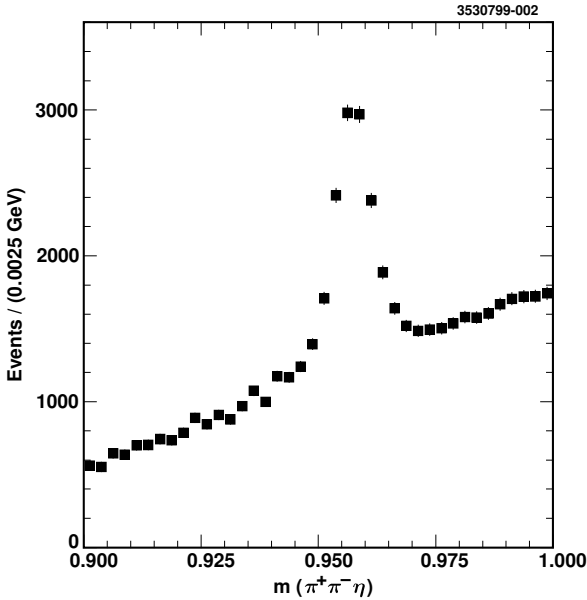
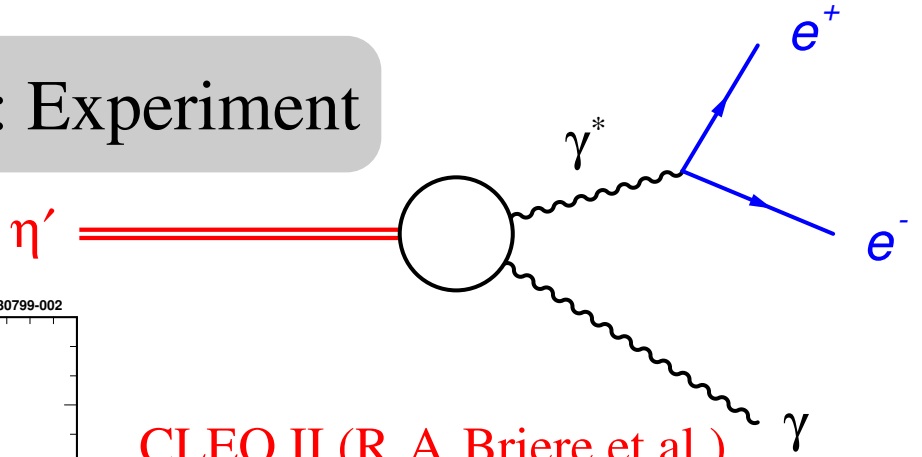


*probe  
qq coupling of  
 $\eta'$*

for  $\eta$ : L. Ametller et al.,  
Nucl. Phys. 228 (1983) 301

$$F_{\eta}(q^2) = \frac{\sum_q (g_{Pq\bar{q}}/m_q) Q_q^2 f(q^2, m_q, m_{\eta})}{\sum_q (g_{Pqq}/m_q) Q_q^2}$$

# $\eta'$ Dalitz Decay: Experiment

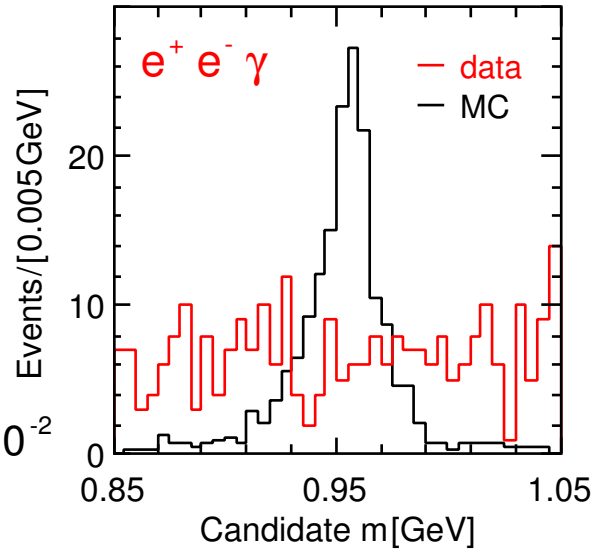


CLEO II (R. A. Briere et al.)

Phys. Rev. Lett. 84 (2000) 26

→ 6700 events

→  $BR(\text{exp}) < 0.9 \times 10^{-3}$



expected branching ratio

$$\frac{BR(\eta \rightarrow e^+ e^- \gamma)}{BR(\eta \rightarrow \gamma \gamma)} \approx 0.015 \quad BR(\eta' \rightarrow \gamma \gamma) = 2.1 \times 10^{-2}$$

$$\rightarrow BR(\eta' \rightarrow e^+ e^- \gamma) \approx 3 \times 10^{-4}$$

expected counting rate WASA@COSY  $\approx$  130 events/day

( $BR = 0.9 \times 10^{-3}$ )

experimental conditions and background

for  $\eta$ : J. Stepaniak et al.,

Phys. Scripta T99 (2002) 133

$e^\pm \leftrightarrow \mu^\pm, \pi^\pm$  misidentification  $\approx 10^{-3}$

$l^+ l^-$  mass resolution  $\approx 2.5\%$

admixture  $pp \rightarrow pp\pi^0\pi^0 \rightarrow ppe^+e^- \gamma(\gamma) < 1\%$

admixture  $pp \rightarrow pp\eta' \rightarrow pp\gamma\gamma \rightarrow pp\gamma e^+ e^-$  negligible



# Physics Issues In $\eta'$ Decays

*Charge Symmetry Breaking*

*Pseudoscalar Nonet Parameters*

*Nature of the  $\eta'$*

*QCD Anomalies*

*Scalar Meson Exchange*

*Tests of ChPT Predictions*

