# The Scalar Resonances $a_0/f_0(980)$ at COSY

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Abstract. Fundamental properties of the scalar resonances  $a_0/f_0(980)$ , like their masses, widths and couplings to  $K\bar{K}$ , are poorly known. In particular, precise knowledge of the latter quantity would be of great importance since it can be related to the  $K\bar{K}$  content of these resonances.

An experimental program is under way at COSY-Jülich aiming at the extraction of the isospin violating  $a_0/f_0$  mixing amplitude  $\Lambda$  which is in leading order proportional to the product of the coupling constants of the  $a_0$  and  $f_0$  to kaons.  $a_0/f_0$  production is studied in *pp*, *pn* and *dd* interactions, both for the  $K\bar{K}$  and the  $\pi\eta/\pi\pi$  decays, using the ANKE and WASA spectrometers. The latter will be available for measurements at COSY in 2007.

As a first step, isovector  $K\bar{K}$  production has been measured in the reaction  $pp \rightarrow dK^+\bar{K^0}$ . The data reveal dominance of the  $a_0^+$  channel, thus demonstrating the feasibility of scalar meson studies at COSY. Analyses of  $K\bar{K}$ - and  $\bar{K}d$ -FSI effects yield the corresponding scattering lengths,  $a(K\bar{K})_{I=1} = -(0.02 \pm 0.03) - i(0.61 \pm 0.05)$  fm and  $|\text{Re } a(\bar{K}d)| \le 1.3$  fm, Im  $a(\bar{K}d) \le 1.3$  fm.

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#### THE LIGHT SCALAR RESONANCES

QCD is the fundamental theory of the strong interactions. How quarks and gluons are bound into hadrons is a yet unsolved strong coupling problem. QCD can be treated explicitly in this regime using lattice techniques [1], which are, however, not yet in the position to make quantitative statements about the light scalar mesons. Alternatively, QCD-inspired models, which employ effective degrees of freedom, can be used. The constituent quark model is one of the most successful in this respect (see *e.g.* [2]). However, more states with quantum numbers  $J^P=0^+$  have been identified experimentally than would fit into a single SU(3) scalar nonet: the  $f_0(600)$  (or  $\sigma$ ),  $f_0(980)$ ,  $f_0(1370)$ ,  $f_0(1500)$  and  $f_0(1710)$  with I=0, the  $\kappa(800)$  and the  $K^*(1430)$  (I=1/2), as well as the  $a_0(980)$  and  $a_0(1450)$  (I=1) [3]. Consequently, the  $a_0/f_0(980)$  have been associated with crypto-exotic states like  $K\bar{K}$  molecules [4] or compact  $qq-\bar{q}\bar{q}$  states [5].

In the sixties Weinberg suggested how to decide whether a (stable) particle is composite or elementary [6]. The formalism was applied to the deuteron and it was shown that it is not an elementary particle but made of a proton and a neutron. Baru *et al.* [7] have extended Weinberg's approach to the (unstable)  $a_0/f_0(980)$  and find evidence for significant mesonic components in these states. From the formalism in Ref. [7] it follows that precise knowledge of the resonance parameters, in particular the coupling constants of the  $a_0$  and  $f_0$  to kaons, would allow one to model independently determine the  $K\bar{K}$ content of the  $a_0/f_0$ . However, the values for  $g_{a_0K\bar{K}}$  and  $g_{f_0K\bar{K}}$  are still poorly known and range from 0.224 to 0.834 and from 1.31 to 2.84, respectively [8] — depending on the fitted Flatté parameterizations of measured  $\pi\eta/\pi\pi$  and  $K\bar{K}$  spectra.

## **EXPERIMENTAL PROGRAM AT COSY**

An experimental program is under way at COSY-Jülich aiming at the extraction of the isospin-violating (IV)  $a_0/f_0$  mixing amplitude  $\Lambda$  which is in leading order proportional to the product of  $g_{a_0K\bar{K}}$  and  $g_{f_0K\bar{K}}$  [9, 10].  $a_0/f_0$  production has been or will be studied in *pp*, *pn* and *dd* interactions, both for the  $K\bar{K}$  and the  $\pi\eta/\pi\pi$  decay channels [11]. While decay channels with at least one charged kaon can well be investigated with the magnetic spectrometer ANKE ("Apparatus for the detection of Nucleonic and Kaon Ejectiles"), the  $\pi\eta$  and  $\pi\pi$  final states will be measured with WASA ("Wide Angle Shower Apparatus") which will be available for measurements at COSY in 2007 [12].

# **Isospin filters and violation**

A  $pp \rightarrow dX$  reaction must lead to  $a_0^+$  (*I*=1) production, a  $pn \rightarrow dX$  interaction is not isospin selective, whereas the  $dd \rightarrow \alpha X$  reaction — neglecting the small IV contributions which are the final goal of the proposed experimental program — is a filter for the  $f_0$  (*I*=0) resonance, since the initial deuterons and the  $\alpha$  particle in the final state have isospin *I*=0 ("isospin filter").

Since at COSY it is possible to fix the initial isospin one can selectively produce the  $a_0$  or  $f_0$  resonances and can identify observables that vanish in the absence of IV. The idea behind the proposed experiments is the similar to recent measurements of IV effects in the reaction  $dd \rightarrow \alpha \pi^0$  [13]. However, the interpretation of the signal from the scalar mesons is much simpler as compared to the pion case. Since the  $a_0$  and the  $f_0$  are rather narrow overlapping resonances, the  $a_0$ - $f_0$  mixing in the final state is enhanced by more than an order of magnitude compared to IV in the production operator (*i.e.* "direct" IV  $dd \rightarrow \alpha a_0$  production) and should give the dominant contribution to the IV effect via the reaction chain  $dd \rightarrow \alpha f_0(I=0) \rightarrow \alpha a_0^0(I=1) \rightarrow \alpha (\pi^0 \eta)$  [10, 14].

Any observation of  $\pi^0 \eta$  production in the  $dd \rightarrow \alpha X$  reaction is a direct indication of IV and the cross section  $d\sigma/dm_{\pi\eta}$  is given by the product of the mixing amplitude  $\Lambda(m)$  and the  $dd \rightarrow \alpha f_0$  production operator. It is therefore compulsory to determine the latter in an independent measurement in order to extract the mixing amplitude. A corresponding measurement of the  $dd \rightarrow \alpha (K^+K^-)_{I=l=0}$  cross section is foreseen for winter 2005/06 at ANKE. These data, together with the information on the  $dd \rightarrow \alpha (\pi^0 \eta)$ reaction from WASA will allow one to determine the  $a_0$ - $f_0$  mixing model independently.

## First measurements with ANKE: isovector $K\bar{K}$ production

As a first measurement, the production of  $K\bar{K}_{I=1}$  pairs has been investigated in the reaction  $pp \rightarrow dK^+\bar{K}^0$  at excitation energies  $Q_{K\bar{K}} = 48$  and 105 MeV. This reaction has the advantage of lower background as compared to dd scattering, a  $K\bar{K}$  production cross section which is expected to be ~100 times larger, and the fact that admixtures of I = 0 components are forbidden by charge conservation. So far, in pp collisions the  $a_0(980)$  production has been measured at  $p_p = 450$  GeV/c via  $f_1(1285) \rightarrow a_0^{\pm} \pi^{\mp}$ 



**FIGURE 1.** Left:  $K^+\bar{K}^0$  mass distribution from the reaction  $pp \to dK^+\bar{K}^0$  measured at an excitation energy of Q = 48 MeV with ANKE [18]. The solid line shows a fit to the data from which the imaginary part of the isovector  $K\bar{K}$  scattering length has been determined [22]. Right: Plot of  $Re(a_1)$  (filled circles) *vs.* the dimensionless parameter  $\alpha = 2\varepsilon_0/\Gamma_{\pi\eta}$ . The error bars show the errors introduced into  $\alpha$  and  $Re(a_1)$  by the uncertainties in the associated  $a_0(980)$  mass values.

decays [15] and in inclusive measurements of the  $pp \rightarrow dX^+$  reaction at  $p_p = 3.8$ , 4.5, and 6.3 GeV/c [16]. The best data so far on the  $K\bar{K}_{I=1}$  decay mode of the  $a_0$  have been obtained with Crystal Barrel at LEAR, with a mass resolution of  $\delta(m_{K\bar{K}}) \approx 20$  MeV [17].

A model-independent analysis of the ANKE angular distributions at Q = 48 MeV shows dominance of an *s*-wave between the two kaons accompanied by a *p*-wave deuteron with respect to the mesons. This has been interpreted as dominant production via the  $a_0(980)$  channel near threshold [10, 18]. Model calculations of the reaction  $pp \rightarrow dK^+\bar{K}^0$  performed by Grishina *et al.* [19] confirm this conclusion. In particular, the non-resonant (*p*-wave)  $K^+\bar{K}^0$  production is shown to be small for excess energies *Q* less than ~ 100 MeV.

In principle, the  $dK^+\bar{K}^0$  final state is sensitive to three FSIs,  $dK^+$ ,  $d\bar{K}^0$  and  $K^+\bar{K}^0$ . The former is known to be small and can be neglected for the extraction of the latter two. The FSI in the  $\bar{K}d$  system reduces the cross section, but leaves the invariant mass distributions virtually unaffected [19]. Sibirtsev *et al.* [20] have extracted limits for the  $\bar{K}d$  scattering length from the ANKE data [18] and found  $|\text{Re } a(\bar{K}d)| \le 1.3$  fm, Im  $a(\bar{K}d) \le 1.3$  fm. A recent study [21] based on this formalism finds an optimal fit to the COSY data for a purely imaginary  $d\bar{K}$  scattering length of  $a_{d\bar{K}} = (0.0 + i1.0)$  fm.

The ANKE experiment has achieved a resolution of 1-8 MeV for the invariant  $K\bar{K}$  mass-spectrum (see Fig. 1) which is considerably better than in previous measurements. The relatively small influence of the antikaon-deuteron FSI on the shape of the measured invariant mass distributions as indicated in Refs. [19, 20, 21] allows one to determine the  $K\bar{K}$  scattering length by a fit to the measured mass spectrum assuming that the deuteron's role is that of a spectator [22].

In Ref. [22] it has been assumed that  $K^+\bar{K}^0$  production in  $pp \to dK^+\bar{K}^0$  is dominated by FSI in the meson-meson channels only via the resonant intermediate mode  $\pi^+\eta \to$   $a_0^+ \to K^+ \bar{K}^0$ . Then the cross section is proportional to the I = 1,  $I_3 = +1$  cross section  $\sigma(\pi^+ \eta \to K^+ \bar{K}^0)$  and the *s*- (*p*-)wave contributions to the cross section can be expressed as

$$\frac{\mathrm{d}\sigma^{(s)}}{\mathrm{d}m_{K\bar{K}}} = C_s \frac{k\Delta t}{p^2} [1 + 2Im(a_1)k] \quad \text{and} \quad \frac{\mathrm{d}\sigma^{(p)}}{\mathrm{d}m_{K\bar{K}}} \approx C_p \frac{k^3\Delta t}{p^2} \tag{1}$$

with overall normalizations  $C_{s,p}$ , and factors k,  $\Delta t$  and p which are given by the reaction kinematics. A fit to the data (solid lines in Fig. 1) yields for the imaginary part of the scattering length  $Im(a_1) = -(0.61 \pm 0.05)$  fm at  $\chi^2_{min} = 0.81$  [22].

The spectator model only fixes the imaginary part of the scattering length. In order to determine  $Re(a_1)$  one has to introduce further assumptions regarding the structure of the  $K\bar{K}$  scattering amplitude in the isovector channel. If one expresses the  $a_0(980)$ mass distribution by the Flatté formula, there is a linear relation between the real and imaginary parts of the scattering lengths,  $Re(a_1) = Im(a_1)\alpha$  with  $\alpha = 2\varepsilon_{a_0}/\Gamma_{\pi\eta}$ .  $\varepsilon_{a_0}$  is the binding energy  $M_{a_0}$  relative to the  $K\bar{K}$  threshold and  $\Gamma_{\pi\eta}$  the  $a_0(980)$  partial decay width. If one takes  $Im(a_1) = -0.61$  fm from the spectator model fit, this fixes the slope of the straight line in a  $Re(a_1)$ -vs.- $\alpha$  plot, see right hand side of Fig. 1. The result can then be compared with the values of  $Re(a_1)$  and  $\alpha$  extracted from data obtained at other experiments [8, 22]. This comparison is also shown in Fig. 1. The spectator model fit is seen to be consistent with all of the data once the uncertainties in  $\alpha$  and hence  $Re(a_1)$ due to the experimental error in the  $a_0(980)$  mass are taken into account.

By assuming scale invariance of Flatté distributions [8], one can infer a value for  $\alpha$  by calculating the mean of the  $\alpha$ 's shown in Fig. 1,  $\alpha_c = 0.031 \pm 0.054$ . Inserting this estimate one obtains  $Re(a_1) = -(0.02 \pm 0.03)$  fm. The final result for the extracted isovector scattering length thus reads

$$a_1 = -[(0.02 \pm 0.03) + i(0.61 \pm 0.05)] \text{fm} \,. \tag{2}$$

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